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**Maximum-information photoelectron metrology**

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Photoelectron interferograms, manifested in photoelectron angular distributions (PADs), are high-information, coherent observables. In order to obtain the maximum information from angle-resolved photoionization experiments it is desirable to record the full, three-dimensional (3D), photoelectron momentum distribution. Here we apply tomographic reconstruction techniques to obtain such 3D distributions from multiphoton ionization of potassium atoms, and fully analyze the energy and angular content of the 3D data. The PADs obtained as a function of energy indicate good agreement with previous 2D data and detailed analysis [Hockett *et al.*, *Phys. Rev. Lett.* **112**, 223001 (2014)] concerning the main spectral features, but also indicate unexpected symmetry breaking in certain regions of momentum space, thus revealing additional continuum interferences which cannot otherwise be observed. These observations reflect the presence of additional ionization pathways and, most generally, illustrate the power of maximum-information measurements of coherent observables for quantum metrology of complex systems.

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**I. INTRODUCTION**

Interferometric measurements are the gold standard in metrology, since they offer observables of high precision and information content, which can be used to glean detailed understanding of underlying physical processes. In particular, interference patterns can be used to obtain the relative phase(s) of contributing waves, quantities which provide key physical insights in general, and in particular provide a window into underlying quantum mechanical phenomena. One specific and well-known example is the wave nature of a free electron, as verified by Young's double-slit-type experiments. In such experiments, a particle described by a plane wave impinges on two slits in an otherwise opaque barrier, resulting in a more complex wave pattern described by two transmitted spherical wave fronts. These wave fronts interfere with each other, leading to a characteristic interference pattern. In this case, the relative phase of the spherical wave fronts depends on the distance from the slits, and this geometric phase manifests as a spatial dependence of the observed interferogram.

The process of atomic or molecular photoionization is conceptually similar, and has long been discussed in terms of interfering wave fronts [1,2], but is in general significantly more complex. An illustrative example is the photoionization of H<sub>2</sub>, the "simplest double slit" [3]. In this case, following single-photon absorption, the photoelectron wave function can be considered as a superposition of two indistinguishable spherical waves, launched from the two atomic sites

upon photoabsorption. The observable photoelectron flux, determined by the coherent square of the continuum wave function, exhibits a characteristic angular interference pattern in very close analogy with Young's double slit [1,3]. Another illustrative example is Young's double slit in the time domain, which has been demonstrated by atomic ionization via a coherent two-pulse laser sequence, resulting in an interference pattern in the photoelectron energy distribution [4,5]. In this case the temporal evolution of the interferogram responds to the relative phase of the laser pulses, which can be controlled via their temporal separation, and is ultimately transferred to the photoelectron wave function.

For more complex light-matter systems the continuum wave function is described by a superposition of many constituent *partial waves* of differing character, correlated with the various ionization pathways accessed, and the simple analogy with Young's double slit fails. Despite this complexity, the resulting photoelectron flux, measured spatially, remains, in essence, a self-referencing angular interferogram of the continuum wave function. In this light, measurements of the energy and angle-resolved photoelectron flux, i.e., the three-dimensional (3D) photoelectron momentum distribution, are particularly powerful, since they provide a phase-sensitive metrology of the continuum wave function and the scattering event (photoionization) which gave rise to this wave. For example, photoelectron interferograms have been used to obtain complete information on the scattering wave function for both atoms and molecules [6–10]; to investigate electron correlation and entanglement in multiple ionization [3,11]; and in the related context of photoelectron diffraction [12] and photoelectron holography [13,14], wherein intense laser

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fields are used to drive rescattering of continuum waves from the photoion and, in the case of holography, additional interferences between direct (reference) and the rescattered continuum waves are observed. Furthermore, in time-dependent cases, the continuum wave function will respond to the underlying dynamics of the ionizing system, for instance evolving electronic or nuclear configurations [15–19], which may in turn depend on the properties of the laser pulse(s) applied and even allow for control [20,21]. It is also of note that the scattering phase accumulated by the partial waves is correlated, in the time domain, with the relative ionization time delay, often termed the Wigner delay [22,23]. In short, photoelectron interferograms are remarkably versatile and rich, with many existing and potential applications.

The last decade has seen a surge in “users” of photoelectron interferograms, and as many types of experimental study [24]. While this popularity is in part due to the versatility of the measurement, it is largely due to the proliferation of photoelectron imaging techniques. In particular *velocity-map imaging* (VMI), since a basic VMI apparatus offers a robust and simple experimental configuration for measuring photoelectrons. However, in the majority of cases the use of standard VMI methodologies means that measurements are restricted to 2D projections of the full 3D momentum distribution [25–27]. Although 2D projections of any arbitrary 3D distribution may be measured and interpreted phenomenologically, the resulting loss of dimensionality means that only cylindrically symmetric distributions can be quantitatively analyzed [27,28]. This further limits the information extractable from the 2D data and, more fundamentally, the type of experimental studies possible. While it is trivial to state that 3D measurements offer a higher information content than 2D measurements, the restrictions inherent to 2D measurements are highly detrimental to the understanding of the photoelectron interference pattern and the concomitant ability to use subtle changes in this pattern as a probe of the underlying quantum mechanics. This statement becomes more applicable as the complexity of the light-matter interaction grows and the number of interfering pathways increases; for instance, ionization with polarization-shaped laser pulses, where highly structured, noncylindrically symmetric, photoelectron distributions are the norm [20,21].

Figure 1 illustrates some of these concepts in photoelectron interferometry and imaging, with an example angular interferogram  $I(\theta, \phi)$ , representations in velocity space for [Fig. 1(b)] narrow and [Fig. 1(c)] broad energy distributions, and [Fig. 1(d)] 2D projections of (c) onto various image planes. The details of these calculations are discussed further below, but we note here that in this particular case only the 2D projection in the  $(X, Y)$  plane reveals the noncylindrically symmetric nature of the distribution, and this key information is lost in the other projections. While the precise details of the information loss depend on the initial distribution and the geometry of the measurement, this result is applicable to all cases in which the symmetry is broken in the plane of polarization, e.g., ionization with elliptically polarized or polarization-shaped laser pulses. Because this plane is orthogonal to the beam propagation direction it would not be possible to measure in a standard VMI configuration.

In recent work (Refs. [21,29]), we explored a relatively complex ionization process: a net three-photon ionization of

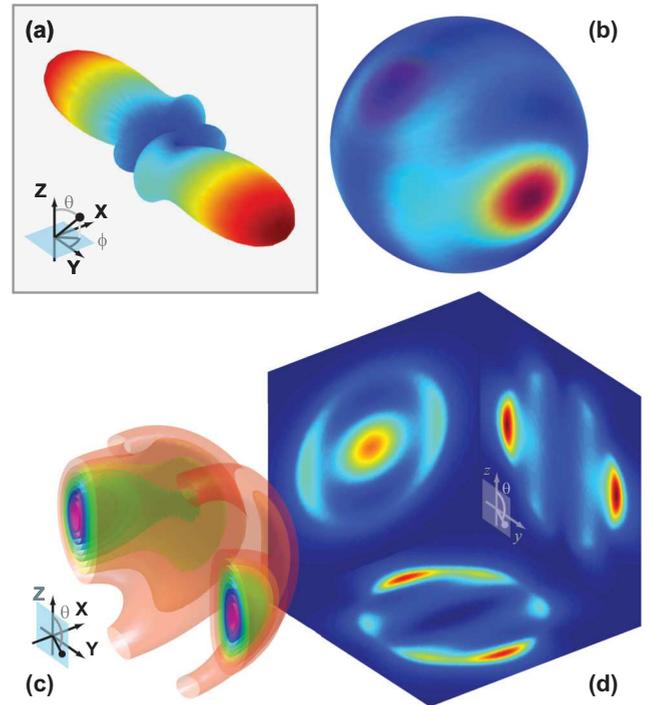


FIG. 1. (Color online) Concepts in photoelectron interferometry and imaging. (a) Example photoelectron interferogram in angular space,  $I(\theta, \phi)$ , plotted in polar form. (b) Same angular interferogram as (a), projected onto the surface of a Newton sphere (velocity isosphere), as it would appear spatially in an ionization experiment for a single photoelectron energy  $k$ . (c) Volumetric representation of the angular interferogram (a) in velocity space (shown only for one hemisphere), assuming a Gaussian energy envelope. This is essentially a set of nested Newton spheres (b), now plotted as flux isosurfaces, and the full distribution is denoted  $I(\theta, \phi, k)$ . (d) 2D images of the photoelectron flux (c), simulating a velocity-map imaging measurement. The interferogram illustrated is the theoretical result of three-photon ionization of potassium with elliptically polarized light (see Sec. II for further details), where the laser propagates along the  $Z$  axis, and the polarization ellipse lies in the  $(X, Y)$  plane with ellipticity defined by a spectral phase  $\phi_y = 0.5$  rad (see Sec. III D for details).

potassium atoms using moderately intense 800 nm light and a range of polarizations from linear to circular, and fully polarization-shaped pulses. We made use of measurements of 2D photoelectron momentum distributions, combined with the calculation of 2D photoelectron interferograms (including intrapulse electronic dynamics, driven by the instantaneous pulse polarization) and a fitting procedure, in order to determine the full set of contributing partial-wave magnitudes and phases. Perhaps surprisingly, this analysis allowed for “complete” details of the photoionization event in terms of the contributing pathways to this particular photoelectron interferometer, despite the restrictions of the 2D data, but it was concluded that application to more complex cases would likely require the additional level of detail available from 3D data; in this work we explore the capabilities gained from measurement of full 3D photoelectron distributions created by the same ionization scheme. Measurements are made using a standard 2D VMI setup, and combined with tomographic reconstruction

to provide full 3D metrology. With the 3D measurements we are additionally able to (a) observe noncylindrically symmetric distributions directly (Sec. III A) [30]; (b) quantitatively analyze these distributions as a function of energy (Sec. III C); and, consequently, (c) compare these results directly with calculations based on the previously determined photoionization dynamics (Sec. III D); (d) investigate unexpected symmetry breaking which was obscured in the 2D measurements, but is clear in the 3D distributions, and directly reflects additional ionization pathways contributing to the photoelectron interferogram (Sec. IV). All of these aspects serve to highlight the power of full 3D photoelectron interferograms and provide a general *maximum-information methodology* for analysis of these measurements, as demonstrated by the insights obtained into this complex light-matter interaction.

## II. PHOTOELECTRON METROLOGY

In this work ionization of potassium atoms with a single  $\sim 30$  fs IR laser pulse was investigated. This provides the specific light-matter system we use to illustrate the concepts of maximum-information photoelectron metrology. As noted above, interaction of moderately intense ( $10^{12}$ – $10^{13}$  W cm $^{-2}$ ) light near 800 nm results in a net three-photon ionization process. More specifically, the process can be considered in terms of a strongly coupled, bound-bound  $4s + h\nu \rightarrow 4p_{\pm 1}$  transition at the one-photon level, followed by a much weaker,

two-photon ionizing transition  $4p_{\pm 1} + 2h\nu \rightarrow |k, l, m\rangle$ , where the continuum states are labeled by photoelectron energy  $k$  and (orbital) angular momentum  $l$  with projection  $m$  on the  $Z$  axis. Because the bound-bound transition is near resonant at 800 nm, and carries significant oscillator strength, Rabi oscillations are driven; these intrapulse electronic population dynamics play a significant role in the final photoelectron interferogram. Furthermore, since the polarization of the laser pulse affects both the population dynamics and the ionization dynamics, the final continuum state populated is sensitive to the pulse polarization. In effect, the polarization of the light controls the photoionization interferometer, and finer control can be gained via the use of polarization-shaped pulses, which have a polarization state that evolves over the pulse envelope. This process serves to represent a typical, complex, light-matter interaction in the sense discussed above: many partial waves contribute to the final continuum state; electronic dynamics play a significant role; the interaction is sensitive to controllable experimental parameters, as well as the inherent physical properties of the ionizing system. As described above, in this work we are concerned with the additional insight available from 3D measurements, so the reader is referred to Refs. [21,29] for full details of the ionization process, including the ionization pathways, angular momentum coupling diagrams, and the full theoretical treatment.

In order to develop a maximum-information methodology for photoelectron interferograms we make use of three key

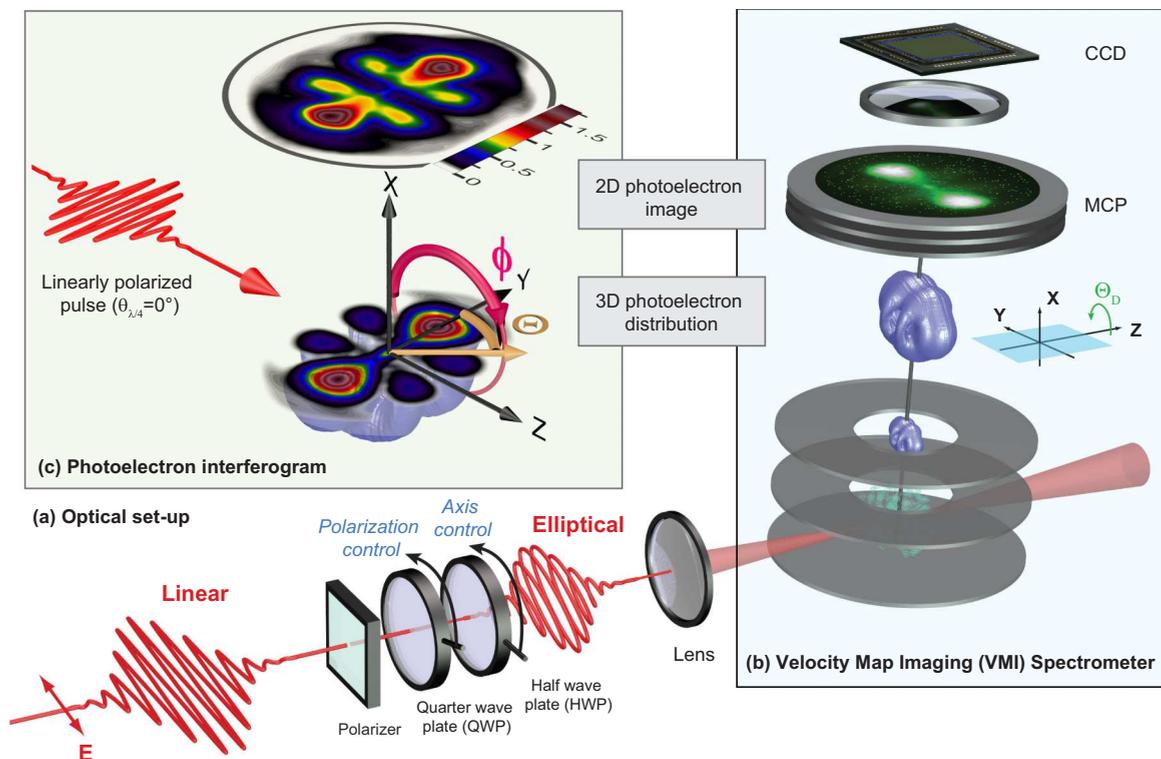


FIG. 2. (Color online) Experimental setup for photoelectron imaging and tomography. (a) Optical setup. The polarization state of the incident light is controlled via a quarter-wave plate (QWP) and rotation relative to the detector plane via a half-wave plate (HWP). (b) Velocity-map imaging. Potassium atoms are ionized, and the resulting photoelectron distribution is projected onto a microchannel plate (MCP) assembly, allowing 2D images to be recorded. (c) Photoelectron interferogram measured for ionization with a linearly polarized pulse, leading to a cylindrically symmetric distribution. The 2D projection shows an experimental photoelectron image on the  $(Y, Z)$  detector plane, and the 3D distribution reconstructed from this. This case can be contrasted with the noncylindrically symmetric example shown in Fig. 1.

elements: (1) sets of 2D VMI measurements, (2) tomographic reconstruction techniques, and (3) detailed analysis of the radial and angular content of the resulting 3D data, with a particular focus on the angular photoelectron flux. Each of these aspects is detailed below, and the data are presented in Sec. III.

### A. Experimental setup

The experimental setup is illustrated in Fig. 2. Herein we describe the salient details, and the reader is referred to Refs. [20] and [31] for a more detailed description. In brief, femtosecond laser pulses of 27 fs pulse duration [full width at half maximum (FWHM) of the intensity profile] centered at 795 nm with a pulse energy of 800  $\mu\text{J}$  are provided by an amplified 1 kHz Ti:sapphire laser system (Femtolasers model Femtopower Pro). The laser beam is focused with a lens of 200 mm focal length into potassium vapor supplied by an alkali-metal dispenser source. A mean focal spot size radius of about 22  $\mu\text{m}$  ( $1/e^2$  of intensity profile) was obtained and measured with a beam-profiling CCD camera. At a pulse energy of 7.8  $\mu\text{J}$  this leads to a peak intensity of about  $4 \times 10^{13} \text{ W cm}^{-2}$  assuming Gaussian profiles in time and space.

We use a home-built velocity-map imaging spectrometer [25] to record 2D photoelectron images, illustrated in Fig. 2. The imaging assembly consists of a chevron microchannel plate (MCP) detector with a phosphor screen deposited on a fiber optic (SI-Instruments GmbH model S3075-10-I60-PS-FM). A 10-bit CCD camera with  $1.4 \times 10^6$  pixels (Lumenera Corporation model Lw165m) is used to image the signals on the phosphor screen. The energy resolution of the VMI spectrometer in the present measurements is better than 80 meV (FWHM) at an energy of about 0.5 eV.

The polarization of the initial laser pulses is linear, with the polarization axis perpendicular to the spectrometer axis and coplanar to the detector surface, as shown in Fig. 2. We use a dichroitic visible-IR (VIS-IR) polarizer (CODIXX) to clean up the linear polarization. An achromatic quarter-wave plate (QWP) (B. Halle Nachfl.) is placed after this polarizer to generate different polarization states with an adjustable amount of circularity. The polarization states are therefore defined by the QWP rotation angle  $\theta_{\lambda/4}$ , where  $\theta_{\lambda/4} = 0^\circ$  corresponds to linearly polarized light,  $\theta_{\lambda/4} = 45^\circ$  to circularly polarized light, and all values in between to elliptically polarized pulses. The ellipticities of the laser pulses are defined as the ratio of the minor to major axes of the polarization ellipse; hence  $\varepsilon = 0$  for linearly polarized light and  $\varepsilon = 1$  for pure circularly polarized light. Herein we present data for three polarization states defined by  $\theta_{\lambda/4} = 0^\circ$  (linear polarization),  $15^\circ$ , and  $30^\circ$  (elliptically polarized states). The corresponding Stokes vectors, denoted  $S(\theta_{\lambda/4})$ , and ellipticities  $\varepsilon(\theta_{\lambda/4})$  are given in Table I, where the Stokes parameters were measured experimentally using the method of Ref. [32] (further details can be found in Ref. [31]). In this work only the ellipticities are of fundamental importance, and hereafter the three polarization states are denoted  $\varepsilon_1$ ,  $\varepsilon_2$ , and  $\varepsilon_3$ , respectively. Although the Stokes parameters indicate a slight rotation of the polarization ellipse as a function of  $\theta_{\lambda/4}$  (relative to the laboratory-frame  $Y$  axis defined in Fig. 3), this rotation does

TABLE I. Polarization states used in this work, defined by the QWP rotation angle  $\theta_{\lambda/4}$ , and corresponding Stokes parameters and ellipticities.

Label	QWP $\theta_{\lambda/4}$	Stokes $S$	Ellipticity $\varepsilon$
$\varepsilon_1$	$0^\circ$	(1, 1.00, 0.04, 0.00)	0
$\varepsilon_2$	$15^\circ$	(1, 0.76, 0.43, 0.49)	$\approx 0.27$
$\varepsilon_3$	$30^\circ$	(1, 0.28, 0.39, 0.88)	$\approx 0.58$

not affect the photoelectron distributions beyond a trivial frame rotation, and was removed during data processing (although it is present in the raw data shown in Fig. 3).

To record different 2D projections of the photoelectron distribution, an achromatic half-wave plate (HWP) (B. Halle Nachfl.) is utilized after the QWP. This HWP provides control over the polarization axes of the incoming light, and hence the rotation of the 3D photoelectron distribution relative to the detector plane. This rotation angle is defined as  $\Theta_D$ ,

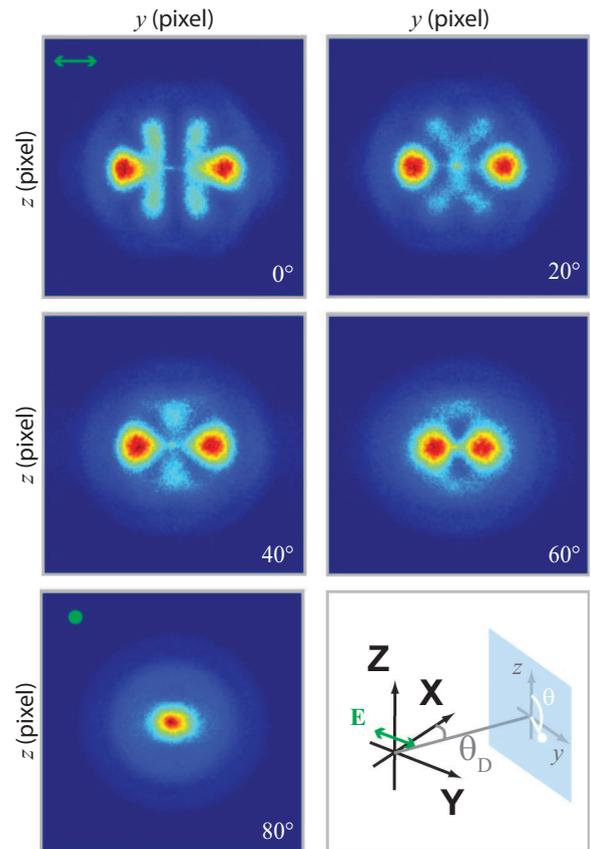


FIG. 3. (Color online) Experimental data for photoelectron tomography. Panels show examples of raw photoelectron images for different projection angles  $\Theta_D$  onto the 2D imaging detector, following the coordinate system illustrated in the bottom right panel. The raw images were obtained with linearly polarized light ( $\varepsilon_1$ ), and the frame rotation from top to bottom corresponds to a rotation of the detection plane ( $y, z$ ) from  $(Y, Z)$  ( $\Theta_D = 0^\circ$ ) to  $(X, Z)$  ( $\Theta_D = 90^\circ$ ), with behavior similar to that in the calculated case shown in Fig. 1(d) for an elliptically polarized ionizing pulse.

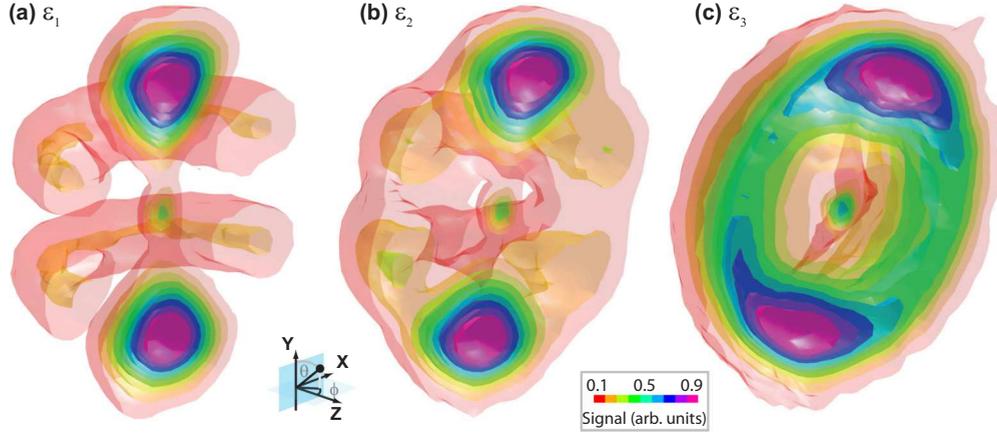


FIG. 4. (Color online) Experimental 3D photoelectron images for three polarization states. (a) Linearly polarized light ( $\varepsilon_1$ ); (b),(c) elliptically polarized light  $\varepsilon_2$  and  $\varepsilon_3$ , respectively (see Table I). To reveal the details in the plane of polarization, the distributions are sliced in the  $(X,Y)$  plane, plotted for only one hemisphere, and the coordinate frame rotated as indicated in the figure; the isosurfaces are plotted for 10%–90% signal levels.

where  $\Theta_D = 0^\circ$  for the case shown in Fig. 2, with the  $(Y,Z)$  plane parallel to the detector plane, and  $\Theta_D = 90^\circ$  for the case where the  $(X,Z)$  plane is parallel to the detector (see also Fig. 3). Photoelectron images are measured for a range of  $\Theta_D$ , and this series of projections is used to reconstruct the initial 3D distribution for each polarization state  $\varepsilon_n$ , as detailed in Sec. II B. For each  $\Theta_D$  images are integrated for approx. 30 000 laser pulses; under the conditions described above approx. 33 electrons are measured per pulse, resulting in a total electron count of approx.  $9 \times 10^5$  per 2D projection. Overall, each tomographic measurement includes approx.  $2.4 \times 10^6$  laser pulses and approx.  $8 \times 10^7$  electrons, and takes around 50 min. Due to the large number of electron counts in each measurement, statistical (Poissonian) uncertainties are negligible in these data, and are consequently not shown on the plots presented herein.

### B. Tomographic reconstruction

For each polarization state, photoelectron images were recorded for a set of projection angles  $\Theta_D$ , as described above. As illustrated in Figs. 1(c) and 1(d), each image is a 2D projection  $(y,z)$  of the original 3D velocity space  $(V_x, V_y, V_z)$ , where the lower-case coordinates  $(y,z)$  are defined in the detector plane and the upper-case coordinates  $(X,Y,Z)$  in the ionization frame, and the  $Z$  axis is chosen to coincide with the laser propagation axis. Raw experimental images are shown in Fig. 3 for a few values of  $\Theta_D$ . In this case, as distinct from the example shown in Fig. 1, the ionizing light was linear, and the full 3D distribution is cylindrically symmetric. Here the symmetry is clear for the  $\Theta_D = 0^\circ$  case, which shows a distribution with two intense poles aligned with the  $Y$  axis and band structure of lower intensity. As this distribution is rotated the poles, in 2D projection, appear to come closer to one another, and ultimately align for  $\Theta_D = 90^\circ$ . The band structure initially becomes more complex in projection, and at  $\Theta_D = 90^\circ$  appears as a weak, radially dependent feature dropping off from the central spot. (The reconstructed 3D distribution from this data is shown in Fig. 4.)

In the tomographic reconstruction procedure the images were stacked to form a data cube of dimensions  $(V_x, V_y, \Theta_D)$ , and an inverse Radon transform performed on each  $(V_y, \Theta_D)$  plane in the image stack to recreate the original  $(V_x, V_y, V_z)$  space. This procedure is equivalent to those detailed in Refs. [33–35], although the numerical details are slightly different. In this case, the reconstruction was performed in MATLAB (R2010a), see Ref. [36], using the built-in IRADON function. The input  $(V_x, V_y)$  images were cropped and down-sampled by a factor of 2 before reconstruction, yielding raw velocity-space images of  $251 \times 251$  pixels, and the inverse Radon transform included a Ram-Lak frequency filter with Hann windowing to remove high-frequency noise. Sets of images for  $\Theta_D = 0^\circ$  to  $90^\circ$ , in  $2^\circ$  steps, were used, resulting in image sets of 45 projections for each polarization state. Combined with the down-sampling, this resulted in a data cube  $(V_x, V_y, \Theta_D)$  of dimension  $251 \times 251 \times 45$ , and a reconstructed velocity space volume of dimension  $251 \times 251 \times 251$  voxels.

### C. Information content of 3D data

In the following we determine and discuss the details of the radial and angular components obtained from the 3D momentum data. Most generally, the distributions, in spherical polar coordinates, can be described by

$$I(\theta, \phi, k) = \sum_{L,M} \beta_{L,M}(k) Y_{L,M}(\theta, \phi). \quad (1)$$

Here the  $Y_{L,M}(\theta, \phi)$  are spherical harmonic functions and the  $\beta_{L,M}(k)$  are the anisotropy parameters, explicitly given as functions of energy. The experimental volumetric data can be expressed in terms of this characteristic expansion by defining a coordinate origin, converting the Cartesian volume  $(X,Y,Z)$  to a spherical-polar coordinate system  $(\theta, \phi, R)$ , then extracting radial slices, and, finally, determining the  $\beta_{L,M}(k)$  by fitting the radial slices with Eq. (1). Note that, since the raw radial spectrum recorded via a VMI experiment is linear in velocity space, it is nonlinear in energy space (because  $k \propto v^2 \propto R^2$ ). For simplicity of data analysis we therefore work primarily in

this linear space, defined in practice by CCD pixels and labeled by the arbitrary radial coordinate  $R$ , but use the notation  $\beta_{L,M}(k)$  in all cases. The  $\beta_{L,M}(k)$  thus determined constitute the full information content of the measurement, and fully characterize distributions such as the one shown in Fig. 1(c).

The radial spectrum, summed over all angles, corresponds to the photoelectron velocity (or energy) spectrum. This component is given by the  $\beta_{0,0}(k)$  parameters, or equivalently can be obtained by direct angular integration of the data:

$$I(k) = \iint I(\theta, \phi, k) \sin(\theta) d\theta d\phi. \quad (2)$$

The angular photoelectron interferograms  $I(\theta, \phi)$  at any given  $k$ , and hence the set of  $\beta_{L,M}(k)$  at any given  $k$ , depend on the composition of the continuum wave function, defined by the partial waves  $|l, m\rangle$ . Although the nature of the interferences and coupling is complicated (see Refs. [21,29]), in general the limits on  $L$  and  $M$  in this expansion depend directly on the continuum states populated, which depend in turn on both the characteristics of the ionizing radiation and the intrinsic properties of the ionizing system. These properties effectively determine the ionization pathways accessible, via the symmetry of the problem and coupling to the partial waves [9,24,37]; for example,  $L \leq 2l_{\max}$  and, in the case of linearly polarized light, only  $M = 0$  terms are allowed. The resulting interference pattern, at a single energy, is often termed the *photoelectron angular distribution* (PAD), as distinct from the radial component which reflects the photoelectron energy spectrum. It is important to note that the  $\beta_{L,M}(k)$  parameters cannot be determined from 2D images in general, due to the loss of information which occurs with projection of the full distribution on a 2D plane.

The exceptions to this are cylindrically symmetric ( $\phi$ -invariant) distributions, for which Abel-type inversion techniques can be employed [27]. Since cylindrical symmetry is maintained only for linearly or pure circularly polarized light ( $\varepsilon = 0$  or  $\varepsilon = 1$ ), this stipulation corresponds in practice to a restriction on the experiments possible and, ultimately, on the partial-wave interferences which can be observed [9,38]. This latter consideration provides a fundamental limit to the information content which can be quantitatively obtained from a 2D measurement.

### III. RESULTS AND ANALYSIS

#### A. 3D photoelectron momentum images

The images obtained experimentally are shown in Fig. 4. In the figure we show 3D isosurface renderings of the tomographically reconstructed distributions, equivalent to the computational result shown in Fig. 1(c). The distributions are sliced in the  $(X, Y)$  plane to reveal details of the radial (velocity) spectrum and highlight the angular structure of the signal in the polarization plane. The radial component of the images shows two features: a central spot, and a main radial feature which appears to have a Gaussian-like envelope. The angular component shows little clear structure for the central spot, and a complex multilobed structure over the main radial feature.

Broadly, the results over the main feature show the expected behavior as the polarization state of the light is changed, evolving from a distribution with primarily  $L = 3$  structure

(or  $f$ -like structure in the language of atomic orbitals [39]) in Fig. 4(a), to a more ringlike structure in Fig. 4(c). This general evolution with the laser polarization matches that seen in the 2D photoelectron images recorded at lower laser intensities and predicted theoretically (see Refs. [21,29]). There is little apparent change in the radial distribution with polarization, also as expected, although more careful analysis (see below) indicates this is not entirely true. The central spot was not observed in the previous 2D images, although such a feature is quite typical of VMI measurements and is usually assumed to indicate photoelectrons generated via many possible pathways to low- $k$  continuum states (e.g., field ionization of high-lying excited states). Such pathways may be laser-intensity and VMI-parameter dependent and have been exploited in “photoionization microscopy” studies [40,41], and more recently investigated in the context of strong-field atomic and molecular ionization [42,43]. In the former case, near-threshold ionization is analyzed in a joint atom–electric-field potential, leading to the formation of complex quasibound states; in the latter case, low- and zero-energy photoelectrons are associated with electron tunneling, followed by scattering and Coulomb focusing or recapture into high-lying Rydberg states, with subsequent field ionization of these states. Effectively, the same processes operate in both regimes, but the precise details vary with the strength of the laser field and the applied static fields. We do not consider these low-energy contributions further in this work.

In detail, the full 3D data begin to reveal additional information which can be inferred but not observed directly, in 2D projections. As noted above, this is particularly true for any structure in the  $(X, Y)$  plane—the plane of polarization of the laser pulse—which cannot be observed in a 2D image in standard VMI configurations (see Figs. 1 and 3). For the linearly polarized light the distribution is cylindrically symmetric so, as described above, there is nominally no loss of information in the 2D projections. This case does, however, serve as a good test of the tomographic reconstruction and an intuitive example, since the distribution is relatively simple and can be readily checked by eye against the 2D images. It is clear how the  $f$ -like structure, with intense polar lobes and two radial bands, can form the various projections shown in Fig. 3.

For the elliptically polarized cases the distributions are more interesting; of particular note is the rotation in the  $(X, Y)$  plane, which appears in the 2D images as a smearing of the features in the equatorial plane. In this case the rotation is somewhat trivial in origin, and simply due to the optical setup (as detailed in Sec. II A) which results in a slight reference-frame rotation for the elliptically polarized cases relative to the linear case. In the 3D data this effect can be clearly observed, understood, and removed in data analysis. However, it is clear that in a 2D measurement this kind of overlap or blurring will be present in any case where features overlap in projection, regardless of the experimental or physical origin of this overlap. This general effect was illustrated in detail above for the linear case (Fig. 3), where the effects of frame rotations on 2D projections are observed as the approach and overlap of the polar features as  $\Theta_D$  is increased. Obviously the magnitude of this effect, and the loss of detailed structure in the projections, will depend on the complexity and, especially, the width of the features.

Similarly, the loss of structure away from the  $(X, Y)$  plane can be inferred from a 2D projection as a narrowing of the observed distribution, but in the 3D case the persistence of the lobe pattern in plane can be observed. In all cases, the potential for the conflation of (trivial) experimental with physically interesting effects is high, and detrimental to detailed analysis and fundamental insight.

Although visually arresting and phenomenologically useful, direct consideration of the isosurface plots provides only a cursory overview of the data, and does not clearly reveal minor contributions to the photoelectron interferograms. In the following sections, a more careful quantitative analysis of these data is reported in order to provide more detail and ultimately give physical insight into these 3D interferograms [44].

### B. Radial spectra

The radial spectra extracted from the volumetric data are shown in Fig. 5. As expected from the full 3D plots of Fig. 4, there is little difference in the overall structure of the distributions with polarization state. However, there is a clear double peak, with a splitting of  $\sim 270$  meV. The ratio of the peaks forming this doublet varies as a function of polarization, with a slight dominance of the lower-energy feature observed for  $\theta_{\lambda/2} = 0^\circ$  which evolves smoothly with ellipticity to a more significant dominance at  $\theta_{\lambda/2} = 30^\circ$ . This trend is not obvious from Fig. 4, nor, was it observed in previous 2D images.

The double-peaked structure of the spectrum is due to the Autler-Townes (AT) effect, and has been studied in detail in previous work [20,46,47]. The dependence of this structure on polarization has not been systematically explored before; however, since the splitting depends on the time-dependent Rabi frequency, given by the dipole operator times the (complex) laser electric field, one might expect it

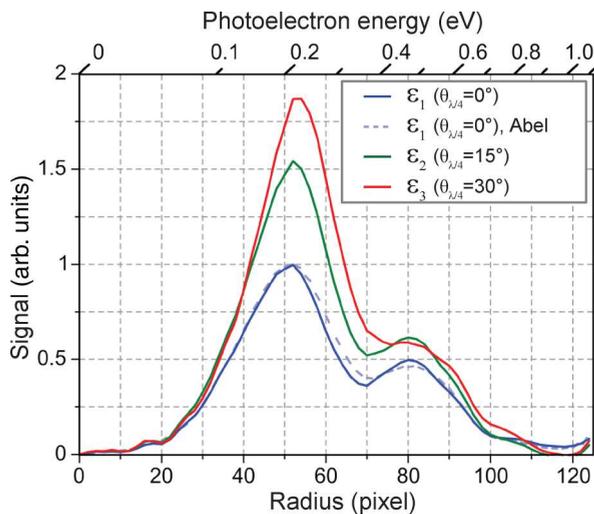


FIG. 5. (Color online) Radial spectra obtained from the 3D data shown in Fig. 4. For the linear case ( $\varepsilon_1$ ) the spectrum obtained via the Abel-transform-based PBASEX algorithm is also shown. The spectra are plotted in the native velocity space, and the upper abscissa indicates the (nonlinear) calibration to the photoelectron kinetic energy.

to respond to pulse polarization due to the dependence of the AT features on the details and ratios of the various ionization pathways, which are sensitive to the pulse polarization (see Ref. [21]). As discussed further below, there is some evidence for interferences between ionization paths of different photon-order in the PADs, and this may also contribute to the differences observed in the radial distributions.

As a further cross-check of the tomographic procedure the radial spectrum obtained for the cylindrically symmetric  $\varepsilon_1$  case can be compared to the spectrum determined using standard Abel-based methods. Here an adapted version of the PBASEX algorithm [28,31] was used, which makes use of a forward Abel transform of a set of polar basis functions combined with a fitting routine in order to determine the original,  $\phi$ -invariant, photoelectron distribution  $I(\theta, k)$  from a single image (with  $\Theta_D = 0^\circ$ ). It is clear that the results of the methods are in good agreement.

### C. Angular distributions and anisotropy parameters

Photoelectron angular distributions (PADs)  $I(\theta, \phi, k)$  were extracted from the 3D data as defined in Sec. II C. Figure 6 shows some examples of the raw data and the fitted interferograms, plotted in spherical polar space as a function of energy. A radial step size of  $\Delta r = 2$  was used in this procedure, and the fitting can be considered as both a means to determine the  $\beta_{L,M}(k)$  parameters and a data-smoothing procedure. From these two examples it is apparent that the spherical harmonic expansion describes the experimental data very well. Furthermore, it is immediately clear that the PADs have quite complex angular and energy structure, where only the former aspect was expected from the previously obtained 2D images (Ref. [21]) and visual inspection of the 3D data (Sec. III A). Figure 6(a) corresponds to the main spectral

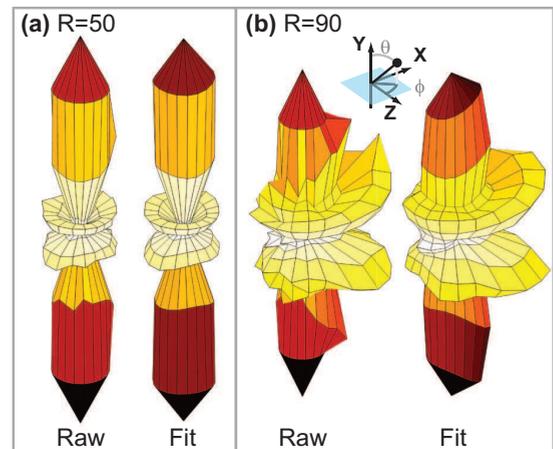


FIG. 6. (Color online) Raw and fitted photoelectron angular interferograms  $I(\theta, \phi, k)$  for selected  $k$  following ionization with linearly polarized light ( $\varepsilon_1$ ). (a) PAD at the peak of the spectrum ( $R = 50$ ), displaying cylindrical symmetry; (b) PAD at the high-energy wing ( $R = 90$ ), displaying symmetry breaking in the plane of polarization. In both panels the raw data are on the left and the fit on the right, with the fit results displayed at the same angular binning as used for the raw data. Further examples of fitted PADs are shown in Fig. 7, and the complete set of extracted  $\beta_{L,M}(k)$  in Fig. 8.

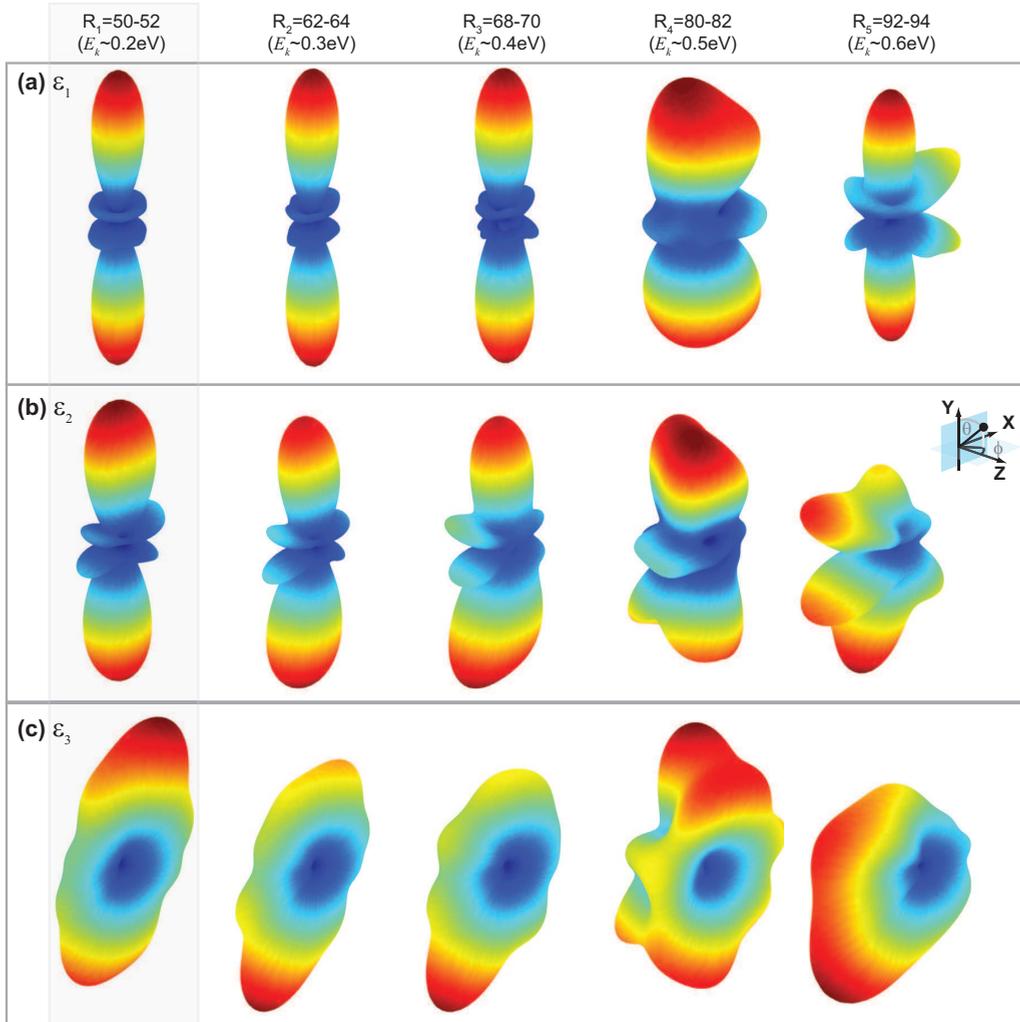


FIG. 7. (Color online) Photoelectron angular interferograms. PADs are shown for a range of photoelectron energies for (a) linearly polarized light  $\varepsilon_1$ ; (b),(c) elliptically polarized light  $\varepsilon_2$  and  $\varepsilon_3$ , respectively. Radial windows are labeled, and correspond to the regions 1–5, in Fig. 8, and approximate photoelectron kinetic energies  $E_k$  are also given. In all cases the PADs are generated from the  $\beta_{L,M}(k)$  obtained from the experimental data, i.e., they correspond to the fit results of Fig. 6 but at higher resolution. This is shown explicitly for (a), where the first and last distributions correspond to the distributions of Fig. 6. The corresponding  $\beta_{L,M}(k)$  are shown in Fig. 8.

peak. Here the structure matches that observed directly in the volumetric plots of Fig. 4 and indicates the expected cylindrical symmetry. However, Fig. 6(b), which corresponds to the high-velocity wing of the spectrum, shows that the form of the PADs changes and, most interestingly, symmetry breaking is observed, with asymmetries appearing in the plane of polarization.

A more detailed view of this behavior is presented in Figs. 7 and 8. The former shows PADs for all polarization states and a range of  $k$ , while the latter shows the  $\beta_{L,M}(k)$  which provided the full information content of the data. Although not as evocative as the spherical polar representations shown in Fig. 7, this reduced-dimensionality representation allows for a more detailed overall view of the energy-resolved interferograms. To reduce the complexity of the presentation slightly, the plots here show only the major parameters, defined in this case by  $|\beta_{L,M}(k)| > 0.2$  for any polarization state  $\varepsilon_n$ . To maintain consistency the same set of parameters is shown for all polarization states, and the color mapping is similarly

maintained for all data sets. Note that the polar coordinate space used is defined such that the polar axis is parallel to the  $Y$  axis (the same convention as in Figs. 3, 6, and 7). This allows for the linear case to take its simplest form, with  $M = 0$  terms only, and matches the frame definition used for the calculations of Refs. [21,29].

In both Figs. 7 and 8 the evolution of the interferograms with  $k$  is clear: over the main spectral feature ( $30 \lesssim R \lesssim 70$ ) the  $\beta_{L,M}(k)$  are almost invariant, but away from this feature there are significant—but smooth—changes. In particular, the wings of the peaks ( $R \lesssim 30$ ,  $R \gtrsim 95$ ) show significant evolution of the  $\beta_{L,M}(k)$ , as does the region of overlap of the major and minor spectral features ( $75 \lesssim R \lesssim 85$ ). In general, the results show fairly smooth evolution of the  $\beta_{L,M}(k)$  with energy, with faster evolution as a function of energy in the regions of peak overlap. The symmetry breaking noted above corresponds to the highest-energy regions; in  $\beta_{L,M}(k)$  terms these are regions where significant odd- $L$  and odd- $M$  values are present. This symmetry breaking is particularly clear for cases  $\varepsilon_1$  and  $\varepsilon_2$ ,

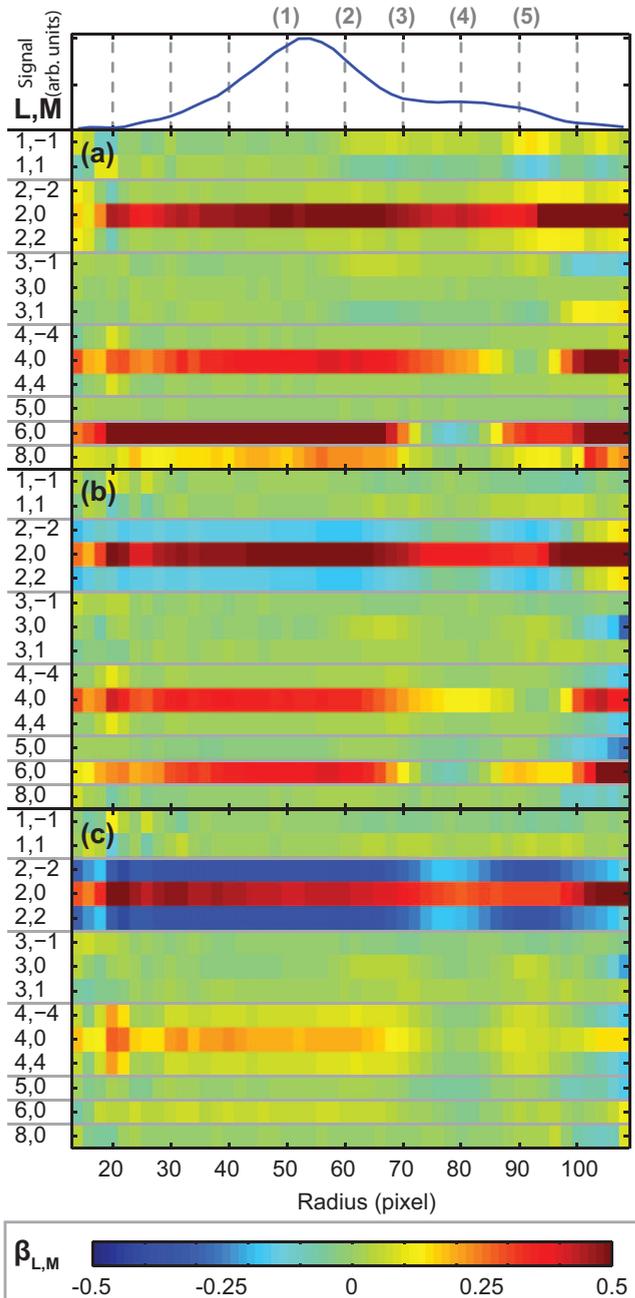


FIG. 8. (Color online) Full  $\beta_{L,M}(k)$  parameters for (a) linearly polarized light  $\varepsilon_1$ ; (b),(c) elliptically polarized light  $\varepsilon_2$  and  $\varepsilon_3$ , respectively. For reference, the velocity spectrum for the linear case is shown in the top panel, and the radial slices labeled correspond to the PADs plotted in Fig. 7. All  $L, M$  values for which  $|\beta_{L,M}(k)| > 0.2$  for any data set (i.e., all  $\varepsilon_n$ ) are plotted. To best visualize and compare the large parameter space, the color bar is fixed over all plots from  $-0.5$  to  $+0.5$ , although this does result in a few regions over the main feature where the values are out of range.

which both have lobes along the  $X$  axis in the positive or negative directions only, corresponding to significant  $L = 1$  and  $L = 3$  contributions in the  $\beta_{L,M}(k)$  spectra. Additionally, Fig. 8(a) also shows that significant  $L = 8$  terms are present. The interpretation of these observations is discussed in Sec. IV.

Overall, the results clearly show the benefits of a maximum-information metrology approach. In particular, the clear symmetry breaking within the plane of polarization is a signature of the presence of additional interfering channels in the photoionization interferometer. These signatures are not observable in the current or previous 2D images, nor allowed by the theoretical treatment, and indicate additional complexities in the light-matter interaction beyond the net three-photon ionization framework previously established (Sec. II and Refs. [21,29]), details which were otherwise lost.

#### D. Comparison with theoretical results

In Ref. [21], a comparison of 3D distributions based on ionization matrix elements determined from 2D experimental data were compared qualitatively to tomographically reconstructed experimental distributions. While qualitatively in good agreement, a more quantitative comparison at the level of the  $\beta_{L,M}(k)$  can now be made. This comparison is shown in Fig. 9. In the theory, the energy dependence of the  $\beta_{L,M}(k)$  is neglected; hence they are assumed to be constant over the observed radial spectrum. From the analysis above, it is clear that this assumption is valid over the FWHM of the main feature in the spectrum, but does not hold in other regions. Figure 9 therefore compares the theoretical results with the experimental  $\beta_{L,M}(k)$  averaged over the FWHM of the main spectral feature. In the theoretical results, the polarization state of the light is parametrized by  $\phi_y$ , the spectral phase of the  $y$

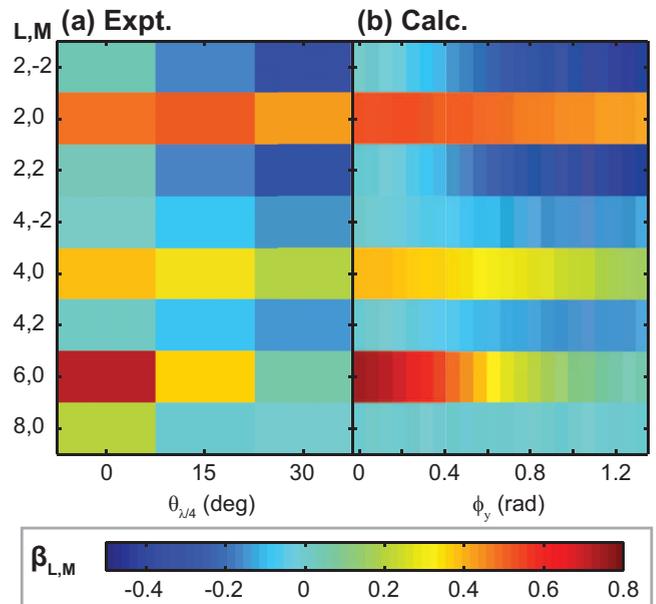


FIG. 9. (Color online) Comparison with theoretical results. (a) Experimentally determined  $\beta_{L,M}$ , averaged over the main spectral feature, for each polarization state as defined by  $\theta_{\lambda/4}$ . (b) Theoretical results (see Ref. [29] for details), plotted as a function of polarization state as defined by  $\phi_y$ , the phase shift of the  $y$ -polarized component of the electric field. In the former case,  $0 \leq \theta_{\lambda/4} \leq 45^\circ$  spans all polarization states from linear to circular, and in the latter  $0 \leq \phi_y \leq \frac{\pi}{2}$  (the full angular interferogram for  $\phi_y = 0.5$  is shown in Fig. 1). The scales on the plots are set to approximately match the experimental polarization space.

component of the electric field, where  $0 \leq \phi_y \leq \frac{\pi}{2}$  spans all polarization states from linear ( $\phi_y = 0$ ) to circular ( $\phi_y = \pi/2$ ). The experimental results for polarization states  $\varepsilon_1$ ,  $\varepsilon_2$ , and  $\varepsilon_3$  correspond to  $\phi_y = 0$ ,  $\sim 0.5$ , and  $\sim 1.2$  rad, respectively. (For further details of the theory and a complementary presentation of the theoretical and tomographic results, see Ref. [29].)

It is clear, as expected from the previous qualitative comparison, that the agreement is good—but not exact. More specifically, the results show that the tomographic data, as a function of  $\theta_{\lambda/4}$ , are close to the theoretical results, plotted as a function of  $\phi_y$ , over the main spectral peak, and both smoothly evolve with the pulse polarization. In a general sense this indicates that the theory results, based solely on 2D data, are validated by this comparison with more detailed 3D data. It also suggests, however, that some refinement could be made of the previously obtained ionization matrix elements based on this more detailed data, in particular via the inclusion of the radial dependence of the  $\beta_{L,M}(k)$  in the fitting methodology. This is a clear potential offered by the 3D data and is discussed further in Sec. IV.

There are also additional experimental issues which may play a role here. In this case, the exact  $\beta_{L,M}(k)$  expansion depends fairly sensitively on the frame-of-reference definition applied, which includes both the definition of the image center and the choice of the  $\phi = 0$  plane. Appropriate frame rotations were applied during data analysis, but small inaccuracies may still be present. Any processing inaccuracies or artefacts of this type would appear as systematic errors in the extracted  $\beta_{L,M}(k)$ , but would not show a clear or smooth energy dependence, so would not affect the results or conclusions presented herein more generally. There is also the assumption that the polarization state of the light is identical over the pulse bandwidth, which may also not be rigorously true. In this case, an apparent energy dependence would be observed in the  $\beta_{L,M}(k)$ , but would be caused by this polarization state drift rather than any inherent energy dependence of the photoionization dynamics. Again, any effects here are likely to be small, but may be noticeable at this quantitative level of comparison. As observed in the previous section, there are also additional terms which appear in the experimental data, but are not allowed by the current theoretical treatment. Over the main spectral feature there is no symmetry breaking, but significant  $L = 8$  terms are present and, as shown in Fig. 9(b), do not appear in the theoretical results. The possible origin of these features is discussed in the following section.

#### IV. DISCUSSION

In the preceding section the benefits of a full 3D photoelectron measurement were discussed in terms of the quantitative analysis of the observed angular interferograms, facilitated by the  $\beta_{L,M}(k)$  parameters. While this treatment is experimentally rigorous, and represents the full information content of the observable, the complexity of the coupling of the continuum wave function into the observable necessitates further phenomenological discussion and theoretical analysis in order to understand the physical significance of these observations and draw firmer conclusions about the light-matter interaction.

First, it is important to reiterate that the good agreement of the current results with the previous model over the

main spectral feature suggests that the dominant channels are identical to the 2D data analyzed in that case (at a lower peak intensity of  $\sim 10^{12}$  W cm<sup>-2</sup>) and, therefore, the observation of additional interferences in the 3D data are a direct benefit of the maximum-information measurement. It is this enhanced metrology which allows for minor contributions to the interferogram to be cleanly resolved. The ability to directly and quantitatively compare the theoretical results from the previous analysis with experimentally obtained interferograms also provides a rigorous benchmark against which to validate the previous analysis, including the accuracy of the ionization matrix elements determined and the limitations of the theory developed.

#### A. Phenomenological analysis

In order to understand the additional insights gained from the maximum-information measurements, one can approach from a purely experimental perspective. In this case, there are two key observations to consider: the general evolution of the angular interferograms over the energy spectrum or, equivalently, over the Autler-Townes structure of the spectrum [48] and the strong symmetry breaking observed in certain energy regions. These observations are already enough to provide a phenomenological understanding of the interferences observed. The AT structure is a direct result of the ac Stark effect, which causes a dynamic shifting of the energy levels of the ionizing system and continuum as a function of the laser field. In the frequency domain, this effect results in an effective level splitting defined by the time average of the laser field, defining a quasistatic “dressed-state” level structure. In this picture the photoelectron wave packet will gain an additional (energy-dependent) phase due to the level splitting, and interferences from different components of the AT structure will occur in regions where photoelectron wave packets correlated with different quasistatic levels overlap energetically. Analogous behavior can be seen in energy-domain cases where different ionizing transitions are made to interfere via, for example, multicolor ionization schemes [50], which similarly allow the creation of new interferences in the continuum. A similar effect has also been considered in energy-domain work probing intensity effects, for instance in Refs. [51] and [52], which investigated the high-intensity nanosecond pulse regime where ac-Stark-shifted levels may be tuned in and out of resonance with the excitation pulse, yielding a strong intensity dependence in the angular interferograms according to the number and nature of the states which were coupled by the multiphoton ionization scheme at a given intensity. Due to the the additional laser bandwidth present in the femto- or attosecond regime, and consequent broad photoelectron bands, this type of effect might be expected to be very general, and has indeed recently been explored in theory for attosecond ionization in strong fields [53].

A more appropriate framework in this case is that of a time-domain interferometer. Here, there is an additional time-dependent phase, and additional interferences will appear in the measurement—which is integrated over the pulse duration—providing that the instantaneous contributions to the continuum wave function remain coherent. Examples of this type of effect include the time-domain interferometer discussed in Ref. [4], and the “atomic phase matching” in the two-pulse control scheme of Ref. [54]. In this picture,

the additional interferences observed are analogous to those which appear with polarization-shaped pulses, in which the coherent temporal interferences are correlated with the instantaneous polarization state of the pulse, allowing for “polarization multiplexing” in the time-integrated measurement (see Refs. [21,29]). Here, the additional interferences are associated with the instantaneous pulse intensity, but are otherwise analogous. These types of interferences can be generally termed *dynamic*, since they depend on the details of the laser pulse and the driven dynamics of the ionizing system. This phenomenology readily explains a strong dependence of the photoelectron interferograms on the AT structure, and is in fact implicit in the band structure of the photoelectron energy spectrum which results from these same dynamical interferences [47,55], and have also recently been explored in the context of intense XUV pulses [56]. However, this phenomenology does not obviously account for the observed symmetry breaking which requires  $m$ -state-dependent phase contributions. This latter effect may, however, be a result of the polarization dependence of the temporal phase, in terms of either the bound or continuum states. For instance, the populations of the  $4p_{+1}$  and  $4p_{-1}$  bound states accessed by the left- and right-circularly-polarized components of the field will correlate with the instantaneous electric field polarization, and hence ionize at different parts of the field cycle and accumulate different temporal phases [57]. In the dressed-state (energy-domain) picture this would be manifested as exactly the required symmetry breaking of the positive and negative  $m$  states, with a time-dependent superposition of the dressed states created—effectively a manifestation of the electronic ring currents discussed in the current context in Ref. [20], in terms of high-harmonic generation in Ref. [58], and more recently in the attosecond XUV regime in Refs. [53,59]. This phase would be directly mapped into the ionization continuum, again analogously to the polarization-multiplexed case previously explored. Similar considerations may also apply to the continuum states, in the case where the ionization cannot be considered in the perturbative regime.

### B. Theoretical analysis

To further investigate the specifics of the light-matter interaction and the additional minor contributions to the photoelectron interferograms, a more quantitative analysis of the observations can be made by considering the results within our existing theoretical framework. This treatment assumes a single active electron, dipole coupling, and perturbative ionization (see Refs. [21,29] for further details). In this scheme strict limits are placed on the allowed angular momenta and symmetries of the final continuum states. Any breaking of these limits therefore indicates additional physical complexities not included in the modeling of the light-matter coupling, for instance the dynamical phase discussed above, other nonperturbative effects, multielectron effects, and so forth. For the three-photon absorption process outlined in Sec. II, i.e.,  $4s + h\nu \rightarrow 4p_{\pm 1} + 2h\nu \rightarrow |k, l, m\rangle$ , treated within this scheme, the final states are restricted to  $l = 1, 3$ , and odd- $m$  terms only. This, in turn, places limits on observable interferograms: only  $\beta_{L,M}(k)$  with even  $L$  and even  $M$  are allowed, and are further restricted to  $L \leq 6$ . Therefore, the appearance

of additional  $L, M$  terms in the experimental data indicates the presence of additional partial waves in the continuum wave function. The dynamic interferences described above do not involve angular momentum exchange, so cannot be responsible for the appearance of new  $L$  terms, although they may be implicated in symmetry breaking if  $\pm m$  states are split and accumulate different phases as suggested above.

The appearance of additional angular momentum rather indicates additional interactions—(a) additional photon absorption and/or (b) photoelectron (re)scattering. The former could lead to angular momentum ladder climbing if additional  $|n, l, m\rangle$  bound or dressed states were accessible at the one- or two-photon level (e.g., high-lying Rydberg states), although it is not clear which specific states could be coupled in this way, and result in ensemble polarization; a similar effect could result from multiple, cascaded Raman transitions (ultimately equivalent to a field-mediated picture), in which atomic orbitals align with the strong laser field, thus creating ensemble alignment. In the case of elliptically polarized light, such effects could drive electronic wave packets with ring-current-like behavior, as suggested above, and this effect could indeed be responsible for the observed symmetry breaking, depending on the time-averaged ionization of the ring-current density. The latter effect essentially describes any other core-photoelectron interactions, such as angular momentum exchange during ionization, or field-mediated effects at longer range. In this case the single-active-electron picture (essentially a hydrogenic light-matter interaction) breaks down, and additional electron-electron scattering occurs. Such processes can be treated with more complex angular momentum coupling schemes, and experimentally would be indicated by the creation of electronically excited ions.

A final, but less likely, possibility is the breakdown of the dipole approximation. This would also result in the creation of high-order continuum states, but due to direct multipolar light-matter couplings. Since the dipole approximation relies on the wavelength of the electric field being large compared to the target, it is expected to hold at 800 nm and low photoelectron energies, although it has previously been observed that relatively low-energy processes may still require multipole couplings [60,61]. However, such effects break the interferogram symmetry along the photon propagation axis, so would not explain the main observations here. Finally, it should be noted that additional macroscopic effects may also play a role here, including intensity averaging over the laser pulse and the static electric fields present in the VMI chamber (which are known to influence states near threshold as mentioned in Sec. III A); any irregularities in the laser pulse could also affect the minor channels observed, such as nonuniform spectral phase and polarization state, although such effects are expected to be negligible in this case.

### V. CONCLUSIONS

From the considerations above it appears that both dynamical interferences, resulting from the mapping of the AT effect onto the photoelectron spectral phase and resulting in a strong energy dependence to the interferograms, and angular momentum couplings, resulting in the  $L > 6$  terms observed in the interferograms, must be invoked to explain the observed

photoelectron interferograms. Although a more sophisticated theoretical treatment, and possibly additional experiments to consider the intensity dependence, is needed in order to assess the exact nature of these possibilities and the precise details of the symmetry-breaking interactions, from the experimental perspective the ability to *resolve* these effects is a uniquely powerful result of maximum-information methods.

This type of 3D photoelectron data, reflecting the complex set of interfering ionization channels through the observable dissected in terms of energy-dependent angular interferograms and associated anisotropy parameters, reveals a wealth of detailed information on the fundamental physics of the light-

matter interaction (including the scattering of the outgoing electron) and requires no *a priori* assumptions regarding the symmetry of the light-matter interaction. This high level of detail necessitates careful analysis but, ultimately, provides the most complete picture of such interactions possible, whether the goal is quantum metrology or quantum control.

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