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#### **Publisher's version / Version de l'éditeur:**

<https://doi.org/10.1016/j.fuel.2021.121110>

*Fuel*, 302, 15 October 2021, pp. 1-13, 2021-05-29

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# 1 Effect of pre-main-post diesel injection strategy on greenhouse gas and nitrogen oxide 2 emissions of natural gas/diesel dual-fuel engine at high load conditions

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## 5 Abstract

6 Natural gas/diesel dual-fuel (NDDF) engine technology is an interesting concept for decreasing greenhouse gas  
7 (GHG) emissions of heavy-duty diesel engines. One of the main limitations of this concept is the emissions of  
8 unburned methane which is estimated to have a GHG potential factor of 25 – 34 over a 100-year period. Our previous  
9 study has shown that a NDDF engine using pre-main-post diesel injection strategy can reduce unburned methane  
10 emissions compared to that using single diesel injection strategy under high engine load conditions. However, it  
11 yields lower indicated thermal efficiency (ITE) and higher carbon dioxide (CO<sub>2</sub>) and nitrogen oxides (NO<sub>x</sub>) emissions  
12 due to the advanced combustion phasing. In this study, the combustion phasing of pre-main-post diesel injection  
13 strategy is further optimized with the goal to improve the ITE and reduce the GHG and NO<sub>x</sub> emissions without  
14 compromising the unburned methane emissions when compared to single injection strategy. The results reveal that  
15 changing pre diesel injection timing gives more controllability of the combustion phasing than changing the main  
16 and post diesel injection timing. A more homogenous premixed mixture of pre injected diesel – natural gas – air  
17 retards the combustion phasing which allowed further improvement of the ITE and GHG emissions of NDDF engines  
18 while maintaining the low unburned methane emissions feature of the pre-main-post injection strategy. It is found  
19 that the optimized pre-main-post diesel injection strategy is able to reduce unburned methane, GHG, and NO<sub>x</sub>  
20 emissions by 13.4%, 1.5%, and 42%, respectively, and increase ITE by 0.37% compared to single injection strategy.

21 **Keywords:** natural gas; diesel; pre-main-post injection strategy; dual-fuel engine; GHG and NO<sub>x</sub> emissions.

## 22 1. Introduction

23 Despite the extensive use of diesel engines in transportation and various other industries over the last century,  
24 the future sustainability of the diesel fueled compression ignition (CI) engines is subject to speculation. The reason  
25 is that the combustion of diesel fuel still generates significant carbon dioxide (CO<sub>2</sub>) emissions and the diffusion

26 combustion inside the cylinder of diesel engines leads to high levels of nitrogen oxides (NO<sub>x</sub>) and particulate matter  
27 (PM) emissions. The Paris Agreement on climate change which was adopted in 2015 aims to strengthen the global  
28 response to the threat of climate change by “limiting the global average temperature rise to well below 2 degrees  
29 Celsius and pursue efforts to limit the increase to 1.5 degrees Celsius” compared to pre-industrial levels [1]. This goal  
30 requires an extensive reduction in greenhouse gas (GHG) emissions and signatory nations were requested to show  
31 their own numerical goals. For instance, the Government of Canada has committed to a 30% and 80% reduction in  
32 GHG emissions by 2030 and 2050, respectively, relative to the recorded emissions in 2005 [2]. This has exerted  
33 significant pressure on industries using diesel engines. The technological advancements and continuous  
34 improvement of diesel engines and after-treatment devices have significantly reduced the exhaust NO<sub>x</sub> and PM  
35 emissions of the CI diesel engines over the last couple of decades [3–7]. Moreover, the fact that CI engines are some  
36 of the most efficient combustion engines makes them well suited for not only heavy-duty transportation, but also  
37 power generation and marine industries. Therefore, despite the surge of electrification and hybridization in light-  
38 duty vehicles, it is projected that CI engines will still play a predominant role in major industries until 2050 [8].  
39 However, the urgency to reduce GHG emissions requires additional steps towards the decarbonisation of CI diesel  
40 engines. Improvement of engine efficiency and implementation of alternative cleaner fuels seem to be two apparent  
41 solutions to this problem.

42 Natural gas as a low-carbon fuel is potentially a feasible alternative fuel for use in CI engines to replace diesel and  
43 meet stringent emission regulations. It is mainly composed of methane (CH<sub>4</sub>) which produces lower CO<sub>2</sub> emissions  
44 compared to gasoline and diesel when it combusts completely. When compared with other alternative fuels (i.e.,  
45 ethanol, methanol, hydrogen, biogas, etc.), natural gas has advantages of relatively lower cost, abundant reserves,  
46 global distribution network as well as mature infrastructure for storage and delivery. Natural gas/diesel dual-fuel  
47 (NDDF) concept enables the utilization of natural gas in existing CI diesel engines [9–13]. In this concept, diesel  
48 directly-injected into the engine cylinder provides an ignition source for the premixed natural gas – air mixture.  
49 Typically, a conventional diesel engine can be modified into a NDDF engine without significant changes to the original  
50 design. The major change is the addition of a natural gas supply system to the stock diesel engine, which slightly  
51 increases control complexity of the fueling system [14]. Conventional NDDF engines produce significant amounts of

52 unburned methane and GHG emissions and demonstrate lower thermal efficiency at low to medium load conditions  
53 compared to their counterpart diesel engines [13,15–17]. This is mainly due to the extra lean premixed charge of  
54 natural gas – air mixture which causes the flame propagation failure at low to medium load conditions. Several  
55 strategies have been investigated to improve the thermal efficiency and unburned methane and GHG emissions of  
56 NDDF engines at low to medium load conditions. Advancing diesel injection timing [11,14,16,18–20], increasing  
57 diesel injection rail pressure [21–23], using split diesel injection [15,24–27], and stratification of natural gas – air  
58 mixture [28–31] have been the most important strategies to achieve these goals.

59 Several studies have also shown that NDDF engines can achieve comparable or sometimes higher thermal  
60 efficiency and lower GHG emissions compared to their counterpart diesel engines under medium to high load  
61 conditions [16,32–38]. For instance, Guo et al. [20] examined the effect of natural gas energy fraction on thermal  
62 efficiency and CO<sub>2</sub> equivalent (or GHG) emissions of a NDDF engine at high load conditions. They found that the  
63 NDDF engine mode achieves higher thermal efficiency and lower CO<sub>2</sub> equivalent (i.e., CO<sub>2</sub> equivalent = CO<sub>2</sub> + 25 ×  
64 CH<sub>4</sub>) emissions than the diesel engine mode. Rimmer et al. [37] compared the combustion performance and exhaust  
65 emissions of a NDDF engine mode with those of diesel engine mode at high load conditions. They also reported that  
66 the NDDF engine obtains higher thermal efficiency and lower GHG emissions compared to the diesel engine mode  
67 at high load conditions [37]. This is due to the fact that the premixed natural gas – air mixture equivalence ratio is  
68 high enough to obtain stable flame propagation after its ignition by diesel.

69 To the best of authors' knowledge, no research effort had been expended towards providing effective measures  
70 for further improvement in thermal efficiency and emissions of NO<sub>x</sub>, unburned methane, and GHG of NDDF engines  
71 at medium to high load conditions. This is mainly because of the already higher thermal efficiency and lower GHG  
72 emissions of NDDF engines at medium to high engine load conditions compared to their counterpart diesel engines.  
73 However, according to the Phase (II) of Environmental Protection Agency's (EPA's) GHG regulation which starts in  
74 2021, the global warming potential factor for methane will increase from 25 to 34, making the GHG impact of  
75 methane emissions more severe [39]. Moreover, for the EPA Tier 4 final of off-road diesel engines for the power  
76 generation category of up to 560 kW and above, the NO<sub>x</sub> emissions mandate is 0.4 g/kWh [40]. Therefore, developing  
77 strategies to simultaneously improve thermal efficiency and reduce emissions of NO<sub>x</sub>, unburned methane, and GHG

78 originating from NDDF engines at medium to high load conditions is also of great importance. In a recent study [10]  
79 we proposed a new diesel injection strategy named ‘pre-main-post’ diesel injection strategy to further reduce the  
80 unburned methane emissions of NDDF engines at high load conditions. In this diesel injection strategy, part of the  
81 diesel fuel was injected before the main injection during the compression stroke (pre-injection) and part of the diesel  
82 fuel was injected after the main injection during the expansion stroke (post-injection). It was found that pre-main-  
83 post diesel injection strategy had the potential to decrease the unburned methane emissions of NDDF engines  
84 compared to the single diesel injection strategy under high engine load conditions [10]. However, the thermal  
85 efficiency of the investigated NDDF engine with pre-main-post diesel injection strategy was lower than that of single  
86 diesel injection due to the overly advanced combustion phasing, which leads to higher GHG emissions of pre-main-  
87 post diesel injection strategy compared to those of single diesel injection strategy [10].

88 In this paper the combustion phasing of a NDDF engine with pre-main-post diesel injection strategy is further  
89 optimized by tuning the diesel injection timings (i.e., pre, main, and post diesel injection timings) to improve the  
90 thermal efficiency and GHG and NO<sub>x</sub> emissions of the NDDF engine without compromising the unburned methane  
91 emissions compared to the NDDF engine with single diesel injection strategy. A computational fluid dynamic (CFD)  
92 model based on CONVERGE 3.0 software is used to simulate the in-cylinder combustion process and help understand  
93 the underlying mechanisms of the experimental observations.

## 94 **2. Experimental setup and methods**

### 95 *2.1. Experimental apparatus*

96 The experimental setup used in this paper is the same as that in our previous paper [10]. A modified single cylinder,  
97 four stroke, heavy-duty CAT 3401 base diesel engine is used for the engine tests. Figure 1 shows a schematic of the  
98 main components of the experimental setup and Table 1 outlines the relevant specifications of the engine. The  
99 engine is coupled with necessary auxiliary systems such as common-rail direct injection (DI) diesel fuel supply  
100 systems, charge-air, gaseous port fuel injection (PFI), data acquisition (DAQ) system, as well as exhaust gas emissions  
101 analyzer and engine control unit. The common-rail injection system is externally powered by a high-pressure fuel  
102 pump and is capable of producing diesel injection pressure up to 1800 bar. A Bronkhorst mini CORI-FLOW mass flow

103 meter was used to monitor the diesel mass flow rate. A port fuel injection (PFI) system consisting of eight gas  
 104 injectors (manufactured by Alternative Fuel Systems Inc, Calgary, Alberta) and a Bronkhorst in-flow IP-65 flow meter  
 105 which measured the flow rate of natural gas were added to introduce natural gas to the engine. National Instruments  
 106 (NI) hardware (PXI-1031 chassis with PXI-8184 embedded controller) and LabVIEW-based software were used to  
 107 control the injection timing, pulse width, and injector pressure of both diesel and natural gas.

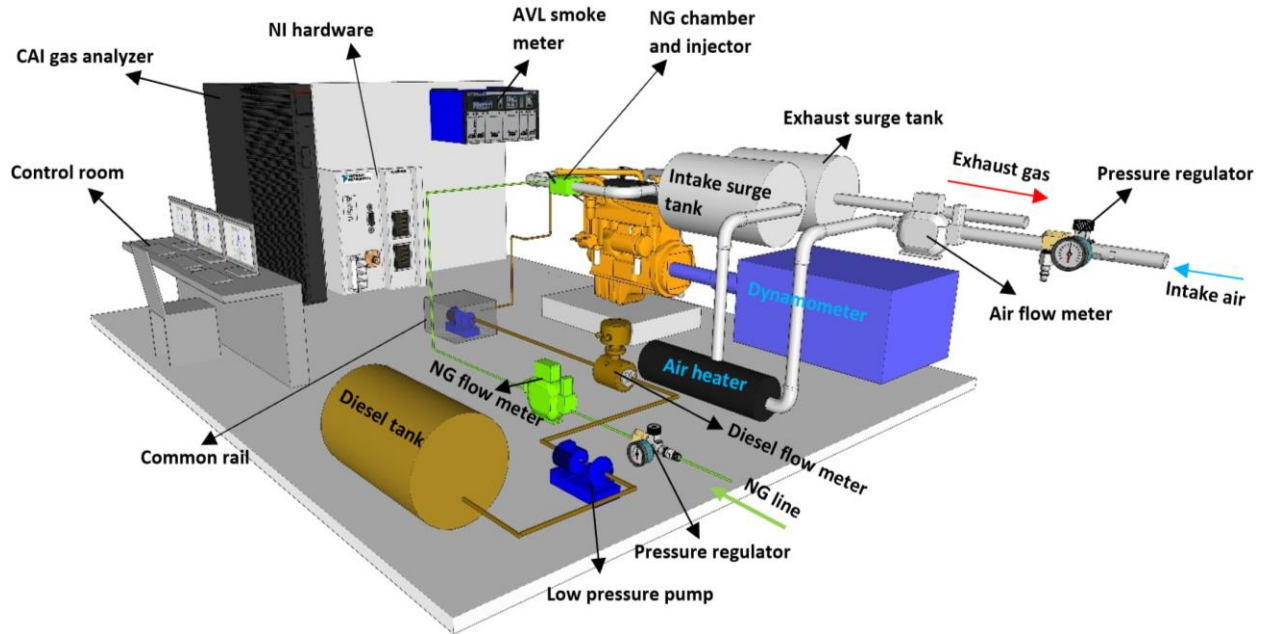


Fig. 1: Schematic of the experimental setup

108

**Table 1.** Engine specifications.

Engine model	Caterpillar 3401
Number of cylinders	1
Bore × Stroke (mm × mm)	137.2 × 165.1
Conn. rod length (mm)	261.62
Compression ratio	16.25
Displacement (L)	2.44
Combustion chamber type	Quiescent
Diesel injector	Ganser CRS AG injector
No. diesel injector hole × diameter (mm)	6 × 0.21
Natural gas injector	AFS Inc. GS60 injectors
Maximum power (kW)	74.6 (@ 2100 RPM)
Maximum torque (N.m)	441 (@ 1200 RPM)

109

110 The intake charge-air system was equipped with a compressed air supply which supplied a pressure of 5.50 bar  
 111 to the engine test cell, a Fisher-Emerson control valve to regulate the intake air pressure, a turbine type mass

112 flowmeter manufactured by Sierra Instruments Inc., and a by-pass heater located upstream of the intake surge tank  
113 to provide a desirable intake air temperature. Surge tanks were used before the intake and after the exhaust  
114 manifolds to reduce the pressure oscillations during the test. An exhaust back pressure valve was installed  
115 downstream of the exhaust surge tank to control the exhaust pressure. The emissions analyzing system comprised  
116 of a set of California Analytical Instruments' 600 series analyzers which obtained the gas sample from the engine  
117 exhaust pipe through a heated line. The analyzers measured the concentrations of NO<sub>x</sub> (detection limit: 5,000 ppm,  
118 resolution: 1 ppm), CH<sub>4</sub> (detection limit: 3,000 ppm, resolution: 1 ppm), carbon monoxide (CO) (detection limit: 5,000  
119 ppm, resolution: 1 ppm), and CO<sub>2</sub> (detection limit: 20% vol., resolution: 0.01% vol.) in the exhaust gas.

120 An eddy current (EC) dynamometer was connected to the test engine in order to control the engine load according  
121 to the experimental requirements. An AVL angle encoder (365C) with a speed ranging from 50 to 20,000 RPM and a  
122 resolution of 0.01 CAD was used to determine the angular position of the crankshaft and engine speed. An AVL  
123 Digalog Test- mate system was used to interface with the engine electronic control unit to control the engine load  
124 and speed. An electric motor was used for motoring the engine to an engine speed of 500 revolution per minute  
125 (rpm), and subsequently the diesel fuel injection was initiated to fire the engine. A k-type thermocouple installed  
126 slightly down-stream of the exhaust valves measured the exhaust gas temperature. The exhaust gas temperature,  
127 lubricating oil pressure, exhaust gas oxygen concentration, exhaust gas emissions, flow rates of natural gas, diesel,  
128 and air, and cooling water temperature were recorded by a DAQ system based on LabVIEW platform over three  
129 minutes for each steady state test condition. A Kistler Piezo-Star 6125C pressure transducer continuously recorded  
130 cylinder pressure over 100 consecutive cycles at a sampling resolution of 0.2 crank angle degree (CAD). The cylinder  
131 pressure value was used to calculate the heat release rate (HRR) and other combustion characteristics.

## 132 2.2. Test Fuels

133 All tests were carried out using natural gas supplied by Enbridge Inc. and Canadian ultra-low sulfur diesel (ULSD).  
134 The lower heating value (LHV) of natural gas is 48.22 MJ/kg and that of diesel is 43.17 MJ/kg. The hydrogen to carbon  
135 (H/C) ratio of natural gas and diesel are 3.93 and 1.89, respectively. More properties of natural gas and diesel fuel  
136 can be found in Table 2.

**Table 2.** Fuel properties.

Property	Natural gas	Diesel
Density (kg/m <sup>3</sup> )	0.711 (@ 15 °C and 1 atm)	814
Cetane number	-	44
LHV (MJ/kg)	48.22	43.17
H/C ratio	3.93	1.89
Composition (%vol.)	CH <sub>4</sub> : 95.17 C <sub>2</sub> H <sub>6</sub> : 3.22 CO <sub>2</sub> : 0.779 N <sub>2</sub> : 0.743 Other component: 0.088	-

137

138 *2.3. Experimental procedure and operating conditions*

139 In this study, a break mean effective pressure (BMEP) of 12.15 bar which is equivalent to 75% of full engine load  
140 is selected for the experiments with a natural gas energy fraction of 50% and an engine speed of 910 rpm. The  
141 selected engine load and speed is similar to the 13-mode EPA Supplemental Emissions Test (SET) of heavy-duty  
142 engines. It is noted that during experiments, the control system adjusts the mass flow rates of diesel and natural gas  
143 to maintain the engine load at BMEP of 12.15 bar. Since PM emissions are no longer a main issue in NDDF engines  
144 and high-pressure diesel injection usually increases the peak pressure rise rate (PPRR) and NO<sub>x</sub> emissions, a high-  
145 pressure diesel injection is not necessary. On the other hand, very low injection pressure is not desirable in order to  
146 ensure the atomization quality of diesel. Therefore, an appropriate diesel injection pressure of 525 bar was selected  
147 in all tests of this investigation. Natural gas injection pressure and timing were maintained at 4.4 bar and -355° after  
148 top dead center (ATDC), respectively. The intake pressure, intake temperature, and exhaust back pressure were fixed  
149 at 1.80 bar, 40 °C, and 1.95 bar, respectively. To prevent engine damage, the maximum PPRR, cylinder pressure, and  
150 exhaust gas temperature were maintained below 14 bar/CAD, 150 bar, and 600 °C, respectively. As shown in Table  
151 3, the ratio of pre-injected diesel fuel was fixed at 25% for the pre-main-post and pre-main injection strategies. This  
152 is due to the fact that increasing and decreasing the ratio of pre-injected diesel led to significant increase of the PPRR  
153 and unreliable delivery of pre-injected diesel fuel, respectively, during the test.. To maintain stable combustion, the  
154 coefficient of variation (COV) of indicated mean effective pressure (IMEP) was kept lower than 5%. In order to record  
155 reliable exhaust emissions data, each test point reported in this paper represents the average of data collected over  
156 a three minute duration at steady-state conditions, which was achieved when the exhaust gas temperature varied  
157 by less than 1%.

158 Table 3 shows different diesel injection strategies used in the experiments. A schematic of diesel injection strategy  
 159 is also shown in Fig. 2. It is noted that SODI and EODI are defined as the start of diesel injection and end of diesel  
 160 injection, respectively. Diesel pulse width ratio (%PWR), which is calculated using Eq. (1), is defined as the ratio of  
 161 pulse width (PW) of each injection pulse (pre, main, or post) to the total diesel injection pulse width.

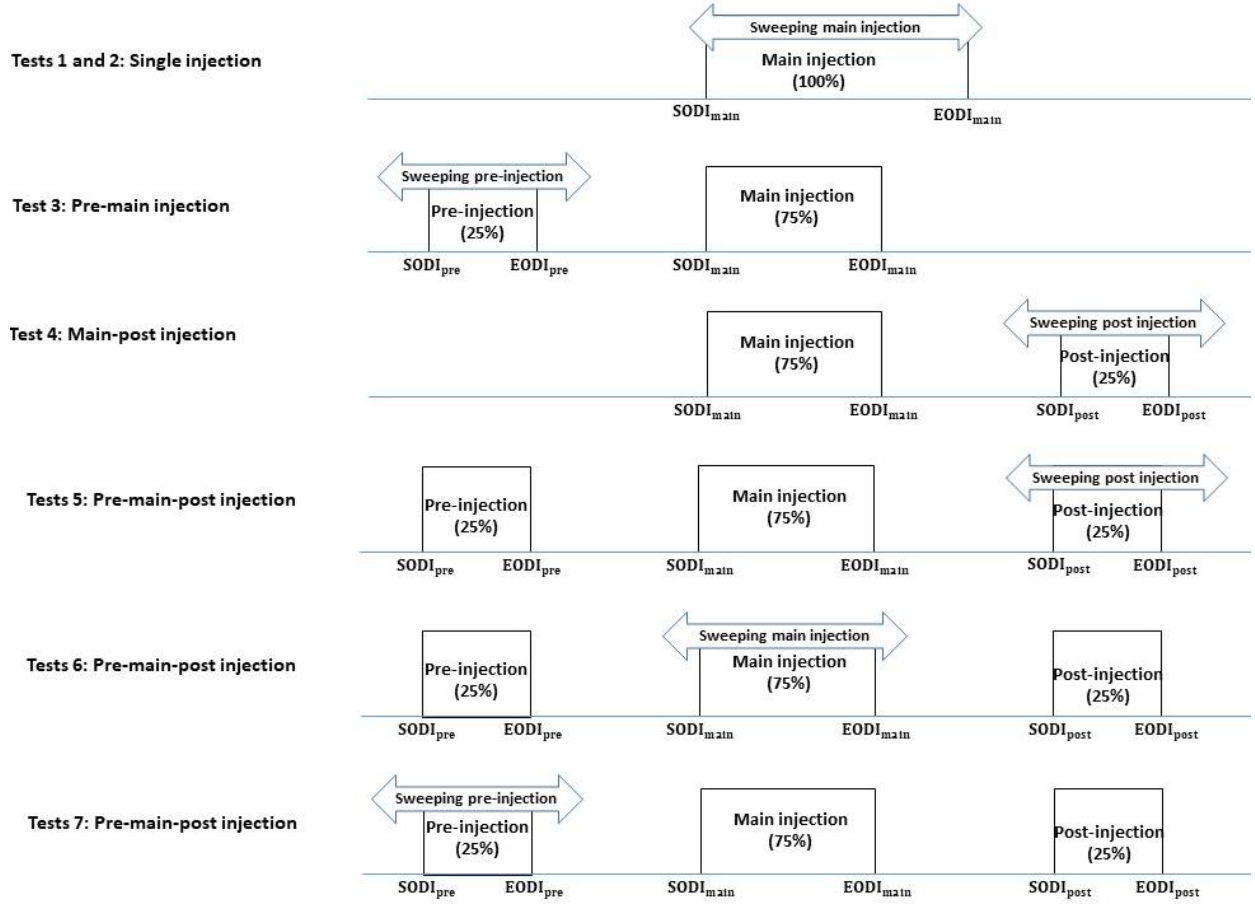
$$\%PWR = \frac{PW_{D-pre,main,or\ post}}{PW_{D-total}} \quad (1)$$

162 The experiments started with a sweep of start of diesel injection (SODI) timing for diesel engine mode with single  
 163 diesel injection strategy (Test 1) in order to provide the baseline data for a comparative study. Then the engine was  
 164 switched to dual-fuel mode with 50% natural gas energy fraction under same engine load and speed conditions (i.e.,  
 165 BMEP = 12.15 bar and rpm = 910), and Test 2 started to investigate the effect of single diesel injection timing on the  
 166 NDDF engine performance. In order to do a comparison study, two diesel injection strategies of pre-main and main-  
 167 post were also examined in Tests 3 and 4, respectively. The diesel injection timing of the Tests 3 and 4 was optimized  
 168 to achieve the highest thermal efficiency and lowest GHG emissions. Our previous study found that operating a NDDF  
 169 engine with pre-main-post diesel injection strategy has the potential to further decrease the unburned methane  
 170 emissions under high load conditions [10]. However, the trade-off is lower indicated thermal efficiency (ITE) and  
 171 higher GHG emissions compared to that of single diesel injection strategy. In this paper, further effort is made to  
 172 improve the thermal efficiency and GHG emissions of the NDDF engine with pre-main-post diesel injection strategy  
 173 while reducing unburned methane and NO<sub>x</sub> emissions compared to those with single diesel injection strategy.  
 174 Therefore, in Tests 5 to 7, the effect of pre-main-post diesel injection strategy on the NDDF engine was investigated.  
 175 In Test 5, a sweep of post diesel injection timing was conducted while the pre and main diesel injection timings were  
 176 fixed at -50 and -8 °ATDC, respectively. In Test 6, pre and post diesel injection timings were fixed at -50 and +30  
 177 °ATDC, respectively, while a sweep of the main diesel injection timing was conducted. In Tests 7, a sweep of the pre  
 178 diesel injection timing was carried out while the main and post diesel injection timings were fixed at -8 and +14  
 179 °ATDC, respectively.

**Table 3:** Diesel injection strategies.

Operating mode (injection strategy)	Diesel (kg/h)	NG (kg/h)	SODI <sub>pre</sub> (°ATDC)	EODI <sub>pre</sub> (°ATDC)	SODI <sub>main</sub> (°ATDC)	EODI <sub>main</sub> (°ATDC)	SODI <sub>post</sub> (°ATDC)	EODI <sub>post</sub> (°ATDC)	%PWR (pre/main/ post %)
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<b>Test 1</b>	Diesel (Single)		4.619			-14	+7.94				
			4.625			-16	+5.71				
			4.625			-18	+3.60				
			4.649	-	-	-20	+2.80	-	-		
			4.731			-22	+1.34				
			4.759			-24	-2.72				
			4.842			-25	-3.72				
<b>Test 2</b>	Dual-fuel (Single)		2.311	2.087			-12	+0.90			
			2.279	2.061			-14	-1.27			
			2.257	2.035	-		-16	-3.33	-	-	
			2.701	2.027			-17	-4.22			
			2.264	2.026			-17.5	-4.76			
<b>Test 3</b>	Dual-fuel (Pre-main with varying pre injection timing)		2.307	2.063	-26	-21.97	-12	+0.07			
			2.298	2.054	-30	-25.95	-12	+0.14			
			2.310	2.065	-34	-29.95	-12	+0.14			
			2.299	2.064	-38	-33.90	-12	+0.29	-	25/75	
			2.297	2.058	-42	-37.85	-12	+0.43			
			2.285	2.053	-46	-41.86	-12	+0.41			
			2.283	2.041	-50	-45.88	-12	+0.33			
<b>Test 4</b>	Dual-fuel (Main-post with varying post injection timing)		2.327	2.103			-12	+0.37	+10	+14.12	
			2.343	2.100			-12	+0.40	+14	+18.13	
			2.351	2.114			-12	+0.30	+18	+22.10	
			2.354	2.113			-12	+0.34	+22	+26.11	
			2.376	2.114	-		-12	+0.68	+26	+30.22	75/25
			2.352	2.117			-12	+0.71	+30	+34.23	
			2.375	2.119			-12	+0.58	+34	+38.19	
<b>Test 5</b>	Dual-fuel (Pre-main-post 1 with varying post injection timing)		2.380	2.126			-12	+0.61	+40	+44.20	
			2.322	2.076	-50	-44.91	-8	+2.17	+6	+11.08	
			2.358	2.085	-50	-44.79	-8	+2.41	+10	+15.20	
			2.365	2.131	-50	-44.73	-8	+2.53	+14	+19.26	
			2.405	2.151	-50	-44.74	-8	+2.51	+18	+23.25	25/50/25
			2.381	2.153	-50	-44.67	-8	+2.64	+22	+27.32	
			2.451	2.171	-50	-44.50	-8	+2.99	+26	+31.49	
<b>Test 6</b>	Dual-fuel (Pre-main-post 2 with varying main injection timing)		2.516	2.231	-50	-44.41	-8	+3.16	+30	+35.58	
			2.540	2.252	-50	-44.37	-8	+3.24	+40	+45.62	
			2.427	2.196	-50	-44.43	-10	+1.13	+30	+35.56	
			2.474	2.220	-50	-44.44	-8	+3.10	+30	+35.55	25/50/25
<b>Test 7</b>	Dual-fuel (Pre-main-post 3 with varying pre injection timing)		2.471	2.215	-50	-44.49	-6	+5.00	+30	+35.50	
			2.546	2.272	-50	-44.46	-4	+7.06	+30	+35.53	
			2.321	2.101	-50	-44.76	-8	+2.46	+14	+19.23	
			2.307	2.053	-54	-48.76	-8	+2.47	+14	+19.23	
			2.298	2.052	-58	-52.81	-8	+2.37	+14	+19.18	
			2.275	2.061	-62	-56.83	-8	+2.33	+14	+19.16	25/50/25
			2.293	2.045	-66	-60.86	-8	+2.27	+14	+19.13	
<b>Test 7</b>	Dual-fuel (Pre-main-post 3 with varying pre injection timing)		2.281	2.044	-70	-64.88	-8	+2.22	+14	+19.11	
			2.286	2.036	-75	-69.83	-8	+2.32	+14	+19.16	
			2.272	2.039	-80	-74.87	-8	+2.35	+14	+19.12	



**Fig. 2:** Schematic of diesel injection strategies.

181

182 **2.4. Combustion characteristic metrics**

183 For each test point, the cylinder pressure data was used to calculate the net heat release rate (HRR) based on the  
 184 first law of thermodynamics using Eq. (2), where  $\gamma$  is the specific heat ratio,  $P$  is the cylinder pressure,  $V$  is the cylinder  
 185 volume, and  $\theta$  is the engine crank angle.

$$\text{HRR} = \frac{\gamma}{\gamma - 1} P \frac{dV}{d\theta} + \frac{1}{\gamma - 1} V \frac{dP}{d\theta} \quad (2)$$

186 Indicated thermal efficiency (ITE) was calculated using Eq. (3) where  $P_{\text{ind}}$  is indicated power,  $\dot{m}_{\text{NG}}$  and  $\dot{m}_{\text{D}}$  are the  
 187 mass flow rate of natural gas and diesel, respectively, and  $\text{LHV}_{\text{NG}}$  and  $\text{LHV}_{\text{D}}$  are the lower heating value of natural  
 188 gas and diesel, respectively.

$$ITE = \frac{P_{ind}}{\dot{m}_D \times LHV_D + \dot{m}_{NG} \times LHV_{NG}} \quad (3)$$

189 The natural gas energy fraction (%NG), Eq. 4, is defined as the fraction of energy from natural gas in the total  
 190 energy input to the engine.

$$\%NG = \frac{\dot{m}_{NG} \times LHV_{NG}}{\dot{m}_D \times LHV_D + \dot{m}_{NG} \times LHV_{NG}} \quad (4)$$

191 Combustion phasing (i.e., CA50) is determined as the crank angle where 50% of the total heat energy from the  
 192 fuel is released. The zero-crossing point of heat release curve when heat release rate starts to increase is defined as  
 193 start of combustion (SOC). The pressure rise rate is calculated from the pressure profiles using Eq. (5), where P  
 194 represents the discrete pressure signal and  $\Delta\theta$  is 0.2 CAD since the cylinder pressure data is collected at an interval  
 195 of 0.2 CAD.

$$\left(\frac{dP}{d\theta}\right)_i = \frac{P_{i+1} - P_i}{\Delta\theta} \quad (5)$$

### 196 3. Numerical approach

197 A three-dimensional CFD simulation was conducted using a commercial software, CONVERGE (version 3.0) [41],  
 198 to understand the mechanisms of the experimental observations. The details of numerical modeling can be found  
 199 in our previous studies [10,36,42–44] and a brief summary of the numerical method and important models are  
 200 presented in this section. The conservation equations of mass, momentum, species, and energy were discretized by  
 201 a second-order scheme in space and a first-order scheme in time. The CFD code calculated the transport equations  
 202 and a transient chemistry solver, SAGE [41], calculated the reaction rate of each elementary reaction. Diesel and  
 203 natural gas were represented by n-heptane and methane, respectively, using a reduced reaction mechanism  
 204 consisting of 76 species and 464 reactions [45]. An Eulerian-Lagrangian Discrete Droplet Model (DDM) was used to  
 205 model the spray [41]. The Kelvin-Helmholtz Rayleigh-Taylor (KH-RT) model was adopted to model diesel droplet  
 206 atomization and breakup [46]. The collision of diesel spray droplets was simulated by O'Rourke model [47]. Adaptive  
 207 mesh refinement (AMR) was used to efficiently resolve details in the regions of the higher species concentration

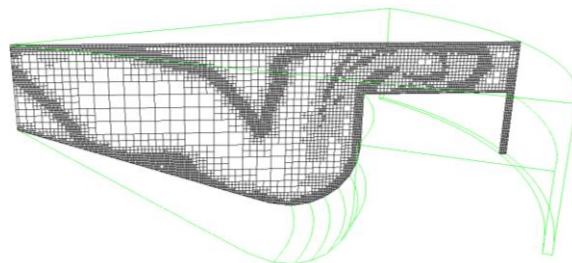
208 gradients and the turbulent flame front [41]. The maximum size of computational cell was set at 2.0 mm. However,  
209 a very fine grid resolution was needed to capture the subgrid-scale effects on flame propagation. AMR allowed the  
210 automatic reduction of the computational cell size to 0.25 mm in order to capture the turbulent flame front (Fig. 3).

211 A closed cycle simulation from intake valve closing (IVC) to exhaust valve opening (EVO) was carried out in this  
212 study. As shown in Table 1, since the diesel injector had six equally spaced nozzle's orifices, a 1/6th section of the  
213 combustion chamber was simulated as a representative volume of the entire chamber. Premixed natural gas – air  
214 mixture was assumed to be homogeneous at the beginning of the simulation since a port fuel injection of natural  
215 gas was used in the experiments. The cylinder charge temperature at the start of simulation was calculated by 1-D  
216 simulation in GT-POWER. This temperature was kept at 360 K for all simulated cases since the engine load and speed  
217 were maintained at BMEP = 12.15 bar and rpm = 910, respectively, during the experiments. As mentioned in section  
218 2.3, the intake manifold pressure was maintained at 1.80 bar in all tests. However, in order to reproduce the trapped  
219 mass and experimental cylinder pressure during the compression stroke the cylinder charge pressure at the start of  
220 simulation was slightly adjusted ( $1.80 \pm 0.02$  bar).

221 According to the study of Wijeyakulasuriya et al. [48], the combustion process and emissions become very  
222 sensitive to wall boundary temperatures when the combustion starts from the outer periphery or near the liner and  
223 then propagates inward. Therefore, estimation of wall boundary temperature is a crucial part of this simulation  
224 study, especially for pre-main and pre-main-post diesel injection strategies where part of the diesel fuel is injected  
225 at a very advanced timing during the compression stroke and the combustion starts from near the cylinder liner and  
226 piston squish regions. The detailed explanation of boundary temperature estimation was presented in our recent  
227 study [10] and a brief description is given in this section. It was shown in our previous study [10] that post-injection  
228 strategies increase the exhaust gas temperature since part of diesel fuel is burnt very late in the expansion stroke.  
229 This increases the subsequent cycle boundary wall temperatures due to the high temperature of residual gas in the  
230 combustion chamber. To take this into account in the closed cycle simulation and to precisely predict the initial wall  
231 boundary temperature, three consecutive closed cycle simulations were performed for each case. After completion  
232 of the first simulation, the average charge temperatures near the wall were calculated and applied for the second  
233 simulation, and those from the second simulation were applied to the third simulation. Finally, an appropriate value

234 of boundary temperature was established by comparing the predicted start of combustion, EVO temperature, and  
235 unburned methane emissions with their experimental counterparts [10].

236 In order to verify the reliability of the developed CFD model, four different diesel injection strategies (i.e., single,  
237 pre-main, main-post, and pre-main-post) are selected to compare the measured and calculated cylinder pressure  
238 and heat release rate of the NDDF engine. As shown in Fig. 4, the calculated cylinder pressure and heat release rate  
239 are in good agreement with the experimental results, suggesting that the combustion process is well reproduced by  
240 the CFD model. The calculated results of thermal efficiency, combustion phasing, start of combustion, PPRR, and  
241 unburned methane, NO<sub>x</sub>, and GHG emissions of some selected cases of pre-main-post diesel injection strategy will  
242 be presented and compared with experimental results in section 4. More validation of single, pre-main, and main-  
243 post diesel injection strategies can be also found in our previous study [10]. It is noted that the ISCH<sub>4</sub> and ISCO<sub>2</sub>  
244 emissions were under-predicted (Figs. 9a and b). This is mainly due to [the use of reduced methane/n-heptane](#)  
245 [chemical mechanism in CFD simulations. Moreover, there is a discrepancy between calculated and measured](#)  
246 [thermal efficiency as shown in Fig. 9c. The calculated cylinder pressure is higher than measured one during the](#)  
247 [expansion stroke \(Fig. 4\) which leads to over-prediction in thermal efficiency. This could be due to the deficiencies](#)  
248 [in adopted wall heat transfer model and the assumption of constant boundary wall temperature.](#)



249 **Fig. 3:** Adaptive mesh refinement in flame front during the flame propagation stage.

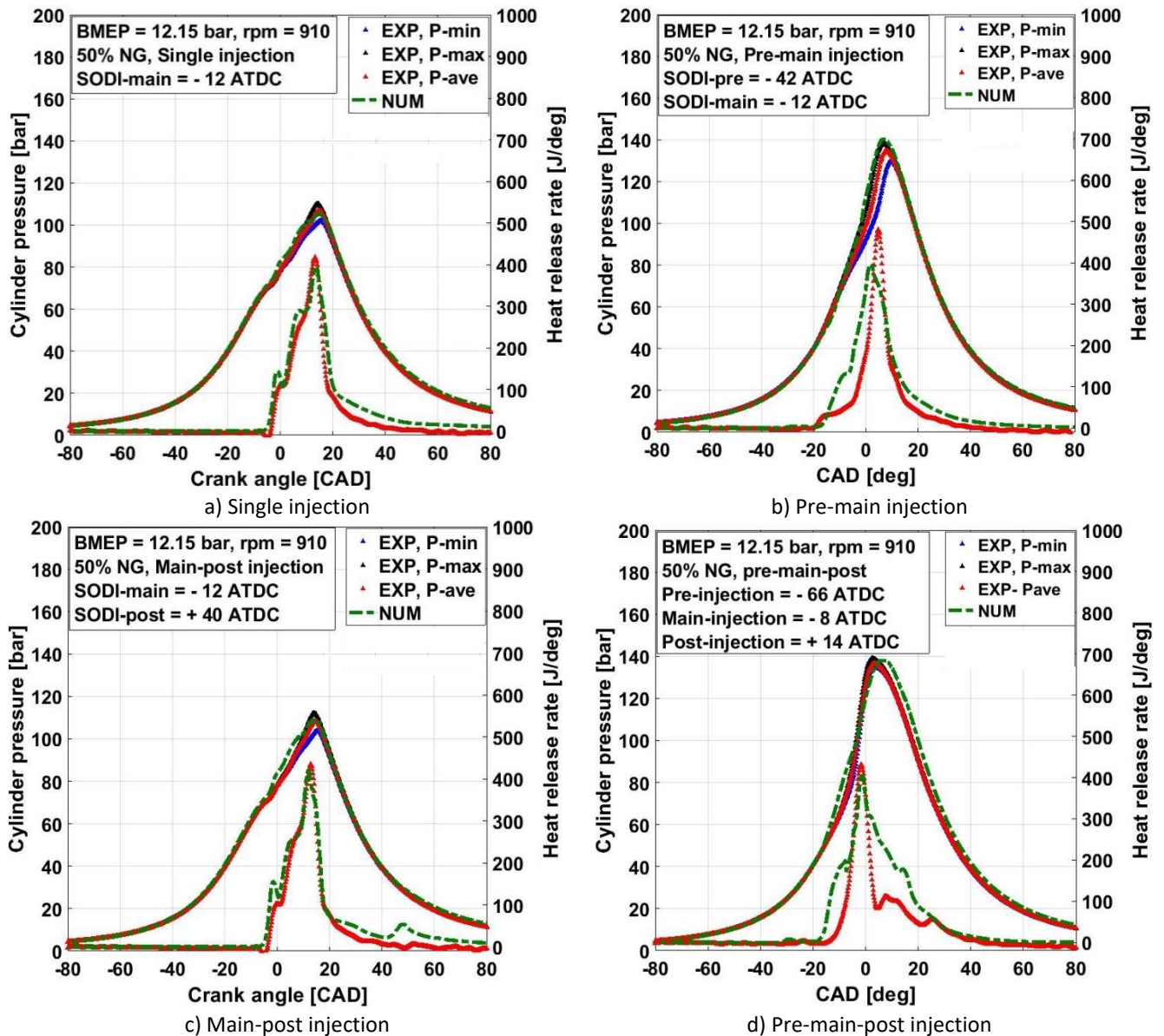


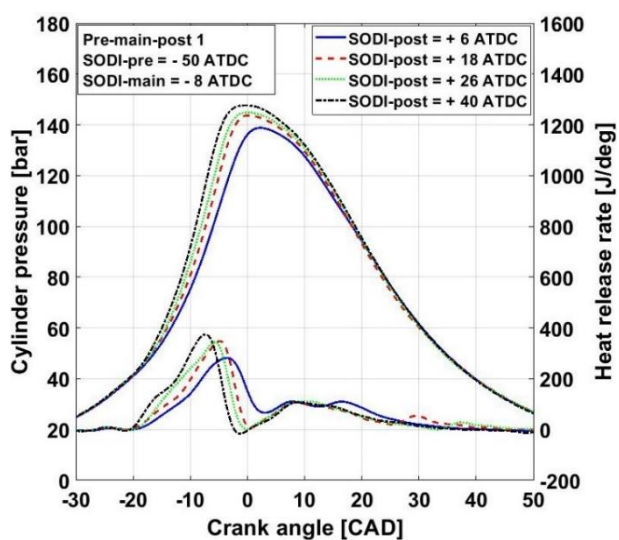
Fig. 4: Measured and calculated cylinder pressure and HRR of single, pre-main, main-post, and pre-main-post diesel injection strategies.

#### 250 4. Results and discussion

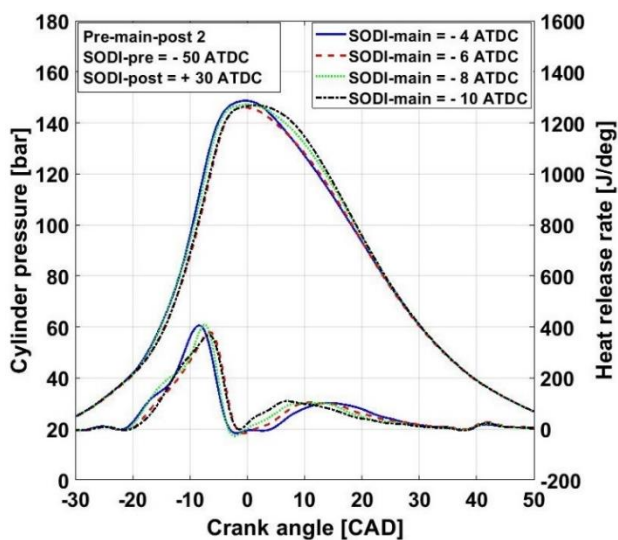
251 In this section, the effect of pre-main-post diesel injection strategies on combustion characteristics (i.e., cylinder  
 252 pressure, HRR, exhaust temperature, start of combustion (SOC), combustion phasing, PPRR, and thermal efficiency)  
 253 and emissions (i.e., CH<sub>4</sub>, NO<sub>x</sub>, and GHG) of the NDDF engine is investigated at 50% natural gas energy fraction. The  
 254 experimental results of pre-main-post injection strategy are also compared with single, pre-main, and main-post  
 255 diesel injection strategies. The focus is on the optimization of combustion phasing and thermal efficiency of pre-

256 main-post injection strategy while maintaining its lower unburned methane emissions compared to single diesel  
 257 injection strategy. Numerical simulation results are presented for selected cases in order to improve the  
 258 understanding of the fundamental mechanisms observed in the experiments.

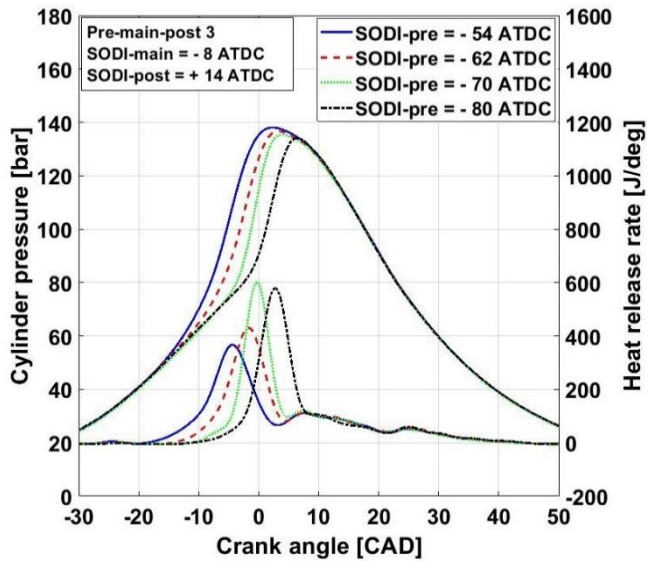
259 Figures 5a, b, and c show the effects of post, main, and pre diesel injection timings, respectively, on cylinder  
 260 pressure and HRR of the investigated NDDF engine with pre-main-post diesel injection strategy. Only the effect of  
 261 selected diesel injection timings on cylinder pressure and HRR is displayed in these figures. The effects of single, pre-  
 262 main, and main-post diesel injection strategies on cylinder pressure and HRR of the NDDF engine have been  
 263 investigated and discussed in our previous study [10], and therefore are not shown in this section. Figure 6 displays  
 264 the effect of pre, main, and post diesel injection timings on exhaust temperature and SOC for various injection  
 265 strategies. It can be seen from Figs. 5 and 6b that the SOC occurs before the main diesel injection timing for all  
 266 examined pre-main-post diesel injection strategies, implying that the premixed mixture of pre-injected diesel and  
 267 natural gas – air is ignited before the main diesel injection timing. This is also confirmed by Hydroxyl (OH) radical  
 268 distribution contours for a selected case of SODI-pre, main, and post = - 62, - 8, and +14 °ATDC, respectively, in Fig.  
 269 7. It is observed that the OH radical initially appears in the piston squish area at an engine crank angle of -15.69  
 270 °ATDC that is 7.69 °CAD before the main diesel injection timing (SODI-main = - 8 °ATDC). The second zone of OH  
 271 radical is also detected two crank angle degree later in the piston crevice region. At an engine crank angle of CAD =  
 272 -10.69 °ATDC, the two flame kernels merge and propagate towards the cylinder center.



a) Pre-main-post 1 (sweeping post injection timing, Test 5)



b) Pre-main-post 2 (sweeping main injection timing, Test 6)



c) Pre-main-post 3 (sweeping pre injection timing Test 7)

Fig. 5: Measured cylinder pressure and HRR of NDDF engine with different pre-main-post diesel injection strategies.

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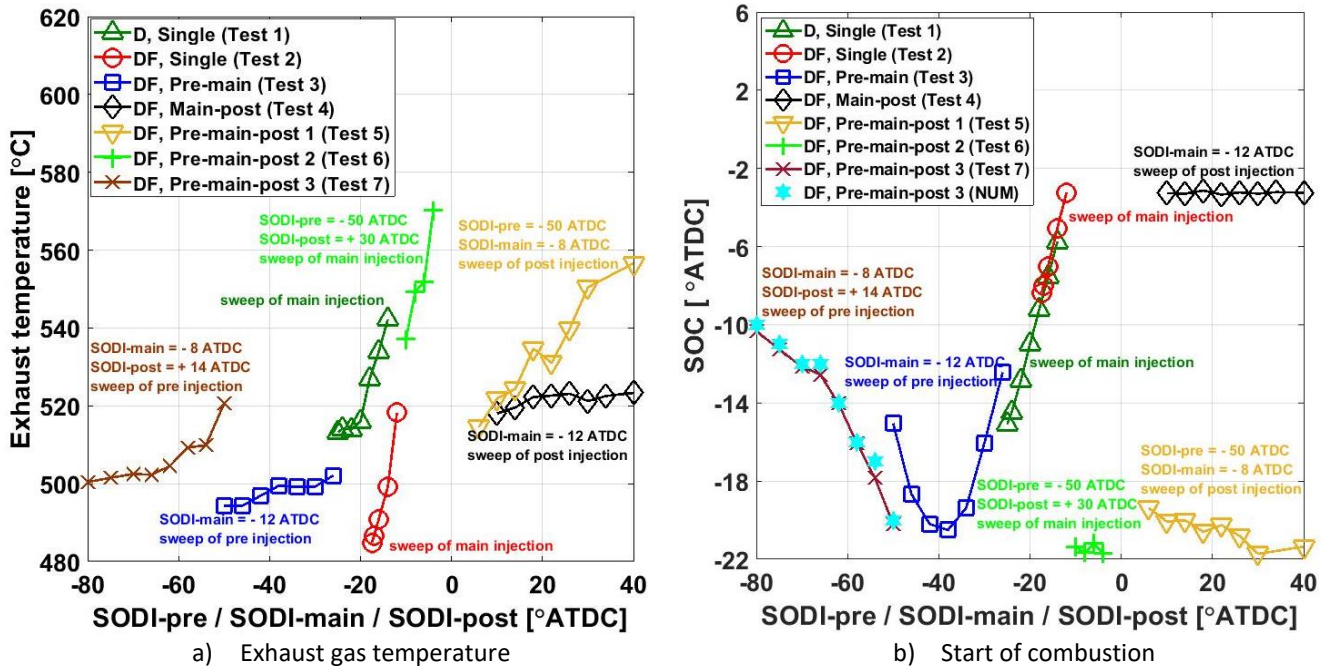


Fig. 6: Exhaust gas temperature and SOC of NDDF engine with different diesel injection strategies.

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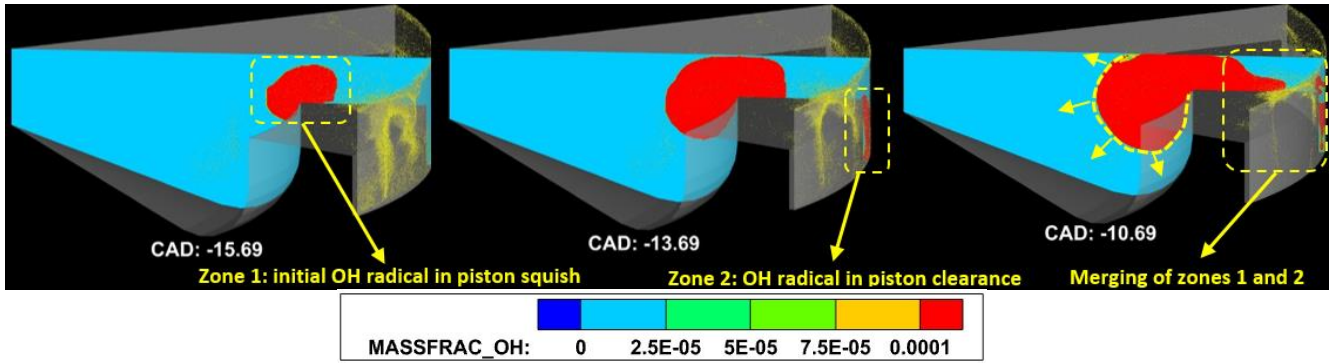


Fig. 7: OH radical distribution of NDDF engine with pre-main-post diesel injection strategy with SODI-pre, main, and post = - 62, - 8, and + 14 °ATDC at 50% natural gas energy fraction.

275 As shown in Figs. 5a and 6b (Test 5), retarding post diesel injection timing advances the start of combustion of  
 276 the NDDF engine with pre-main-post diesel injection strategy. This is mainly due to the exhaust gas temperature  
 277 increase with retarding post diesel injection timing, as shown in Fig. 6a, which increases the wall and cylinder charge  
 278 temperature of the subsequent cycle and thus advances the SOC. As shown in Figs. 6a and b, for Test 5, retarding  
 279 post diesel injection timing from +6 to +40 °ATDC increases the exhaust gas temperature from 514.53 to 556.62 °C  
 280 and advances the start of combustion from -19.3 to -21.2 °ATDC. The reason behind this phenomenon was explained  
 281 in our previous study along with cylinder charge temperature and local equivalence ratio contours [10]. Due to the  
 282 same reasons, retarding main diesel injection timing (Test 6) also advances the SOC.

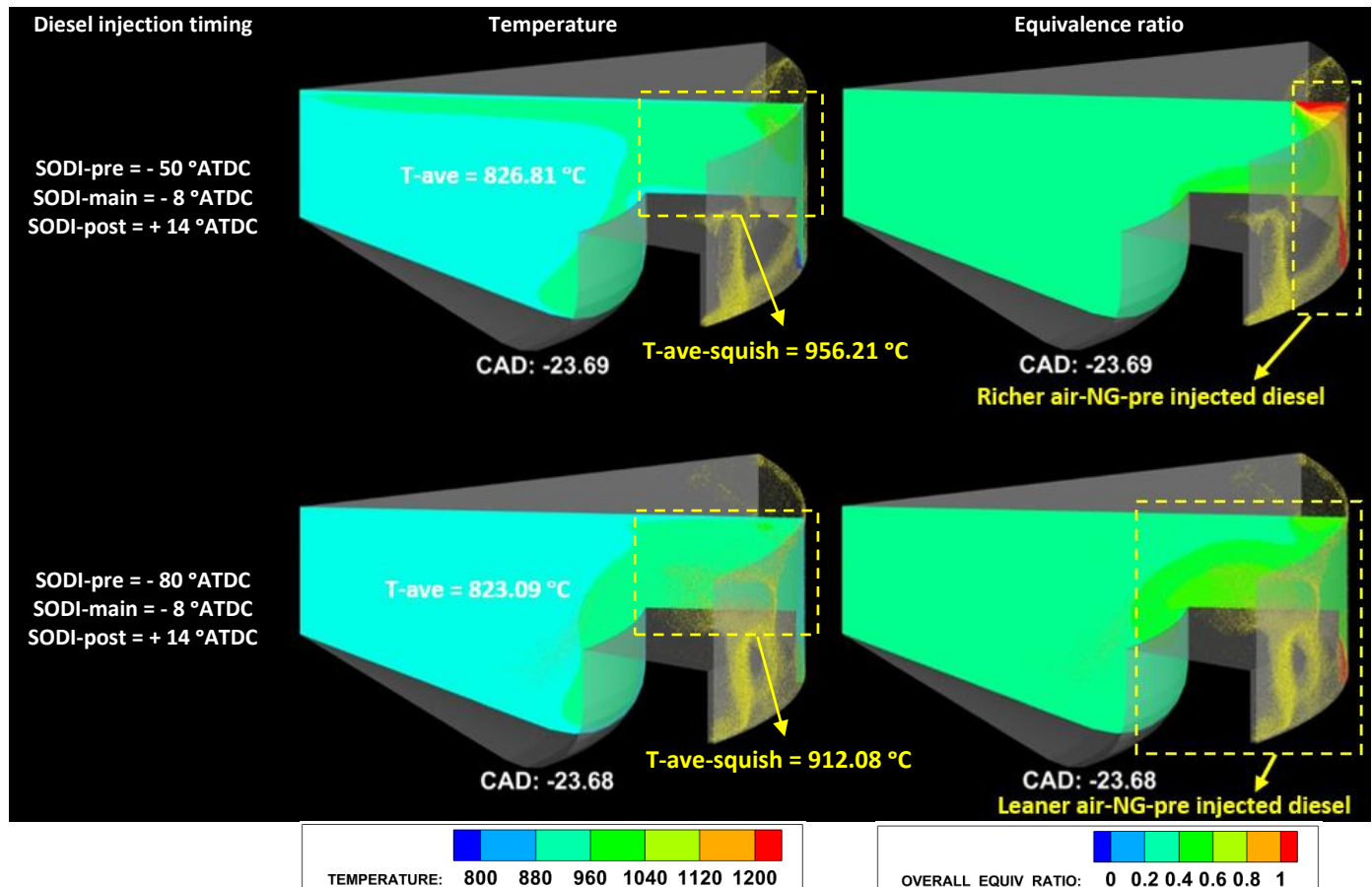
283 As mentioned above, the start of combustion occurs before the main diesel injection timing for all pre-main-post  
 284 diesel injection strategies (see Fig. 6b, Tests 5 and 6). This suggests that the cylinder charge temperature and the  
 285 timing of pre injected diesel affect the stratification of pre-injected diesel and natural gas – air mixture and control  
 286 the start of combustion. In order to prove this, the effect of sweeping pre diesel injection timing on cylinder pressure  
 287 and HRR of the NDDF engine is examined in Fig. 5c (Test 7). It is observed that sweeping pre diesel injection timing  
 288 has more significant effect on SOC compared to sweeping main and post diesel injection timings (Tests 5 and 6, Figs.  
 289 5a and b). This is more clearly shown in Fig. 6b. Similar to sweeping main and post diesel injection timing (Tests 5  
 290 and 6), retarding the pre diesel injection timing also increases the exhaust gas temperature (Fig. 6a). The change in  
 291 the pre diesel injection timing modifies the stratification of pre injected diesel and natural gas – air mixtures and  
 292 therefore the local equivalence ratio inside the combustion chamber before start of combustion. To further elucidate  
 293 this, the cylinder charge temperature and local equivalence ratio contours with two different pre diesel injection

294 timings of -80 and -50 °ATDC and fixed main and post diesel injection timings are shown in Fig. 8. It is noted that the  
295 frame contours in Fig. 8 were selected at an engine crank angle before the start of combustion (i.e., CAD = - 23 .68  
296 °ATDC) to compare the cylinder charge temperature and the local equivalence ratio. It can be seen that the average  
297 charge temperature in piston squish regions for the pre-main-post injection strategy with pre diesel injection timing  
298 of -50 °ATDC ( $T_{\text{ave-squish}} = 956.21 \text{ }^{\circ}\text{C}$ ) is higher than that of -80 °ATDC ( $T_{\text{ave-squish}} = 912.08 \text{ }^{\circ}\text{C}$ ). This is due to the  
299 higher exhaust gas temperature with pre diesel injection timing of -50 °ATDC, which increases the wall and cylinder  
300 charge temperature of the subsequent cycle. Moreover, the local equivalence ratio contours show that the pre  
301 injected diesel for both pre injection timings of -50 and -80 °ATDC targets the piston squish and crevice regions.  
302 However, retarded pre diesel injection timing of -50 °ATDC provides a higher local equivalence ratio regions in the  
303 piston squish and crevice regions (Fig. 8). Therefore, the higher cylinder charge temperature at piston squish regions  
304 along with higher local equivalence ratio of diesel injection strategy with pre diesel injection timing of -50 °ATDC  
305 results in more advanced SOC compared to that of -80 °ATDC.

306 From the above discussion, it can be inferred that two parameters affect the SOC when retarding the pre diesel  
307 injection timing in pre-main-post injection 3 test. The first one is the thermal effect of exhaust temperature when  
308 retarding diesel injection timing, which is also found in pre-main-post 1 and 2 tests where the SOC also slightly  
309 advances (in the range of 1 to 2 CAD) when retarding post and main diesel injection timings. The second one is fuel  
310 stratification of natural gas – air – pre injected diesel and it seems more significant than the thermal effect. This is  
311 because retarding pre diesel injection timing increases the exhaust temperature by only 20 °C that is even smaller  
312 than the exhaust temperature increase in pre-main-post 1 and 2 tests (in the range of 30 to 40 °C) when retarding  
313 post and main diesel injection timings. Therefore, it is concluded that the thermal effect of retarding pre diesel  
314 injection timing could advance the SOC by 1 to 2 CAD, but the SOC advancement may be mainly a result of the fuel  
315 stratification effect of the premixed mixture of pre injected diesel and natural gas – air.

316 As mentioned above, the goal of this paper is to retard the combustion phasing (or SOC) of the NDDF engine with  
317 pre-main-post diesel injection strategy to a more optimized crank angle. Sweeping pre-diesel injection timing gives  
318 more controllability of combustion phasing (start of combustion) than sweeping main and post diesel injection  
319 timings. It is found that a stratified premixed mixture of pre injected diesel – natural gas – air (e.g. SODI-pre = -50

320 °ATDC) leads to overly advanced combustion phasing (or start of combustion) which decreases the thermal efficiency  
 321 of the NDDF engine with pre-main-post diesel injection strategy. However, a more homogenous premixed mixture  
 322 of pre injected diesel – natural gas – air (e.g. SODI-pre = -80 °ATDC) retards the combustion phasing and improves  
 323 the thermal efficiency of the NDDF engine. More details will be discussed in Figs. 9c and d.



**Fig. 8:** Cylinder temperature and local equivalence ratio contours of NDDF engine with two different pre diesel injection timing of -80 and -50 °ATDC and fixed main and post injection timings at SOC.

324 Figures 9a-d display the CO<sub>2</sub> equivalent (or GHG) and unburned methane emissions, indicated thermal efficiency  
 325 (ITE), and combustion phasing for different diesel injection strategies at 50% natural gas energy fraction. The results  
 326 of Test 6 (pre-main-post 2) are not shown here since sweeping main diesel injection timing of pre-main-post injection  
 327 strategy has little effect on the results. In this study, the equivalent CO<sub>2</sub> emission is calculated using Eq. (6) according  
 328 to EPA’s GHG emissions-Phase (II) [39].

$$\text{Equivalent ISCO}_2 = \text{ISCO}_2 + 34 \times \text{ISCH}_4 \quad (6)$$

329 It is observed from Figs. 9a and c (Test 1) that the diesel engine mode with single injection achieves the lowest  
330 GHG emissions of 650.11 g/kW.h and the highest ITE of 40.48% at the diesel injection timing of -22 °ATDC. The NDDF  
331 engine mode with single diesel injection strategy (Test 2) obtains higher ITE and emits lower GHG emissions  
332 compared to its counterpart diesel engine mode. As shown in Figs. 9a and c, advancing single diesel injection timing  
333 from -12 to -16 °ATDC improves both GHG emissions and ITE of the NDDF engine. The lowest GHG emissions and  
334 highest ITE are 609.77 g/kW.h and 40.72%, respectively, which occur at the single diesel injection timing of -16 °ATDC  
335 (Test 2). It is noted that the unburned methane emissions monotonically increase with advancing the single diesel  
336 injection timing, since the increase in cylinder pressure causes more natural gas-air mixture to be trapped in the  
337 crevice and boundary zones [42]. Therefore, the decrease of GHG emissions with advancing of the single diesel  
338 injection timing from -12 to -16 °ATDC is due to the improvement in ITE. The emitted unburned methane emissions  
339 at the optimum point of ITE and GHG emissions is 1.12 g/kW.h. Further advancing diesel injection timing to -17.5  
340 °ATDC increases the GHG emissions and decreases the ITE. These are due to the increase of unburned methane  
341 emissions (Fig. 9b) and overly advanced combustion phasing (Fig. 9d).

342 Advancing pre diesel injection timing improves both GHG emissions and ITE of the NDDF engine with pre-main  
343 diesel injection strategy (Test 3), as shown in Figs. 9a and c. However, advancing pre diesel injection timing increases  
344 the unburned methane emissions of the NDDF engine using pre-main diesel injection strategy (Test 3). The lowest  
345 GHG emissions of 617.94 g/kW.h and the highest thermal efficiency of 40.4% of the NDDF engine with pre-main  
346 diesel injection strategy are obtained at the pre diesel injection timing of -50 °ATDC. The emitted unburned methane  
347 emissions at the optimum point of GHG emissions in the pre-main injection strategy is 1.25 g/kW.h, which is higher  
348 than that of the single diesel injection strategy.

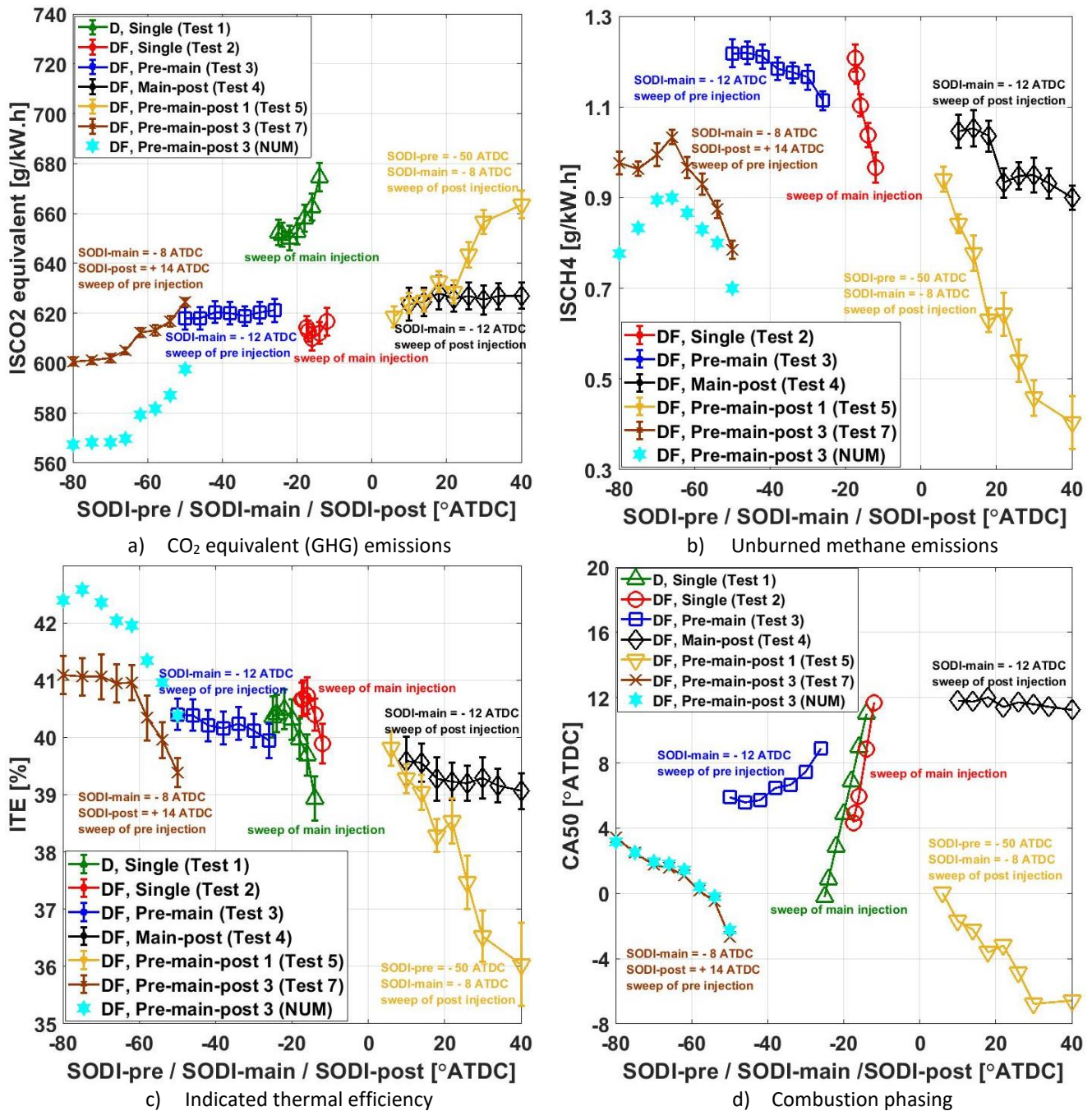


Fig. 9: GHG and unburned methane emissions, ITE, and combustion phasing of NDDF engine with different diesel injection strategies.

349 It can be observed from Fig. 9b that retarding the post diesel injection timing decreases the unburned methane  
 350 emissions of the NDDF engine with both main-post (Test 4) and pre-main-post 1 (Test 5). The reduction is more  
 351 significant when using pre-main-post. This is because pre diesel injection burns most of the trapped unburned  
 352 methane in the crevice regions at the beginning of the combustion, and post diesel injection increases the cylinder  
 353 charge temperature in the late expansion stroke and pushes the remaining unburned gas in the crevice regions into

354 the second-stage of combustion [10]. However, as shown in Fig. 9a, retarding post diesel injection timing increases  
355 the GHG emissions of the NDDF engine, especially for the pre-main-post 1 test (Test 5). This is mainly caused by the  
356 overly advanced combustion phasing (Fig. 9d), which subsequently causes deterioration in thermal efficiency (Fig.  
357 9c) as post diesel injection timing is retarded. Therefore, if the combustion phasing of the NDDF engine can be  
358 retarded while maintaining the low unburned methane emissions feature of the pre-main-post diesel injection  
359 strategy, it may be possible to further reduce GHG emissions. To reach this goal, the pre-diesel injection timing is  
360 further advanced in the pre-main-post 3 test (Test 7) compared to that in pre-main-post injection 1 test (Test 5). It  
361 is observed from Fig. 9d that the combustion phasing is retarded, and therefore ITE and GHG emissions are further  
362 improved as the pre-diesel injection timing is advanced in the pre-main-post diesel injection strategy (Test 7). The  
363 lowest GHG emissions and the highest thermal efficiency of the NDDF engine in pre-main-post 3 test are 600.68  
364 g/kW.h and 41.09%, respectively, which are achieved at an advanced pre-diesel injection timing of -80 °ATDC.  
365 Moreover, the emitted unburned methane emissions at this optimum point of GHG emissions is 0.97 g/kW.h. This  
366 is about 13.4% reduction in unburned methane emissions compared to optimum point of the single diesel injection  
367 strategy.

368 Figure 10 shows the effect of different diesel injection strategies on PPRR of the NDDF engine at 50% natural gas  
369 energy fraction. It can be observed that advancing diesel injection timing significantly increases the PPRR of the  
370 NDDF engine with single diesel injection strategy (Test 2), in which the PPRR reaches 10.88 bar/CAD at the optimum  
371 point of GHG emissions (i.e., SODI = -16 °ATDC). Double and triple diesel injection strategies allow wider ranges of  
372 diesel injection timing while keeping the maximum PPRR well below the engine limit. For example, advancing pre-  
373 diesel injection timing in pre-main-post 3 test (Test 7) from -50 to -70 °ATDC increases the maximum PPRR of the  
374 NDDF engine from 8.37 to 10.31 bar/CAD, but the PPRR starts to decrease with further advancement of the pre-  
375 diesel injection timing. The PPRR of 9.11 bar/CAD is achieved at the optimum point of GHG emissions of the NDDF  
376 engine with pre-main-post 3 test (i.e., SODI-pre = -80 °ATDC). This is about 16.2% reduction of PPRR compared to  
377 the optimum point of single diesel injection strategy.

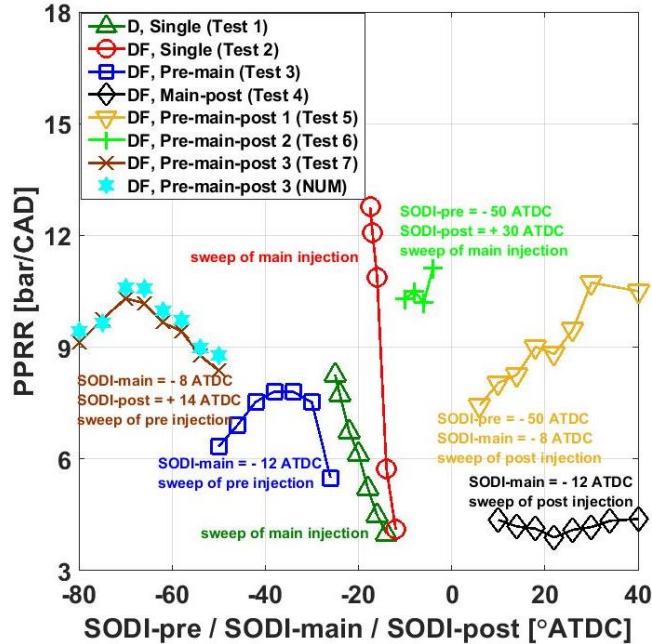


Fig. 10: Peak pressure rise rate of NDDF engine with different diesel injection strategies at 50% natural gas energy fraction.

378 Figure 11 displays the effect of different diesel injection strategies on NO<sub>x</sub> emissions and NO<sub>x</sub> – GHG trade off of  
 379 the NDDF engine at 50% natural gas energy fraction. The results of diesel engine mode with single diesel injection  
 380 strategy are also added for the sake of comparison. It can be observed from Fig. 11a that the NDDF engine with  
 381 single diesel injection strategy (Test 2) produces higher NO<sub>x</sub> emissions compared to that of diesel engine mode (Test  
 382 1) at similar single diesel injection timing. This is mainly because of the faster burning rate of natural gas – air – diesel  
 383 mixtures in NDDF engine mode than that of air – diesel mixtures in diesel engine mode once it is being ignited. This  
 384 faster burning rate advances the SOC (Fig. 6b) and CA50 (Fig. 9d) and increases the combustion temperature and  
 385 therefore the NO<sub>x</sub> emissions of the NDDF engine mode compared to the diesel engine mode. However, the emitted  
 386 NO<sub>x</sub> emission of the diesel engine mode at the optimum point of GHG emissions (Fig. 11b, SODI = -22 ATDC, Test 1)  
 387 is 9.21 g/kW.h, while this value is 6.93 g/kW.h for the NDDF engine with single diesel injection strategy (Fig. 11b,  
 388 SODI = -16 °ATDC, Test 2).

389 The injection of part of diesel before the main injection timing in pre-main injection strategy (Test 3) decreases  
 390 the NO<sub>x</sub> emissions of the NDDF engine compared to that at the optimum GHG point of single diesel injection strategy.  
 391 The NDDF engine with pre-main diesel injection strategy produces 5.78 g/kW.h NO<sub>x</sub> emissions at the optimum point

392 of GHG emissions (Fig. 11b, SODI-pre = -50 °ATDC, Test 3). However, as shown in Fig. 11b, the value of GHG emissions  
 393 at this point is higher than that of single diesel injection strategy.

394 Retarding post diesel injection timing in pre-main-post 1 test (Test 5) significantly increases NO<sub>x</sub> and GHG  
 395 emissions (Fig. 11b) of the NDDF engine. The NDDF engine emits 5.06 g/kW.h NO<sub>x</sub> emissions in pre-main-post 1 test  
 396 (Test 5) at the optimum point of GHG emissions (SODI-post = + 6 °ATDC), which is 618.61 g/kW.h and higher than  
 397 that of single diesel injection strategy. As shown in Fig. 11b, the NDDF engine can obtain the lowest NO<sub>x</sub> and GHG  
 398 emissions simultaneously in pre-main-post 3 test (Test 7), which are 4.01 g/kW.h and 600.68 g/kW.h, respectively,  
 399 at SODI-pre = - 80 °ATDC. These are almost 42% and 1.5% reductions, respectively, in NO<sub>x</sub> and GHG emissions  
 400 compared to those at the optimum point of GHG emissions in single diesel injection strategy.

401 Hence, the NDDF engine can achieve comparable or even better thermal efficiency and GHG emissions while  
 402 reducing unburned methane and NO<sub>x</sub> emissions by 13.4% and 42%, respectively and PPRR by 16.2% in the pre-main-  
 403 post injection 3 test (Test 7) compared to those at the optimum point of the NDDF engine with the single diesel  
 404 injection strategy.

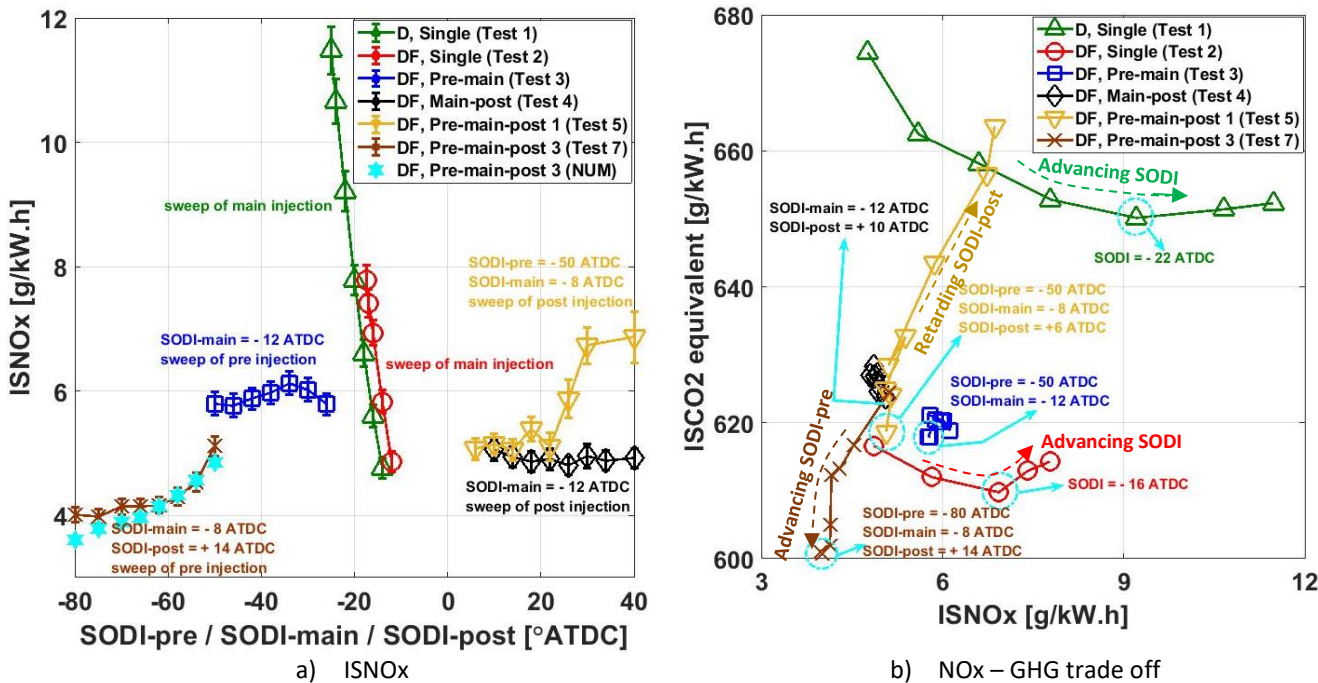


Fig. 11: NO<sub>x</sub> emissions and NO<sub>x</sub> – GHG trade off of NDDF engine with different diesel injection strategies.

405

406 **5. Conclusions**

407 The effect of pre-main-post diesel injection strategy on combustion performance and emissions of a NDDF engine  
408 at 50% natural gas energy fraction and high load conditions has been investigated with focus on further improving  
409 engine efficiency and GHG emissions.

410 The results reveal that the change in pre-diesel injection timing gives more controllability on the combustion  
411 phasing (start of combustion) than that in main and post diesel injection timings for pre-main-post injection strategy,  
412 since it modifies both fuel stratification and thermal conditions inside the combustion chamber before the start of  
413 combustion. It is found that a stratified premixed mixture of pre injected diesel – natural gas – air (e.g. SODI-pre = -  
414 50 °ATDC) leads to overly advanced combustion phasing which decreases the thermal efficiency of the NDDF engine  
415 with pre-main-post diesel injection strategy. However, a more homogenous premixed mixture of pre injected diesel  
416 – natural gas – air (e.g. SODI-pre = -80 °ATDC) retards the combustion phasing which allowed further improvement  
417 of the indicated thermal efficiency and GHG emissions of the NDDF engine while maintaining the low unburned  
418 methane emissions feature of the pre-main-post diesel injection strategy. The lowest GHG emissions of 600.68  
419 g/kW.h and the highest ITE of 41.09% were achieved in pre-main-post diesel injection strategy using very advanced  
420 pre diesel injection timing of -80 °ATDC. This is slightly better than the optimum point of the NDDF engine when  
421 using single diesel injection strategy (GHG = 609.77 g/kW.h and ITE = 40.72%). The emitted unburned methane  
422 emissions at this optimum point of GHG emissions was reduced by 13.4% compared that of the NDDF engine with  
423 single diesel injection strategy. Moreover, using pre-main-post diesel injection strategy decreased the PPRR and NO<sub>x</sub>  
424 emissions by 16.2% and 42%, respectively, compared to the optimum point of GHG emissions of the single diesel  
425 injection strategy.

426 **Acknowledgement**

427 Funding of the experimental and numerical works was provided by Natural Resources Canada through the PERD  
428 Energy End Use Program and National Research Council Canada (NRC) through the internal Advanced Clean Energy  
429 Program. The numerical simulation was supported by CONVERGENT Science Inc.

## Nomenclature

AMR	Adaptive Mesh Refinement
ATDC	After Top Dead Center
BMEP	Brake Mean Effective pressure
CA50	Crank Angle of 50% Cumulative Heat Release
CAD	Crank Angle Degree
CAI	California Analytical Instruments
CFD	Computational Fluid Dynamic
CH <sub>4</sub>	Methane
CI	Compression Ignition
CO	Carbon Monoxide
CO <sub>2</sub>	Carbon Dioxide
COV	Coefficient Of Variation
DAQ	Data Acquisition
DDM	Discrete Droplet Model
DI	Direct Injection
EC	Eddy Current
EODI	End Of Diesel Injection
EPA	Environmental Protection Agency
EVO	Exhaust Valve Opening
GHG	GreenHouse Gas
HRR	Heat Release Rate
ICE	Internal Combustion Engine
IMEP	Indicated Mean Effective Pressure
ISCH <sub>4</sub>	Indicated Specific CH <sub>4</sub>
ISCO <sub>2</sub>	Indicated Specific CO <sub>2</sub>
ISNO <sub>x</sub>	Indicated Specific NO <sub>x</sub>
ITE	Indicated Thermal Efficiency
IVC	Intake Valve Closing
KH-RT	Kelvin-Helmholtz Rayleigh-Taylor
LHV	Lower Heating Value
NDDF	Natural Gas Diesel Dual Fuel
NG	Natural Gas
NI	National Instrument
NO <sub>x</sub>	Nitrogen Oxides
PFI	Port Fuel Injection
PM	Particulate Matter
PPRR	Peak Pressure Rise Rate
PW	Pulse Width
PWR	Pulse Width Ratio
RPM	Revolution Per Minute
SOC	Start Of Combustion
SODI	Start Of Diesel Injection
UHC	Unburned Hydrocarbon
ULSD	Ultra-Low Sulfur Diesel

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