

NRC Publications Archive Archives des publications du CNRC

Qualitative Model Abstraction for Diagnosis

Yan, Y.

This publication could be one of several versions: author's original, accepted manuscript or the publisher's version. /
La version de cette publication peut être l'une des suivantes : la version prépublication de l'auteur, la version acceptée du manuscrit ou la version de l'éditeur.

Publisher's version / Version de l'éditeur:

The 17th International Workshop on Qualitative Reasoning [Proceedings], 2003

NRC Publications Archive Record / Notice des Archives des publications du CNRC :

<https://nrc-publications.canada.ca/eng/view/object/?id=98db93a9-0ad7-4a70-a49d-e2dbe13ef77c>

<https://publications-cnrc.canada.ca/fra/voir/objet/?id=98db93a9-0ad7-4a70-a49d-e2dbe13ef77c>

Access and use of this website and the material on it are subject to the Terms and Conditions set forth at

<https://nrc-publications.canada.ca/eng/copyright>

READ THESE TERMS AND CONDITIONS CAREFULLY BEFORE USING THIS WEBSITE.

L'accès à ce site Web et l'utilisation de son contenu sont assujettis aux conditions présentées dans le site

<https://publications-cnrc.canada.ca/fra/droits>

LISEZ CES CONDITIONS ATTENTIVEMENT AVANT D'UTILISER CE SITE WEB.

Questions? Contact the NRC Publications Archive team at

PublicationsArchive-ArchivesPublications@nrc-cnrc.gc.ca. If you wish to email the authors directly, please see the first page of the publication for their contact information.

Vous avez des questions? Nous pouvons vous aider. Pour communiquer directement avec un auteur, consultez la première page de la revue dans laquelle son article a été publié afin de trouver ses coordonnées. Si vous n'arrivez pas à les repérer, communiquez avec nous à PublicationsArchive-ArchivesPublications@nrc-cnrc.gc.ca.



National Research
Council Canada

Conseil national
de recherches Canada

Institute for
Information Technology

Institut de technologie
de l'information

NRC - CNRC

Qualitative Model Abstraction for Diagnosis *

Yan, Y.
August 2003

* published in The 17th International Workshop on Qualitative Reasoning. Brasilia, Brazil.
August 20-22, 2003. pp. 171-179. NRC 46498.

Copyright 2003 by
National Research Council of Canada

Permission is granted to quote short excerpts and to reproduce figures and tables from this report,
provided that the source of such material is fully acknowledged.

Qualitative Model Abstraction for Diagnosis

Yuhong Yan

NRC Institute of Information Technology, Canada
Yuhong.yan@nrc.gc.ca

Abstract

Building qualitative models is a crucial task for model-based diagnosis. This paper discusses the techniques to automatically transform a quantitative model in CAD environment into a qualitative model, under the cases that the real numbered landmarks are known and unknown. With known landmarks, the abstraction is through the discretization process where the simulation data is discretized according to the given landmarks. If landmarks are unknown, the landmark generation process, which is inspired by the discriminability analysis for multiple behaviour modes, is applicable. For dynamic systems, the pseudo-variables are introduced to describe the dynamic behaviour. The techniques developed are demonstrated by a simplified automotive subsystem.

Introduction

The automobile industry has foreseen the growing demand of diagnostic analysis for automobiles. Engineers need an integrated design environment that enables them to do the diagnostic analysis at the design stage, so that they can understand and evaluate the effects of each choice on the diagnostic properties of the system being designed. European FP5 Project IDD (Integrated Design Process for On-board Diagnosis) aims to formalize and standardize the diagnostic design process and to develop new techniques and tools to support this purpose. After a model-based diagnosis approach is determined, the problem of creating the appropriate qualitative model becomes the crucial issue.

Our starting point is the numeric simulation model which is built to examine a system's behaviour by design engineers in a CAD environment. Matlab/Simulink is the target CAD platform due to its wide adoption in the automotive industry. Models in Matlab/Simulink are illustrated graphically as a set of subsystems/blocks and a number of interconnected input and output links between the blocks. Empirical data, library functions, as well as formulas can be used in the blocks. Normally no explicit equations are available for the general system under study. Our task is to develop automatic approaches to abstract the qualitative model for diagnostic purposes.

The qualitative model used in this paper is in finite domain tuples, i.e. the domain of a variable has multiple landmarks. This paper presents the techniques of model abstraction with or without landmarks for both static and dynamic systems. Section 2 reviews the relevant techniques

for model abstraction and diagnosis. Section 3 discusses the approaches for model abstraction with known landmarks for both static and dynamic system. Section 4 represents the approach for the landmark determination based on diagnosability analysis. Section 5 demonstrates how the approaches developed can be used in a model of a subsystem in automotive. Section 6 is discussion and conclusion.

State of the Art in Qualitative Model Abstraction and Diagnosis

State-based vs. Simulation-based Diagnosis

Diagnosing dynamic system requires checking the consistency of observations over time with the behaviours modeled by the dynamic model of the device. A straightforward solution is to simulate incrementally the model as observations change, in order to predict the immediate successor states. This is the simulation-based approach used in (Dvorak and Kuipers 1992). (Dressler 1996) avoids simulation and generates diagnostic candidates based on checking consistency of the model with observed states only. (Malik and Struss 1996) states a necessary and sufficient condition for the equivalence of state-based and simulation-based diagnosis without giving a proof. (Struss 1997) further presents that if the system dynamic can be modeled as state constraints plus CID constraints, which are general rules about continuity, integration and derivatives, then diagnosis based on checking the state consistency yields results equivalent to diagnosis based on simulation. Of course, the state-based approach is much less costly than the simulation-based approach. If a system has other temporal constraints than the CID constraints (called trans-constraints), the conclusion is no longer held. These trans-constraints are typically constraints introducing discontinuities over time. (Panati and Dupre 2000) and (Dupre and Panati 1998) report a violating case where abrupt faults are considered. Abrupt faults, where a system parameter changes abruptly, are the cases of discontinuity. By adding constraints related to injecting a fault, the simulation may actually be useful to restrict the set of possible diagnoses. There are many methods on how to model the constraints related to injecting a fault (Dupre and Panati 1998), (Mosterman and

Biswas, 1997). Abrupt faults are not considered in this paper.

The state-based diagnosis engine is used in our project, though the state-based way could result in more candidates as stated above. This paper concerns building a qualitative model efficiently and automatically from the simulation environment for the state-based diagnosis engine. Diagnosis equivalence in (Struss, 1997) has a precondition that there are sufficient observables. More specifically, since the state-based approach does not use the relation between x and dx/dt , both x and dx/dt should be observables in order to have enough redundancy for diagnostic analysis. Sometimes not both of x and dx/dt are modeled in the simulation model or not both can be measured as physical variables. In section 3.3, pseudo variables are introduced to describe the dynamic behaviour and also provide redundancy for diagnostic analysis for dynamic system.

Abstraction of Qualitative model

Qualitative models have already been successfully used in the framework of model-based diagnosis. When abstracting a qualitative model for a system, the crucial requirement is to transform the model to the right level of abstraction after composing it. In (Struss 2002), the problem is stated as to find the necessary and sufficient distinctions in the domains of the system variable to achieve a particular *goal* in a certain *context* and under given *conditions*. The right level of abstraction is task-dependent; depending on the requirements of the tasks, the distinctions can be different. (Sachenbacher and Struss 2001) introduces AQUA, a framework for automated qualitative abstraction. In AQUA, the *goal* of using a model is characterized by a set of *target partitions* of the domains of selected variables (e.g. output variables), the context is given by the structure of the model system, and the *conditions* are represented by a set of initial variables and their possible distinctions (e.g. possible observations). AQUA needs a fine-grained qualitative relation as the starting point. The partitions of domain can be given by (finite) sets of landmarks that define qualitative values as intervals between adjacent landmarks. AQUA then eliminates landmarks that do not contribute to a distinction between target partitions. The abstract model will then contain a subset of the landmarks of the original model but maintain the predictive power with respect to qualitative values of the target variables. One difficulty of this method is that the starting “fine” domain model is difficult to obtain. We do not know how fine the starting model should be, so that the abstract process can remove some landmarks to get the optimized qualitative model. Second there are no criteria to determine the target distinctions. (Struss 2002) extends AQUA by giving an approach to automatically determine the landmarks for the variables. It is a recursive subdivision process. The criterion to divide the domain is that if a qualitative value of some variable occurs in many tuples, it is identified as a candidate for refinement and split into two or more intervals by introducing additional

landmarks. This criterion does not show how the new partitions effect on the target distincts, thus its effectiveness is questionable.

Qualitative simulation is a widely used tool. The fundamental difference is QSIM starts from QDE (Qualitative Differential Equation) and the simulation is on qualitative level, while the starting point in this paper is the numerical simulation model, and the simulation is numerically. Many QSIM techniques, such as value generation, constraint filtering, can't be used here. A summary of QSIM techniques and their extensions can be found in (Kuipers 2001).

In FDI community, there is also some work on building qualitative system models. One example is (Lunze et al. 1999), in which the state variables are partitioned along the time based the state transforms. The result is the discrete trajectory of states. In this paper, pseudo-variables, which are the derivatives of flow or effort variables (cf. section 3.3), are introduced to describe system dynamic. The pseudo-variables are equivalents to the state variables. While Lunze uses the state transform equations to determine the state variables in the next time step, our approach does not have transform equations. The discretization is on the values of input and output data after the time information is removed. Thus the two approaches are different from each other and both are suitable for their diagnosis principles.

There are some other commonly used ways to obtain qualitative model, e.g. the qualitative derivation model (Malik and Struss 1996), and Bond-graph analysis (Mosterman and Biswas 1997). They either have no automatic methods available or not start with simulation model. So they are not reviewed here. The techniques listed here are far from complete. A review on qualitative model construction can be found in (Schit and Bredeweg 1996).

Features of a Simulation Model and Its Gap to Qualitative Model

There is a big gap between the simulation model which is a description of the system behaviours and the qualitative model which is used for diagnosis. The qualitative model for diagnosis needs two kinds of information: 1) the structural model which is the physical structure of a system, i.e. how the physical components are connected; 2) the behaviour model which is a description of the input-output relation for every physical component. In a graphical CAD environment, like Matlab/Simulink, the physical components are represented by blocks. A block can have sub-blocks for describing internal structure or functions inside the components. The links between the blocks are the physical connections, where the connected blocks have shared variables. The structural model is obtained by extracting the connections and block information from the CAD environment. This can be done by calling CAD functions to collect this kind of information. The difficulty is in abstracting the behaviour model. The relations of a

component are implied by the blocks. The standard blocks are normally mathematical operators and can be expressed as formulas between inputs and outputs. Many other so called “customized” blocks contain C-code, look-up tables and Matlab scripts, which have no explicit equations. These blocks can be cascaded or sub-composed together for one physical component. This gives the design engineers the maximum flexibility for building models. They can either encode their empirical data into the look-up tables, or embed logic clauses in the script code, or call professional libraries from C-code. But on the other side, this causes a great gap between a simulation model and a model-based diagnosis engine that requires explicit relational expression. Moreover, simulation is executed only in one direction, i.e. we are unable to compute the inputs from the outputs. Though the gap exists, one benefit of the CAD environment is its effective computation capacity to simulate the system behaviour in both static and dynamic processes. We can depend on this when we design our solution.

Abstracting Qualitative Models from Simulation Models using Finite Domains

Finite Relation Qualitative Model

A Finite Relation Qualitative Model uses a set of real numbers as landmarks for each variable. The qualitative values are the intervals between adjacent landmarks. The qualitative relation is the mapping between the qualitative values. More landmarks produce a finer qualitative model.

Definition1: An **interval** is a pair of numeric landmarks: $I_j := [lm_a, lm_b]$, where $lm_a \leq lm_b$.

Definition2: Two intervals are equal if and only if the two landmarks are equal:

For intervals $I_1 := [lm_a, lm_b]$, and $I_2 := [lm_c, lm_d]$, I_1 equals I_2 iff $lm_a = lm_b$ and $lm_c = lm_d$.

Definition3: A **tuple** is a collection of ordered intervals:

$$T := \{I_1, \dots, I_n\} = \{[lm_a, lm_b], \dots, [lm_p, lm_q]\}$$

If vectors $LM_1 := [lm_a, \dots, lm_p]$ and $LM_2 := [lm_b, \dots, lm_q]$, the tuple T can be represented by $T := [LM_1, LM_2]$. An n -dimension tuple can represent an n -dimension rectangle.

Definition4: A **qualitative model** q is a mapping between two sets of intervals:

$q: \Psi_1 \rightarrow \Psi_2$. The source set $\Psi_1 = \{[lm_i^{in}, lm_{i+1}^{in}]\}$ is the set of qualitative inputs to the model, the target set $\Psi_2 = \{[lm_k^{out}, lm_{k+1}^{out}]\}$ is the set of qualitative outputs from the model.

The mapping is a multiple valued relation, i.e.

$\forall [lm_i^{in}, lm_{i+1}^{in}] \in \Psi_1, q: [lm_i^{in}, lm_{i+1}^{in}] \rightarrow \Psi_2' \subset \Psi_2, \Psi_2'$ is empty or has one or more elements. If we can enumerate the mapping pairs, q can be presented in set of tuples, as:

$$\{ \{ [lm_i^{in}, lm_{i+1}^{in}], [lm_j^{out}, lm_{j+1}^{out}] \}, \dots, \{ [lm_p^{in}, lm_{p+1}^{in}], [lm_q^{out}, lm_{q+1}^{out}] \} \} \quad (1)$$

When the input is multi-dimensional, a qualitative model q is a mapping between two sets of tuples: $q: \Psi_1 \rightarrow \Psi_2$. The source set $\Psi_1 = \{T_i\}$ is the set of input tuples and the target set $\Psi_2 = \{S_j\}$ is the set of output tuples of the model. If we

can enumerate the mapping pair of tuples, q can be represented by

$$\{ \{T_1, S_1\}, \{T_2, S_2\}, \dots, \{T_n, S_m\} \} \quad (2)$$

Definition5: If a system described by $y=f(x)$ is a static quantitative model, landmarks x_1, x_2, \dots, x_n and y_1, y_2, \dots, y_m are selected for x and y and in an ordered sequence. A **qualitative abstraction** $q(f)$ is a mapping from set $\Psi_1 = \{[x_1, x_2], [x_2, x_3], \dots, [x_{n-1}, x_n]\}$ to set $\Psi_2 = \{[y_1, y_2], [y_2, y_3], \dots, [y_{n-1}, y_n]\}$:

$q(f): \{[x_1, x_2], [x_2, x_3], \dots, [x_{n-1}, x_n]\} \rightarrow \{[y_1, y_2], [y_2, y_3], \dots, [y_{n-1}, y_n]\}$, such that: $\forall [x_i, x_{i+1}], q(f): [x_i, x_{i+1}] \rightarrow [y_j, y_{j+1}]$, iff $\exists x, x_i \leq x \leq x_{i+1}, y_j \leq y \leq y_{j+1}$.

Qualitative abstraction $q(f)$ results a qualitative model. Landmarks x_1, x_2, \dots, x_n and y_1, y_2, \dots, y_m are selected to cover $y=f(x)$'s domain and range, i.e. $\cup_i [x_i, x_{i+1}] \supseteq \text{Domain}(x)$, and $\cup_j [y_j, y_{j+1}] \supseteq \text{Range}(y)$. Definition 5 can be extended for multiple in-out systems.

Definition6: $Y=f(X)$ is a static quantitative model, where $X = [x_1, x_2, \dots, x_n]$ and $Y = [y_1, y_2, \dots, y_m]$. $[x_{i,1}, x_{i,2}, \dots, x_{i,n}]$ are landmarks for x_i . $[y_{j,1}, y_{j,2}, \dots, y_{j,m}]$ are landmarks for y_j . A **qualitative abstraction** of model $Y=f(X)$ is a mapping from set $\Psi_1 = \{\prod_i [x_{i,p}, x_{i,p+1}]\}$ to set $\Psi_2 = \{\prod_j [y_{j,q}, y_{j,q+1}]\}$:

$q(f): \Psi_1 \rightarrow \Psi_2$, such that $\forall \prod_i [x_{i,p}, x_{i,p+1}], q(f): \prod_i [x_{i,p}, x_{i,p+1}] \rightarrow \prod_j [y_{j,q}, y_{j,q+1}]$, iff $\exists X, X \in \prod_i [x_{i,p}, x_{i,p+1}], Y \in \prod_j [y_{j,q}, y_{j,q+1}]$.

Model Abstraction for Static Simulation Model with Known Landmarks

Discretization Algorithm is designed to deal with the simplest case, in which the simulation model is static and the landmarks for the variables are known. The name come from that the algorithm discretizes the simulation data into intervals of landmarks.

Algorithm 1 is the discretization algorithm with the simulation model $Y = f(X)$, where f can be implicit, and the landmarks for X and Y as inputs. Suppose x_i has a set of landmarks $\{x_lm_1^i, x_lm_2^i, \dots, x_lm_m^i\}$, the adjacent landmarks makes a set of the intervals $\{[x_lm_1^i, x_lm_2^i], \dots, [x_lm_{m-1}^i, x_lm_m^i]\}$. The simulation inputs for x_i are from one of these intervals. Thus, the input points for X are generated from a multi-dimensional rectangle, which is one element in the set of the combination of the intervals:

$\prod_i \{[x_lm_1^i, x_lm_2^i], \dots, [x_lm_{m-1}^i, x_lm_m^i]\}$, as in Line 2.

Suppose $[x_lm_p^i, x_lm_{p+1}^i]$ is the interval for x_i , k random values are generated in this interval. For an n -dimensional rectangle, totally k^n testing points generated (Line 3). The purpose of generating the random values is to probe the extrema when function f is not monotonic. This is just an approximate approach to deal with non-monotonic (ref. discussion below). Line 4 calls Simulink simulation function to get the values of the outputs for each of the k^n testing points. Line5-6 gets the minimum and maximum output values. Line7-8 gets the landmarks that cover the range of output values. The qualitative relation is in line 9.

Algorithm 1: Discretization

Inputs:

- numeric model $Y = f(X)$ in Matlab/simulink format

- $\{x_{lm_1^i}, x_{lm_2^i}, \dots, x_{lm_m^i}\}$ is the set of landmarks for x_i ,
- $\{y_{lm_1^j}, y_{lm_2^j}, \dots, y_{lm_q^j}\}$ is the set of landmarks for y_j
- a nature number k

Outputs:

- a vector q storing the mapping pair (as format in (2))
- 1: create a vector q to store the mapping pair
 - 2: for each element in $\Pi_i\{[x_{lm_1^i}, x_{lm_2^i}], \dots, [x_{lm_{m-1}^i}, x_{lm_m^i}]\}$
 - 3: generate k random values for each $[x_{lm_p^i}, x_{lm_{p+1}^i}]$, lets say $\{xx_1^i, \dots, xx_k^i, x_{lm_{p+1}^i}\}$, the input points are $\Pi\{x_{lm_p^i}, xx_1^i, \dots, xx_k^i, x_{lm_{p+1}^i}\}$
 - 4: call Simulink function to simulate $f(\Pi_i\{x_{lm_p^i}, xx_1^i, \dots, xx_k^i, x_{lm_{p+1}^i}\})$
 - 5: $Y_{min} = \min(f(\Pi\{x_{lm_p^i}, xx_1^i, \dots, xx_k^i, x_{lm_{p+1}^i}\}))$
 - 6: $Y_{max} = \max(f(\Pi\{x_{lm_p^i}, xx_1^i, \dots, xx_k^i, x_{lm_{p+1}^i}\}))$
 - 7: $y_{low}^j = \max(\{y_{lm_u^j} \mid y_{lm_u^j} \leq y_{min}^j\})$
 - 8: $y_{high}^j = \min(\{y_{lm_v^j} \mid y_{lm_v^j} \geq y_{max}^j\})$
 - 9: store $\langle \Pi [x_{lm_m^i}, x_{lm_{m+1}^i}], [y_{low}^j, y_{high}^j] \rangle$ in q
 - 10: end for
 - 11: report q

Algorithm 1 is similar to the method in (Struss 2002). The similarities are both methods use real numbers as landmarks and discretize the continuous model with these landmarks. The differences are: first, (Struss 2002) considers the precision of the model, i.e. the base model is given by the envelope of $f(\mathbf{X})$. This is perhaps for considering noise in the signals or the computation error in simulation. We consider it is not necessary to add this envelope. If concerning the noise, it is better to eliminate the noise from the signals than adding the tolerance at the modeling stage. If concerning about the computation error, it is rather small that ignoring it won't affect the approximation of the qualitative model. Adding envelope could degrade the qualitative model because the distinctions between right and faulty behaviour might be removed. Secondly, (Struss 2002) limits the algorithm to monotonic functions or monotonic sections of a function. With the monotonic constraint, the tuples are determined by the bounding landmarks (e.g. the corners of the rectangle). If users do not know the shape of the function, users can choose wrong landmarks that the relation determined by the bounding landmarks can miss the extreme points, thus abstracted qualitative behaviour is not "sound". To get the monotone pieces from the discrete simulation data is not a trivial problem. The way to compute the derivative numerically from the discrete simulation data in order to determine the monotone as in (Struss, 2002) is not feasible because the very small but numerous turbulences on the data, which is the case for the simulate data, could lead to wrong results. Our method using random points to probe the extrema between the landmarks is a practical solution for the non-monotonic function. If the random points are in a large amount, practically this method can get satisfactory results for non-monotonic systems. But this problem is still open. (Brooks, 1984) gives a mathematical foundation for detecting monotonic pieces from discrete data (simulation

data). We believe this could be a solution, though we did not test this technique yet.

Model Abstraction for Dynamic Model

As discussed in Section 2.1, there are two views on how to diagnose dynamic systems. State-based diagnosis is used in our project. In state-based diagnosis, the relations between the time steps are not considered, i.e. dx/dt is not computed from x , or when dx/dt and x are both known, the relation between them is ignored. One straightforward way to model the dynamic for state-based diagnosis is to model the derivatives of the variables. But in many situations, the derivative of a variable is not a variable in the simulation model, or physically is not a measurable variable. For example, Figure 1 is the model for a RC circuit. Voltages, u_1 , u_2 , and u_3 , are the observable variables, while current i is non-observable. u_1 and u_3 are constant. The derivatives of the voltages or the currents, which are necessary for modeling the dynamic behaviour, are missing in the simulation model.

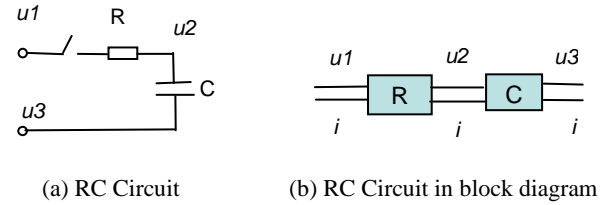


Fig. 1 Example: RC Circuit and Simulation Model

Our solution is to introduce the **pseudo variables**, which are the derivatives of *effort* or *flow* variables, in the qualitative model. A systematic framework exists for building consistent and well constrained models of dynamic physical systems from multiple domains (e.g. electrical, mechanical, hydraulic), which is based on the *continuity of power* and *conservation of energy* between system components (Karnopp and Rosenberg 1975) The *effort* variables are to represent generalized voltage, pressure, temperature, etc., and the *flow* variables are to represent generalized current, volume flow, entropy flow, etc. Depending on the dynamic is caused by capacity or inertia element, the derivatives of *effort* or *flow* variables are chosen as the pseudo variables. As shown in figure 2, (a) is the original model, in which E is the *effort* vector, and F is the *flow* vector. For the system has capacity dynamic, dE/dt is added as pseudo variables, or for inertia dynamic, dF/dt is added as pseudo variable. Fig 2(b) is a case with capacity dynamic, in which $dE1/dt$ to $dE3/dt$ are added as pseudo variables. The pseudo variables are a part of the qualitative relations as the other variables.

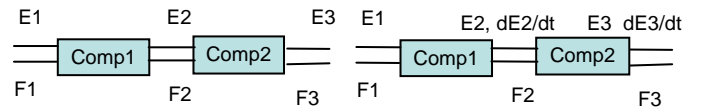


Fig. 2 Dynamic System

For the RC example, the derivative of u_2 (du_2 in figure

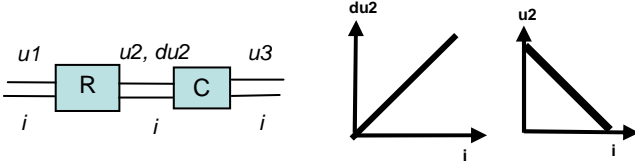
3(a)) is added as the pseudo variable. The qualitative model of the capacitor is:

$$Q(f_c): \{u_2, u_3, du_2\} \rightarrow \{i\} \quad (3)$$

The qualitative model for the resistor is

$$Q(f_r): \{u_1, u_2, du_2\} \rightarrow \{i\} \quad (4)$$

At the *modeling time*, the pseudo variables are computed numerically from their correspondent variables using the simulation data. Then time index is eliminated from the data to obtain value relations between all the variables including the pseudo variables.



(a) Qualitative model (b) relations of i - du_2 and i - u_2
Fig. 3 Example: RC Circuit Qualitative Model

Eliminating the time index from the data is a trivial problem, especially when there is the aide of the simulation tool. Figure 3(b) is the relations between i and du_2 and between i and u_2 . Algorithm 1 then can be used to obtain the qualitative model.

At the *diagnosing time*, we assume the observables are measured along time. If an observable's derivative is a pseudo variable, the derivative values are computed numerically from the observations and supplemented to the diagnosis engine as observations. For the RC example, if du_2 is considered as an observable, one can see there are enough redundant relations to diagnose the dynamic behavior.

One last point is that if more knowledge is used, the qualitative model can be simplified. For example, if the dynamic element and the static element can be identified, the pseudo variables can be added only to the dynamic element, not to the static element. For the RC circuit, the capacitor is a pure dynamic element and the resistor is a pure static element, the qualitative model can be simplified to:

$$Q(f_c): \{du_2\} \rightarrow \{i\} \quad (5)$$

$$Q(f_r): \{u_1, u_2\} \rightarrow \{i\} \quad (6)$$

If we use the knowledge that the current of a resistor is proportional to the difference of the voltages on its two terminals, i.e. equation $(u_1 - u_2)/R = i$, the qualitative model can be:

$$Q(f_c): \{du_2\} \rightarrow \{i\} \quad (7)$$

$$Q(f_r): \{u_1 - u_2\} \rightarrow \{i\} \quad (8)$$

Model Structure Extraction

Model structure extraction is to get the physical connections between components. It is just a technique problem. In Matlab/Simulink, the details of model, e.g. the blocks and the links between blocks are described in a script file. Matlab/Simulink parses the script information and loads the system into its workspace. We can call Matlab/Simulink functions to get the structural information,

more specifically, `get_param()` and `get_link()` are the functions used for this purpose. The function interfaces remain unchanged when software version evolves.

Landmark Determination and qualitative model Abstraction

In the discretization algorithm, landmark selection is crucial. Only if landmarks have necessary and sufficient distinctions, the expected diagnosis results can be obtained. Design engineers can contribute their knowledge in selecting good landmarks. But it is not a reliable way to get landmarks. In this section automatic landmark generation is discussed and the model abstraction algorithm is modified.

Discriminability vs. Domain Partition

Our method is inspired by the discriminability definition in [Struss et al. 02], where the relation of two behavior modes falls into three categories: non-discriminable (ND), deterministically discriminable (DD), and possibly discriminable (PD). In this section we will discuss the relation of domain partition and discriminability. The criterion for selecting landmarks is to keep the necessary and sufficient distinctions between the right and the fault mode, i.e. the deterministic discriminability. In the following context, the two behavior modes are one right mode and one faulty mode.

The notations are the same as in [Struss et al. 02]: V_{obs} is the set of observable variables; $V_{o-cause}$ is the set of "causal" variables in V_{obs} ; and $V_{obs/cause}$ is the set of the rest variables in V_{obs} that are not "causal". For the model abstraction problem, we are only interested by DD scope. Define $SIT_{o-cause}$ is the scope of $V_{o-cause}$ for DD, then ([Struss et al. 02]):

$$SIT_{o-cause} = PROJ_{o-cause}(OPC_i) \setminus PROJ_{o-cause}(PROJ_{obs}(MODEL_{mode1} \cap OPC_i) \cap PROJ_{obs}(MODEL_{mode2} \cap OPC_i)) \quad (9)$$

where PROJ is projection operation, OPC is operation conditions.

In the problem of qualitative model abstraction, the right and fault mode have the same input values, i.e. the $V_{o-cause}$ are the same. Thus the discriminability is determined by the discrepancy of the output, i.e. the projection on $V_{obs/cause}$:

Proposition 1: Assume $V_{o-cause}$ variables take value from tuple $[X1, X2]$, $MODEL_{mode1}$ and $MODEL_{mode2}$ is DD in $[X1, X2]$, iff $PROJ_{obs/cause}(MODEL_{mode1} \cap OPC_i) \cap PROJ_{obs/cause}(MODEL_{mode2} \cap OPC_i) = \emptyset$ (10)

Proof: *efficiency:* assume (10) is satisfied, we need to prove $[X1, X2] \subset SIT_{o-cause}$. (10) means that Mode1 and Mode2 are disjoint when projected on $V_{obs/cause}$ under condition $V_{o-cause} \in [X1, X2]$. So their projections on V_{obs} are also disjoint under condition $V_{o-cause} \in [X1, X2]$. We get: $PROJ_{obs}(MODEL_{mode1} \cap OPC_i) \cap PROJ_{obs}(MODEL_{mode2} \cap OPC_i) = \emptyset$. Thus under condition $V_{o-cause} \in [X1, X2]$, (10) is simplified to

$\text{PROJ}_{\text{o-cause}}(\text{OPC}_i) \setminus \text{PROJ}_{\text{o-cause}}(\emptyset) = \text{PROJ}_{\text{o-cause}}(\text{OPC}_i) = [\text{X1}, \text{X2}]$.

This proved $[\text{X1}, \text{X2}] \subset \text{SIT}_{\text{o-cause}}$.

Necessary: assume $[\text{X1}, \text{X2}] \subset \text{SIT}_{\text{o-cause}}$, we need to prove that (10) is satisfied.

Notice that $V_{\text{o-cause}}$ variable take value from $[\text{X1}, \text{X2}]$ means $\text{PROJ}_{\text{o-cause}}(\text{OPC}_i) = [\text{X1}, \text{X2}]$, thus from (9):

$$\text{PROJ}_{\text{o-cause}}(\text{OPC}_i) \setminus \text{PROJ}_{\text{o-cause}}(\text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode1}} \cap \text{OPC}_i) \cap \text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode2}} \cap \text{OPC}_i)) = \text{PROJ}_{\text{o-cause}}(\text{OPC}_i)$$

That means the second term of the left side is \emptyset . So we have:

$$\text{PROJ}_{\text{o-cause}}(\text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode1}} \cap \text{OPC}_i) \cap \text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode2}} \cap \text{OPC}_i)) = \emptyset$$

That means the term in bracket is \emptyset , so we have

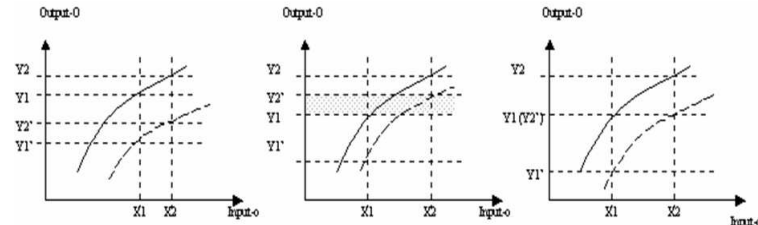
$$\text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode1}} \cap \text{OPC}_i) \cap \text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode2}} \cap \text{OPC}_i) = \emptyset$$

Since $V_{\text{o-cause}}$ takes the same value for mode1 and mode2, we have¹

$$\text{PROJ}_{\text{obs}\backslash\text{cause}}(\text{MODEL}_{\text{mode1}} \cap \text{OPC}_i) \cap \text{PROJ}_{\text{obs}\backslash\text{cause}}(\text{MODEL}_{\text{mode2}} \cap \text{OPC}_i) = \emptyset \quad \square$$

Proposition 1 shows that if the two modes take the same value for $V_{\text{o-cause}}$ variables, the diagnosability is determined by the projections on $V_{\text{obs}\backslash\text{cause}}$ variables. For model abstraction problem, the two modes work under the same operation conditions, and more important, work under the same inputs. Take the observables in inputs as $V_{\text{o-cause}}$, other observables as $V_{\text{obs}\backslash\text{cause}}$, the diagnosability is determined by the observables in $V_{\text{obs}\backslash\text{cause}}$.

Intuitively, if the domain partition is too coarse, the



(a)DD with good margin (b) ND (c) DD with no margin
Figure 4: the limitation of partition for discriminability

output ranges of the two modes will be overlapped. In this case, such that the two modes are undiscriminable (cf. figure 4). In other word, if the discrepancy between the two modes is larger, the domain partition can be coarser. Assume the two behavior modes have numeric models: $Y=f1(X)$ and $Y=f2(X)$. $\text{MODEL}_{\text{mode1}}$ and $\text{MODEL}_{\text{mode2}}$ are the qualitative models, so $\text{MODEL}_{\text{mode1}}=q(f1)$ and $\text{MODEL}_{\text{mode2}}=q(f2)$. If $\exists [X1 \text{ X2}]$, $q(f1): [X1 \text{ X2}] \rightarrow [Y1 \text{ Y2}]$, $q(f2): [X1 \text{ X2}] \rightarrow [Y1' \text{ Y2}]$.

From proposition1, if

$$[Y1 \text{ Y2}]_{\text{obs}} \cap [Y1' \text{ Y2}]_{\text{obs}} = \emptyset, \quad (11)$$

The $[\text{X1} \text{ X2}]$ belongs to DD range. In (11) the $[Y1 \text{ Y2}]_{\text{obs}}$ is the observables in $[Y1 \text{ Y2}]$. This is the case in Figure4(a).

$$\text{If } [Y1 \text{ Y2}]_{\text{obs}} \cap [Y1' \text{ Y2}]_{\text{obs}} \neq \emptyset \quad (12)$$

The $[\text{X1} \text{ X2}]$ belongs to non-DD range. This is the case in Figure4(b).

The limit between DD and non-DD is as Figure 2(c):

$$[Y1 \text{ Y2}]_{\text{obs}} \cap [Y1' \text{ Y2}]_{\text{obs}} = Y1'_{\text{obs}} = Y2_{\text{obs}}, \text{ or} \quad (13)$$

$$[Y1 \text{ Y2}]_{\text{obs}} \cap [Y1' \text{ Y2}]_{\text{obs}} = Y2'_{\text{obs}} = Y1_{\text{obs}} \quad (14)$$

Figure 4(c) is the coarsest partition for V_{obs} that still keeps DD. It is easy to prove if the partition is coarser, the modes are non-DD².

Corollary: The boundary of the coarsest partition is the surface where the two modes joint.

For monotonic functions, the coarsest landmark is easy to compute:

Proposition 2: Assume $\text{MODEL}_{\text{mode1}}$ and $\text{MODEL}_{\text{mode2}}$ have quantitative models $f1$ and $f2$. $f1$ and $f2$ are monotonic.

$\{X1, X2, \dots, Xi, \dots\}$ are the input points. The coarsest partition for $V_{\text{o-cause}}$ satisfies

$$f1(X1) = f2(X2)$$

$$f1(X2) = f2(X3)$$

...

$$f1(Xi) = f2(Xi+1)$$

When $V_{\text{o-cause}}$ get the coarsest partition $\{X1, X2, \dots, Xi, \dots\}_{\text{obs}}$, $V_{\text{obs}\backslash\text{cause}}$ get the coarsest partition $\{f1(X1), f1(X2), \dots, f1(Xi), \dots\}_{\text{obs}}$.

Proposition 2 provides a way to generate new landmarks. It is possible to numerically compute $Xi+1$ from Xi . For non-monotonic functions, proposition 2 does not hold. In

the next section, a non-optimal but satisfactory solution of landmark generation is presented.

Model Abstraction with Landmark Generation

The method presented in this section is relied on one fact that if the domain partition is finer, the discriminability can be improved. $\mathbf{X} = f(t)$ is a dynamic system. The simulation time is from 0 to T_c . The algorithm 2 starts from the coarsest landmark $[\text{LOC}_1, \text{LOC}_2]$, in which LOC_1 and LOC_2 is the lower bound and upper bound of $X_{\text{o-cause}}$. From the simulation data, the discriminability on $[\text{LOC}_1, \text{LOC}_2]$ is examined (based on Proposition 1). If $[\text{LOC}_1, \text{LOC}_2]$ is not a DD range, that might mean that this partition is too coarse. $[\text{LOC}_1, \text{LOC}_2]$ is split from the medium point, i.e. $(\text{LOC}_1 + \text{LOC}_2)/2$ is added as a new landmark. $[\text{LOC}_1, (\text{LOC}_1 + \text{LOC}_2)/2]$ and $(\text{LOC}_1 + \text{LOC}_2)/2, \text{LOC}_2]$ are two intervals to be checked. The split process will continue until a DD scope is found, or the split makes the intervals smaller than a pre-defined minimum length D . Algorithm 2 records the generated landmarks, the qualitative relations,

¹ This can be easily prove by assume $\text{PROJ}_{\text{obs}\backslash\text{cause}}(\text{MODEL}_{\text{mode1}} \cap \text{OPC}_i) \cap \text{PROJ}_{\text{obs}\backslash\text{cause}}(\text{MODEL}_{\text{mode2}} \cap \text{OPC}_i) \neq \emptyset$. Since $V_{\text{o-cause}}$ take the same value for mode1 and mode2, we have $\text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode1}} \cap \text{OPC}_i) \cap \text{PROJ}_{\text{obs}}(\text{MODEL}_{\text{mode2}} \cap \text{OPC}_i) \neq \emptyset$, conflict.

² Without loss of generality, assume $f1$ and $f2$ is monotonic as figure 2(c), and $f1(X1) = f2(X2)$. If $V_{\text{o-cause}}$ has a larger partition $[\text{X3}, \text{X2}]$, where $\text{X3} < \text{X1}$, we get $f1(\text{X3}) < f1(\text{X1}) = f2(\text{X2})$ and $f2(\text{X3}) < f2(\text{X1}) < f1(\text{X1})$. Thus $[f1(\text{X3}), f1(\text{X2})] \cap [f2(\text{X3}), f2(\text{X2})] = [f1(\text{x3}), f1(\text{x1})] \neq \emptyset$.

as well as the discriminability property on each input partitions.

Algorithm2: qualitative model abstraction $\mathbf{X} = f(t)$

Input:

D: Minimum landmark interval

Tc: duration of simulation time

f, f' : Quantitative models for two modes,

$V_{o\text{-cause}} = \{x_i \mid x_i \in \mathbf{X}\}, V_{obs\backslash cause} = \{x_j \mid x_j \in \mathbf{X}\}, V_{obs\backslash cause} \cup V_{o\text{-cause}} \subseteq \mathbf{X}$

$[LOC_1, LOC_2]$: the start landmark for $V_{o\text{-cause}}$, i.e. $LOC_1 = f_{o\text{-cause}}(0), LOC_2 = f_{o\text{-cause}}(Tc)$

Output:

DD: Vector for input scope that system are DD

ND: Vector for input scope that system are non-DD (PD or ND)

q : Vector for storing qualitative model

loop: the Boolean variable controls loop, initialized as true

Internal Variables:

p : stack to store input tuples

1: Store $[LOC_1, LOC_2]$ in p

2: While p is not empty

3: pop a tuple $[LOC_i, LOC_{i+1}]$ from p

4: find t_i and t_{i+1} correspondent to LOC_i, LOC_{i+1}

5: $LONC_i = \min\{f_{obs\backslash cause}(t) \mid t_i < t < t_{i+1}\}$

6: $LONC_{i+1} = \max\{f_{obs\backslash cause}(t) \mid t_i < t < t_{i+1}\}$

7: $LONC'_i = \min\{f'_{obs\backslash cause}(t) \mid t_i < t < t_{i+1}\}$

8: $LONC'_{i+1} = \max\{f'_{obs\backslash cause}(t) \mid t_i < t < t_{i+1}\}$

9: if $[LONC_i, LONC_{i+1}] \cap [LONC'_i, LONC'_{i+1}] = \emptyset$,
(that means $[LOC_i, LOC_{i+1}]$ is in DD scope)

10: store $[LOC_i, LOC_{i+1}]$ in vector DD

12: store $\{[\min\{f(t) \mid t_i < t < t_{i+1}\}, \max\{f(t) \mid t_i < t < t_{i+1}\}]\}$ in vector q

13: remove $[LOC_i, LOC_{i+1}]$ from p

14: else

15: $mid = (LOC_i + LOC_{i+1})/2$

16: if $|LOC_i - mid| \leq D$ or $|LOC_{i+1} - mid| \leq D$

17: store $\{[\min\{f(t) \mid t_i < t < t_{i+1}\}, \max\{f(t) \mid t_i < t < t_{i+1}\}]\}$ in vector q

18: store $[LOC_i, LOC_{i+1}]$ in vector ND

19: remove $[LOC_i, LOC_{i+1}]$ from p

20: else

21: push $[LOC_i, mid]$ and $[mid, LOC_{i+1}]$ into q

22: end-if

23: end-if

24: end-while

25: report DD, ND, q

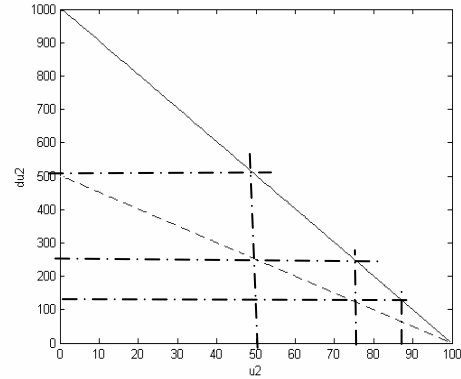
The key issue for algorithm 2 is the splitting procedure that refines the qualitative relation until to the level the fault is discriminable.

Resume the RC example in section 3.3. The voltage $u1$, $u2$, and $u3$ are measurable observables. $du2$, the derivative of $u2$, is the pseudo variable and is also a supplementary observable. The fault considered is the resistance of the resistor doubled, which causes the transient process slower. $u1$ and $u3$ are constant ($u1 = 100v, u3 = 0v$) in this

example. $u2$ is chosen as $V_{o\text{-cause}}$, and $du2$ as $V_{obs\backslash cause}$. Figure 5 is the relation of $u2$ and $du2$ under the right (solid line) and faulty modes (dotted line). Using algorithm 2, the split process is like figure 5.

Some comments on algorithm 2:

1. the partitions obtained from algorithm 2 are not the coarsest but the satisfactory one for diagnosis purpose. It is the



($R=100\text{ohm}, C=0.001F$ for the right mode,
and $R=200\text{ohm}, C=0.001F$ for the faulty mode)

Fig. 5 Landmark Determination and Qualitative Model Abstraction

trade-off of optimization and computation cost.

2. the success of algorithm 2 depends on the selection of the variables to be split. Normally the most influential variables are chosen as the *base variables*. The split of the base variables can cause the largest change on the output variables. It needs special techniques to determine which variables are the most influential variables. The causal ordering algorithm [Iwasaki and Simon, 1994] can be used for this purpose. The base variables used in the RC circuit and in the demonstration case in this paper are selected by experience.

3. For the monotonic functions, the refinement of domain partition always refines the distinctions of $V_{obs\backslash cause}$. For the non-monotonic functions, it is not true due to the local extrema. But it is sure that the partition refinement doesn't remove the distinctions of $V_{obs\backslash cause}$.

4. This algorithm considers only partitions on continuous variables. For discrete variables, normally we regard them as different operation mode. For example: the switch can be on and off. They are considered as two operation modes. Thus this algorithm is suitable for most of the system.

5. For continuous variable, the valid value is bounded by working environment. For example, for a normal AC system, we consider the outside temperature is from -20 to 40 .

Demonstration

A simple Air Conditioning system has 3 components, Blower, Distribution and Cabin (figure 6). Figure 6(a) is the model in Matlab/Simulink, while figure 6(b) is in block schema with the input and output variables for each block. p_i is pressure, f_i is airflow rate, E is the electricity power

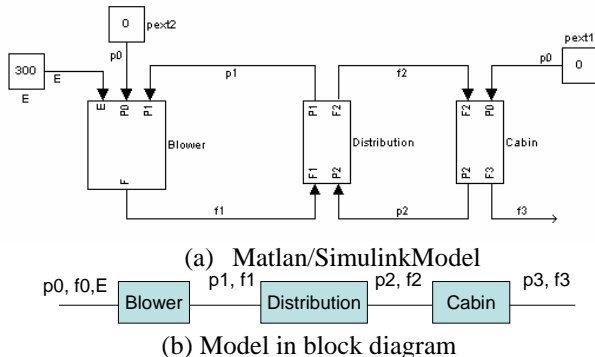
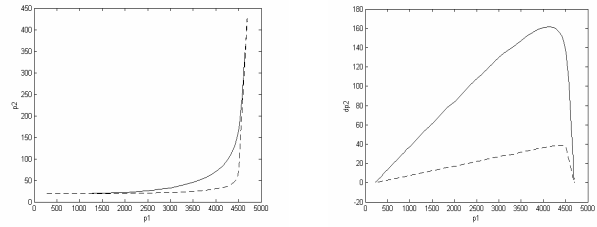


Figure 6: AC system with 3 components

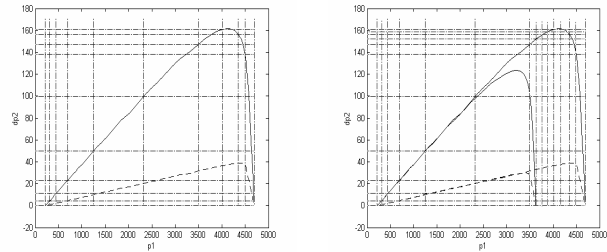
driving the blower. The flow rate and pressure inside the system increase when the blower begins to work, and they reach a stable point when E is unchanged. If the cabin volume increases, the transient procedure is slower than normal case but the same stable point can be reached. It is difficult to manually determine the landmarks for the variables. The algorithm 2 can deal it with. Suppose we can measure any pressure if necessary because normally pressure is easier to measure than flow rate. Since we already know p_0 and p_3 are equal to outside air pressure, they have no influence on diagnosability. Consider $V_o = \{p_1, p_2, dp_2\}$, where dp_2 is the derivative of p_2 . The relations of p_1-p_2 and p_1-dp_2 are drawn from simulation data as in Figure 7, where the solid curve is for the right mode and the dotted line is for the faulty mode. One can see that the relations of p_1-p_2 at the two modes are too close to distinguish the two modes, but the relations of p_1-dp_2 have good distance to each other. And if p_1 is the base variable to be split, the two modes can be distinguished. We choose $V_{o-cause} = \{p_1\}$ and $V_{obs/cause} = \{p_2, dp_2\}$. The landmarks for p_1 and dp_2 are listed in table 1. Figure 8 shows the partitions on p_1-dp_2 . Figure 8(a) is the result of 6 times of split. Except the most right and left interval of p_1 , the other intervals are Deterministic Diagnosable region. The landmarks of other variables are computed accordingly, which are not showed in this paper. Figure 8(b) shows the partition result when E changes. The two solid curves are for $E = 500$ and $E = 300$ respectively. The area between the two curves are the right behaviour when $300 \leq E \leq 500$. The faulty mode is the

| p_1 | dp_2 |
|-----------|----------|
| 209.7617 | 0.3072 |
| 307.2409 | 4.4389 |
| 446.2227 | 11.2196 |
| 697.8665 | 22.7634 |
| 1246.9854 | 49.7219 |
| 2326.6505 | 99.5160 |
| 3491.1238 | 147.2230 |
| 4019.3584 | 160.8867 |
| 4350.6848 | 156.5737 |
| 4498.3403 | 138.0294 |
| 4690.4157 | 0.0 |

Table 1 Landmarks for p_1 and dp_2



(a) Relation of p_1-p_2 (solid line is right mode, dotted line is faulty mode)
 (b) Relation of p_1-dp_2
 Fig. 7 Model of Air Conditioning System



(a) $E = 500$ (b) $300 \leq E \leq 500$
 Fig. 8 partition on the relation p_1-dp_2

area between the two dotted curves. The partitions are result after 6 split. One can see that after $p_1 > 3500$, the refinement of landmarks does not help to increase the diagnosability. For the algorithm 2, the split continues and generates some landmarks that do not help to distinguish the fault.

Discussion and conclusion

This paper bridges the gap between the numeric simulation model and the qualitative model for diagnosis purposes. The problem can be classified into four classes: 1) known landmark, static system; 2) known landmark, dynamic system; 3) unknown landmark, static system; 4) unknown landmark, dynamic system. The first class can be solved by algorithm 1. The performance of algorithm 1 is discussed in section 3.2. The second class can be transformed to the first class if the time information is eliminated from the simulation data. Similarly, the fourth class can be transformed to the third class in this way. For the third class, this paper reveals the relation of discriminability and model partition. The approximation of the qualitative model should keep the distinctions between the right and faulty behaviours. Beginning with the coarsest domain partition, algorithm 2 is a refining process, generating new landmarks until the target modes can be distinguished at the new, finer partitions.

Algorithm 2 can be used as a generalized approach for both static and dynamic systems and both monotonic and non-monotonic cases. Algorithm 2 is limited in two ways. First only single fault is considered. This needs further

work, but the principles developed here can be used. Secondly, the approach is system-context dependent and diagnosis task dependent. That means the abstracted qualitative model depends on the current system structure and the considered fault. If the component model is reused in another system context or to diagnose other faults, we can not guarantee the fault is detectable. This is a compromise of data explosion because theoretically a universal qualitative model contains an unlimited amount of information, which is unable to be described by finite domains. After this project, we believe no universal qualitative model exists. The only feasible way is to get a qualitative model under certain conditions. Based on this, our algorithm has many advantages: first it is a one-step method. By running one process, all component models are obtained. Practically it is not a big deal to run it on each system even if the component model is not reusable. Second the considered fault is guaranteed to be detected using the resulted model. Third it avoids possible conflicts when the shared variables among components are no in the same scope if the component models are collected one by one. From our experience, this approach is very practical in dealing with complex real-world industrial applications.

References

- Brooks, M. 1984., Approximation Complexity for Piecewise Monotone Functions and Real Data. *Computers and Mathematics with Applications* 27(8).
- Dressler, O. 1996. On-line Diagnosis and Monitoring of Dynamic Systems based on Qualitative Models and Dependency-recording Diagnosis Engines, in Proceedings of the 12th European Conference on Artificial Intelligence, 481-485.
- Dupre, D. and Panati, A. 1998. State-based vs simulation-based diagnosis of dynamic systems. In Proceedings of the 9th International Workshop on Principles of Diagnosis, 40-46.
- Dvorak, D. and Kuipers, B. 1992. Model-based Monitoring of Dynamic Systems, in *Readings in Model-based Diagnosis*: 249-254. Morgan Kaufmann Publishers.
- Iwasaki, Y. and Simon, H. 1994. Causality and Model Abstraction. *Artificial Intelligence* 67(1):143-194.
- Karnopp D. and Rosenberg, R. 1975, *System Dynamics: A Unified Approach*, John Wiley & Sons, Inc.
- Kuipers, B. 2001. Qualitative Simulation. In R.A. Moyers (Ed.) *Encyclopedia of Physical Science and Technology*, Third Edition, NY Academic Press.
- Lunze, J., Nixdorf, B. and Schreoder, J. 1999. Deterministic Discrete-event Representations of Linear Continuous-variable Systems, *Automatic* 35:395-406.
- Malik, A. and Struss, P. 1996. Diagnosis of Dynamic Systems Does Not Necessarily Require Simulation. In Proceedings of the 10th International Workshop on Qualitative Reasoning, 127-136.
- Mosterman, P. and Biswas G. 1997. Model Based Diagnosis of Dynamic System. In *Seventh Journées de L.I.P.N.*,134-154, University of Paris Nord, Villetaneuse, France.
- Panati, A. and Dupre, D. 2000. State-based vs simulation-based diagnosis of dynamic systems. In Proceedings of the 14th European Conference on Artificial Intelligence, 176-180.
- Sachenbacher, M. and Struss, P. 2001. AQUA : A Framework for Automated Qualitative Abstraction. In Proceedings of 15th International Workshop on Qualitative Reasoning, 5-12.
- Schit, C. and Bredeweg, B. 1996. An overview of approaches to qualitative Model Construction. *The Knowledge Engineering Review* 11(1):1-25.
- Struss, P., Refus, B., Cascio, F., Console, L. Dague, P., Dubois, P., Dressler, O., and Millet, D. 2002. Model-based Tools for the Integration of Design and Diagnosis into a Common Process – A Project Report. In Proceedings of 13th International Workshop on Principles of Diagnosis, 25-32.
- Struss, P. 1997. Fundamentals of Model-Based Diagnosis of Dynamic Systems. In Proceeding of the 15th International Joint Conference on Artificial Intelligence, 480-485.
- Struss, P. 2002. Automated Abstraction of Numerical Simulation Models – Theory and Practical Experience. In Proceedings of Sixteenth International Workshop on Qualitative Reasoning, p161-168.