

NRC Publications Archive Archives des publications du CNRC

Nonlinear optomechanical paddle nanocavities

Kaviani, Hamidreza; Healey, Chris; Wu, Marcelo; Ghobadi, Roohollah; Hryciw, Aaron; Barclay, Paul E.

This publication could be one of several versions: author's original, accepted manuscript or the publisher's version. / La version de cette publication peut être l'une des suivantes : la version prépublication de l'auteur, la version acceptée du manuscrit ou la version de l'éditeur.

For the publisher's version, please access the DOI link below./ Pour consulter la version de l'éditeur, utilisez le lien DOI ci-dessous.

Publisher's version / Version de l'éditeur:

https://doi.org/10.1364/OPTICA.2.000271 Optica, 2, 3, pp. 271-274, 2015-03-20

NRC Publications Record / Notice d'Archives des publications de CNRC:

https://nrc-publications.canada.ca/eng/view/object/?id=78c9ef1d-4443-4bf0-a96f-609cea2c05b0 https://publications-cnrc.canada.ca/fra/voir/objet/?id=78c9ef1d-4443-4bf0-a96f-609cea2c05b0

Access and use of this website and the material on it are subject to the Terms and Conditions set forth at https://nrc-publications.canada.ca/eng/copyright

READ THESE TERMS AND CONDITIONS CAREFULLY BEFORE USING THIS WEBSITE.

L'accès à ce site Web et l'utilisation de son contenu sont assujettis aux conditions présentées dans le site https://publications-cnrc.canada.ca/fra/droits

LISEZ CES CONDITIONS ATTENTIVEMENT AVANT D'UTILISER CE SITE WEB.

Questions? Contact the NRC Publications Archive team at

PublicationsArchive-ArchivesPublications@nrc-cnrc.gc.ca. If you wish to email the authors directly, please see the first page of the publication for their contact information.

Vous avez des questions? Nous pouvons vous aider. Pour communiquer directement avec un auteur, consultez la première page de la revue dans laquelle son article a été publié afin de trouver ses coordonnées. Si vous n'arrivez pas à les repérer, communiquez avec nous à PublicationsArchive-ArchivesPublications@nrc-cnrc.gc.ca.





Letter Vol. 2, No. 3 / March 2015 / *Optica* 271

optica

Nonlinear optomechanical paddle nanocavities

Hamidreza Kaviani,^{1,2} Chris Healey,^{1,2} Marcelo Wu,^{1,2} Roohollah Ghobadi,³ Aaron Hryciw,^{1,4} and Paul E. Barclay^{1,2,*}

¹National Institute for Nanotechnology, Edmonton, Alberta T6G 2M9, Canada

²Department of Physics and Astronomy and Institute for Quantum Science and Technology, University of Calgary,

Calgary, Alberta T2N 1N4, Canada

³Institute of Atomic and Subatomic Physics, TU Wien, Stadionallee 2, 1020 Wien, Austria

⁴nanoFAB Facility, University of Alberta, Edmonton, Alberta T6G 2R3, Canada

*Corresponding author: pbarclay@ucalgary.ca

Received 22 December 2014; revised 13 February 2015; accepted 16 February 2015 (Doc. ID 230802); published 20 March 2015

Nonlinear optomechanical coupling is the basis for many potential future experiments in quantum optomechanics (e.g., quantum nondemolition measurements, preparation of nonclassical states), which to date have been difficult to realize due to small nonlinearity in typical optomechanical devices. Here we introduce an optomechanical system combining strong nonlinear optomechanical coupling, low mass, and large optical mode spacing. This nanoscale "paddle nanocavity" supports mechanical resonances with hundreds of femtograms of mass that couple nonlinearly to optical modes with a quadratic optomechanical coupling coefficient $g^{(2)} > 2\pi \times 400 \text{ MHz/nm}^2$, and a single-photon to twophonon optomechanical coupling rate of $\Delta\omega_0 > 2\pi \times 16$ Hz. This coupling relies on strong phonon-photon interactions in a structure whose optical mode spectrum is highly nondegenerate. Nonlinear optomechanical readout of thermally driven motion in these devices should be observable for T>50 mK, and measurement of phonon shot noise is achievable. This shows that strong nonlinear effects can be realized without relying on coupling between nearly degenerate optical modes, thus avoiding the parasitic linear coupling present in two-© 2015 Optical Society of America mode systems.

OCIS codes: (050.5298) Photonic crystals; (350.4238) Nanophotonics and photonic crystals; (120.4880) Optomechanics; (130.3120) Integrated optics devices; (130.4310) Nonlinear.

http://dx.doi.org/10.1364/OPTICA.2.000271

The study of the quantum properties of mesoscopic mechanical systems is a rapidly evolving field that has been propelled by recent advances in the development of cavity optomechanical devices [1]. Nanophotonic cavity optomechanical structures [2] allow colocalization of photons and femtogram-to-picogram mechanical excitations, and have enabled demonstrations of ultrasensitive displacement and force detection [3–7], ground-state cooling [8], and optical squeezing [9]. The development of cavity optomechanical systems with large nonlinear photon–phonon

coupling has been motivated by quantum nondemolition (QND) measurement of phonon number $[\underline{10}]$ and shot noise $[\underline{11}]$, as well as mechanical quantum-state preparation $[\underline{12}]$, the study of photon–photon interactions $[\underline{13}]$, mechanical squeezing and cooling $[\underline{14}-\underline{16}]$, and phonon–photon entanglement $[\underline{17}]$.

Recent progress in developing optomechanical systems with large nonlinear optomechanical coupling has been driven by studies of membrane-in-the-middle (MiM) [18-21] and whispering gallery mode [12,22,23] cavities. Demonstrations of massively enhanced quadratic coupling [19,21,22] have exploited avoided crossings between nearly degenerate optical modes, and have revealed rich multimode dynamics [21]. To surpass bandwidth limits [13,24] and parasitic linear coupling [25] imposed by closely spaced optical modes, it is desirable to develop devices that combine strong nonlinear coupling and large optical mode spacing. This can be achieved in short, low-mass, high-finesse optical cavities. In this Letter, we present such a nanocavity optomechanical system, which couples modes possessing low optical loss and terahertz free spectral range to mechanical resonances with femtogram mass, 300 kHz-220 MHz frequency, and large zero point fluctuation amplitude. This device has vanishing linear and large nonlinear optomechanical coupling, with a quadratic optomechanical coupling coefficient $g^{(2)} \approx 2\pi \times 400 \text{ MHz/nm}^2$ and a singlephoton to two-phonon coupling rate of $\Delta\omega_0 = 2\pi \times 16$ Hz.

The strength of photon–phonon interactions in nanocavity–optomechanical systems is determined by the modification of the optical mode dynamics via deformations to the nanocavity dielectric environment from excitations of mechanical resonances. In systems with dominantly dispersive optomechanical coupling, this dependence is expressed to second order in mechanical resonance amplitude x as $\omega_o(x) = \omega_0 + g^{(1)}x + \frac{1}{2}g^{(2)}x^2$, where ω_o is the cavity resonance frequency, and $g^{(1)} = \delta \omega_o/\delta x$, $g^{(2)} = \delta^2 \omega_o/\delta x^2$ are the first- and second-order optomechanical coupling coefficients. In nanophotonic devices, x parameterizes a spatially varying modification to the local dielectric constant, $\Delta \epsilon(\mathbf{r};x)$, whose distribution depends on the mechanical resonance shape and is responsible for modifying the frequencies of the nanocavity optical resonances.

Insight into nonlinear optomechanical coupling in nanocavities is revealed by the dependence of $\delta\omega^{(2)}$ on the overlap between $\Delta\varepsilon$ and the optical modes of the nanocavity [26,27]:

$$g^{(2)} = \frac{\omega}{2} \frac{|\langle E_{\omega} | \frac{\delta \epsilon}{\delta x} | E_{\omega} \rangle|^2}{|\langle E_{\omega} | \epsilon | E_{\omega} \rangle|^2} + \sum_{\omega' \neq \omega} g_{\omega', \omega}^{(2)}.$$
 (1)

Here the first term is a "self-term" and $g_{\omega',\omega}^{(2)}$ represents cross couplings between the fundamental mode of interest (ω) and other modes supported by the cavity (ω') :

$$g_{\omega',\omega}^{(2)} = -\left(\frac{\omega^3}{\omega'^2 - \omega^2}\right) \frac{|\langle E_{\omega'}| \frac{\delta \epsilon}{\delta x} |E_{\omega}\rangle|^2}{\langle E_{\omega'}| \epsilon |E_{\omega'}\rangle \langle E_{\omega}| \epsilon |E_{\omega}\rangle}.$$
 (2)

Here E_{ω} denotes the electric field of a nanocavity mode at frequency ω , and the inner product is an overlap surface integral defined in Ref. [26] and developed in the context of optomechanics in Refs. [27,28] (see Supplement). In cavity optomechanical systems with no linear coupling ($g^{(1)} = 0$), the contribution in Eq. (1) from the self-overlap of the dielectric perturbation vanishes, and the quadratic coupling is determined entirely by mechanically induced cross coupling between the nanocavity's optical modes. Enhancing this coupling can be realized in two ways. In the first approach, demonstrated in Refs. [18-21], the factor $\omega^3/(\omega'^2-\omega^2)$ can be enhanced in a cavity with nearly degenerate modes ($\omega \sim \omega'$), which are coupled by a mechanical perturbation. An alternative approach that is desirable to avoid multimode dynamics $[\underline{21}]$ is to maximize the $g^{(2)}_{\omega',\omega}$ overlap terms. Here we investigate this route, and present a system with optical modes isolated by terahertz in frequency that possesses high quadratic optomechanical coupling owing to a strong overlap between optical and mechanical fields.

The optomechanical device studied here, illustrated in Fig. 1, is a photonic crystal "paddle nanocavity" that combines operating principles of MiM cavities [10,29] and photonic crystal nanobeam optomechanical devices [2]. The device is designed to be fabricated from silicon-on-insulator (refractive index $n_{\rm Si} = 3.48$, thickness t = 220 nm), and to support modes near $\lambda \sim 1550$ nm. A "paddle" element is suspended within the optical mode of the nanocavity defined by two photonic crystal nanobeam mirrors. The width of the gap (d = 50 nm) separating the mirrors from the paddle is chosen for smooth variation in the local effective index of the structure [30], and the paddle length (L = 958 nm) is set to $\approx 1.5 \lambda / n_{\rm eff}$ [31]. This allows the

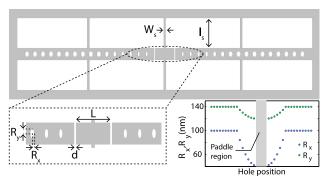


Fig. 1. Schematic of the photonic crystal paddle nanocavity (topview). The paddle is separated from photonic crystal nanobeam mirrors by gaps d=50 nm, and has length L=958 nm. The elliptical hole horizontal and vertical semiaxes (R_x, R_y) are tapered as shown.

nanocavity to support high optical quality factor (Q_o) modes. The length (l_s) and width (w_s) of the paddle supports can be adjusted to tailor its mechanical properties, although $l_s \geq 200$ nm and $w_s \leq 200$ nm are required to not degrade Q_o . We consider three support geometries, labeled p1-p3 (see Fig. 2(c) for dimension). All of these dimensions are realizable experimentally [7].

Figure 2(a) shows the first seven localized optical modes supported by the paddle nanocavity, calculated using finite element simulations (FEM). COMSOL software was used for all FEM simulations. The lowest-order mode (M1) has a resonance wavelength near 1550 nm ($\omega_o/2\pi=191$ THz) and $Q_o>1.3\times10^4$. The mechanical resonances of the paddle nanocavity were also calculated using FEM simulations, and the displacement profiles of the four lowest mechanical frequency resonances are shown in Fig. 2(b). They are referred to here as "sliding" (S), "bouncing" (B), "rotational" (\mathcal{R}), and "torsional" (\mathcal{T}) resonances. As discussed below, we are particularly interested in the ${\cal S}$ resonance, whose frequency and effective mass [28] varies between $f_m = 0.35-217$ MHz and m = 314-589 fg for the support geometries p1-p3, as described in Fig. 2(b). Appropriate selection of geometry p1-p3 depends on the application, with p1 suited for sensitive actuation, p2 a compromise between ease of fabrication and sensitivity, and p3 for high-frequency operation and low thermal phonon occupation.

The spatial symmetry of the nanocavity results in vanishing $g^{(1)}$ for the mechanical resonances considered here. The intensity $E^2(x,y,z)$ of each nanocavity optical mode has even symmetry, denoted $\sigma_{x,y,z}=1$, while the mechanical resonances induce perturbation $\Delta \varepsilon$, which is odd in at least one direction, characterized by $\sigma_x=-1$ (\mathcal{S},\mathcal{R}), $\sigma_y=-1$ (\mathcal{R}), or $\sigma_z=-1$ (\mathcal{B},\mathcal{T}). As a result, $g^{(1)} \propto \langle E_\omega | \delta \varepsilon | E_\omega \rangle = 0$. Similarly, the second-order self-overlap term in Eq. (1) is also zero. However, the electric field amplitude E(x,y,z) may be even or odd, resulting in nonzero cross coupling

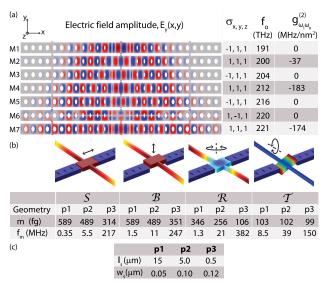


Fig. 2. (a) Properties of the localized optical modes of the paddle nanocavity (labeled M1–M7): electric field distribution (E_y) component), spatial symmetry in x-y plane, optical frequency, and contribution $g_{(p),u_n}^{(2)}$ to the quadratic optomechanical coupling $g^{(2)}$ describing interaction between mode M1 and the S mechanical resonance shown in (b). (b) Displacement profiles and properties of the paddle nanocavity mechanical resonances. m and f_m are indicated for three support geometries, p1-p3, whose cross sections are given in (c).

 $g_{\omega',\omega}^{(2)}$ between optical modes with opposite $\sigma_{x,y,z}$. For example, displacement in the \hat{x} direction of S couples optical modes with opposite σ_x . In contrast, displacement in the \hat{z} direction by the \mathcal{B} and T resonances does not induce cross coupling, as the localized optical modes all have even vertical symmetry ($\sigma_z = 1$). Here we focus on the nonlinear coupling between the ${\cal S}$ resonance and the *M*1 mode of the nanocavity.

To evaluate $g_{\omega,\omega'}^{(2)}$, the mechanical and optical field profiles were input into Eq. (2). The resulting contributions $g_{\omega_1\omega_n}^{(2)}$ of each localized mode to $g^{(2)}$ for optomechanical coupling between the ${\cal S}$ resonance and the M1 mode are summarized in Fig. 2(a). Contributions from delocalized modes are neglected due to their large mode volume and low overlap. The imaginary part of ω_o , which is small for the localized modes whose $Q_a > 10^2$, is also ignored. A total $g^{(2)}/2\pi \approx -400 \text{ MHz/nm}^2$ is predicted, which matches with our direct FEM calculations (see Supplement). The corresponding single-photon to two-phonon coupling rate, $\Delta\omega_o$, depends on the support geometry. For the most flexible p1 geometry, $\Delta \omega_o \equiv |g^{(2)} x_{zpf}^2| = 2\pi \times 16 \text{ Hz}$, where $x_{zpf} =$ $\sqrt{\hbar/2m\omega_m}$. This $\Delta\omega_o$ is about four orders of magnitude higher than typical MiM systems [18,21], while the mode spacing is five orders of magnitude higher than other nonlinear optomechanical systems [13,18,22]. The dominant contributions to $g^{(2)}$ arise from cross coupling between modes $M1 \leftrightarrow M4$ and $M1 \leftrightarrow M7$ due to strong spatial overlap between their fields and the paddle-nanobeam gaps. Increasing $g^{(2)}$ through additional optimization, for example, by concentrating the optical field more strongly in the gap, should be possible.

Given $g^{(2)}$ of the paddle nanocavity, the optical response of the device can be predicted. In experimental applications of optomechanical nanocavities, photons are coupled into and out of the nanocavity using an external waveguide. Mechanical fluctuations, x(t), are monitored via variations, dT(t), of the waveguide transmission, T. In the sideband unresolved regime ($\omega_m \ll \omega_o/Q_o$), optomechanical coupling results in a fluctuating waveguide output $dT = G_1 x(t) + \frac{1}{2} G_2 x(t)^2$, where

$$G_1 = \frac{dT}{dx} = g^{(1)}\frac{dT}{d\Delta},\tag{3}$$

$$G_2 = \frac{d^2T}{dx^2} = g^{(2)}\frac{dT}{d\Delta} + (g^{(1)})^2\frac{d^2T}{d\Delta^2}.$$
 (4)

Here $\Delta = \omega - \omega_o$ is the detuning between input photons and the nanocavity mode, and $dT/d\Delta$ and $d^2T/d\Delta^2$ are the slope and curvature of the Lorentzian cavity resonance in $T(\Delta)$. Equation (4) shows that in general, both nonlinear transduction of linear optomechanics and linear transduction of nonlinear optomechanics contribute to the second-order signal. The nonlinear mechanical displacement can be measured through photodetection of the waveguide optical output. For input power P_i , the waveguide output optical power spectral density (PSD) due to transduction of $x^{2}(t)$ is $S_{p}^{(2)}(\omega) = \frac{1}{4}P_{i}^{2}G_{2}^{2}S_{x^{2}}(\omega)$, where $S_{x^{2}}(\omega)$ is the PSD of the x^2 mechanical motion of the mechanical resonance. To analyze the possibility of observing this signal, it is instructive to consider the scenario of a thermally driven mechanical resonance. As shown in the Supplement and Refs. [15,32], $S_{x^2}(\omega)$ of a resonator in an \bar{n} phonon number thermal state is

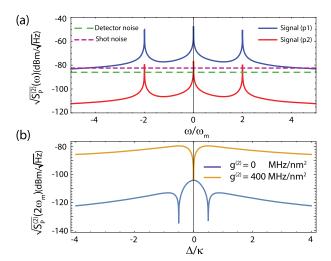


Fig. 3. (a) $S_p^{(2)}(\omega)$ generated by thermal motion of the S mode of a paddle nanocavity for p1 and p2 support geometry, assuming room temperature operation, $\Delta = \kappa/2$, $P_i = 100 \,\mu\text{W}$, and $Q_m = 10^3$. (b) $S_P^{(2)}(2\omega_m)$ as a function of detuning Δ , for varying quadratic coupling strengths $g^{(2)}$.

$$S_{x^{2}}(\omega) = 2x_{zpf}^{4} \left(\frac{2\Gamma(\bar{n}+1)^{2}}{\Gamma^{2} + (\omega - 2\omega_{m})^{2}} + \frac{2\Gamma\bar{n}^{2}}{\Gamma^{2} + (\omega + 2\omega_{m})^{2}} + \frac{8\Gamma\bar{n}(\bar{n}+1) + 1}{\Gamma^{2} + \omega^{2}} \right),$$
(5)

where $\Gamma = \omega_m/Q_m$ and Q_m is the mechanical quality factor. Figure $\underline{3(a)}$ shows $S_p^{(2)}(\omega)$ predicted from Eq. (5), for the Smode of a paddle nanocavity at room temperature (T_b = 300 K). The input optical field is set to $P_i = 100 \mu W$, with detuning $\Delta = \kappa/2$ to maximize the nonlinear optomechanical coupling contribution. The predicted $S_p^{(2)}(\omega)$ is shown for p1and p2 support geometries, assuming $Q_m = 10^3$, $Q_o =$ 1.4×10^4 , and relatively weak fiber coupling $T_o = 0.90$. Note that Q_m is specified assuming the device is operating in moderate vacuum conditions [7], and can increase to 10⁵ in cryogenic vacuum conditions [9]. Also shown are estimated noise levels, assuming direct photodetection using a Newport 1811 photoreceiver (NEP = 2.5 pW/Hz). Resonances in $S_p^{(2)}$ are evident at $\omega =$ $2\omega_m$ and $\omega=0$, corresponding to energies of the two-phonon processes characteristic of x^2 optomechanical coupling. Figure 3 suggests that even for these relatively modest device parameters, the nonlinear signal at $2\omega_m$ is observable. This signal can be further enhanced with improved device performance. For example, if $Q_m = 10^4$, the nonlinear signal is visible for temperatures as low as 50 mK for the p1 geometry. Note that additional technical noise will increase as f_m is further decreased into the kilohertz range.

Nonlinear optomechanical coupling can be differentiated from nonlinear transduction by the Δ dependence of the nonlinear signal. This is demonstrated in Fig. 3(b), which shows $S_p^{(2)}(2\omega_m, \Delta)$ with and without quadratic coupling, assuming that fabrication imperfections introduce nominal $g^{(1)}/2\pi = 50 \text{MHz/nm}$. This demonstrates that at $\Delta = \kappa/2$, the nonlinear signal is dominantly from nonlinear optomechanical coupling.

Next we study the feasibility of QND phonon measurement using a paddle nanocavity. High ω_m is advantageous for

ground-state cooling, which is required for QND measurements. The large optical mode spacing of the paddle nanocavity allows this without introducing Zener tunneling effects [13] or parasitic linear coupling and resulting backaction [25]. Cryogenic temperature of 10 mK could directly cool the S resonance of the p3structure to its quantum ground state. For feasible optical and mechanical quality factors $Q_o = 10^6 \ [\underline{8,30}]$ and $Q_m = 10^5$ [9], the signal-to-noise ratio (SNR) introduced in Ref. [10] of a quantum jump measurement in such a device is $\overline{\Sigma^{(0)}} = \tau_{\rm tot}^{(0)} \Delta \omega_0^2 / S_{\omega_o} = 6.4 \times 10^{-8}$. Here $\tau_{\rm tot}^{(0)}$ is the thermal lifetime quantifying the rate of decoherence due to bath phonons of the ground-state-cooled nanomechanical resonator, and S_{ω} is the shot-noise-limited sensitivity of an ideal Pound-Drever-Hall detector. Introducing laser cooling would potentially allow preparation of the p1 device to its quantum ground state, where the larger x_{zpf} and $\Delta \omega_o$ increase $\Sigma^{(0)}$ to 2.1×10^{-5} . However, this would require development of sideband unresolved nonlinear optomechanical cooling [15].

A more feasible approach for observing discreteness of the paddle nanocavity mechanical energy is a QND measurement of phonon shot noise [11]. The SNR of such a measurement scales with the magnitude of an applied drive, which enhances the signal by $S = 8n_d \bar{n} \Sigma^{(0)}$, where n_d is the drive amplitude in units of phonon number, and $\bar{n} < 1$ for a resonator in the quantum ground state. Using a p3 structure, SNR of more than 1 is achievable assuming a drive amplitude of 62 pm $(n_d \approx 7.8 \times 10^6)$ and thermal bath phonon number $\bar{n} = 1/4$.

In conclusion, we have designed a single-mode nonlinear optomechanical nanocavity with terahertz mode spacing. The quadratic optomechanical coupling coefficient $g^{(2)}/2\pi=400~\mathrm{MHz/nm^2}$ and single-photon to two-phonon coupling rate $\Delta\omega_0/2\pi=16~\mathrm{Hz}$ of this system are among the largest single-mode quadratic optomechanical couplings predicted to date. Observing a thermal nonlinear signal from this structure is possible in realistic conditions, and continuous QND measurements of phonon shot noise may be achievable for optimized device parameters. We acknowledge support from:

Alberta Innovates - Technology Futures; Canada Foundation for Innovation (CFI); Natural Sciences and Engineering Research Council of Canada (NSERC); WWTF; Austrian Science Fund (FWF) through SFB FoQuS; START (Y 591-N16).

See Supplement for supporting content.

REFERENCES

- M. Aspelmeyer, T. J. Kippenberg, and F. Marquardt, Rev. Mod. Phys. 86, 1391 (2014).
- M. Eichenfield, J. Chan, R. Camacho, K. Vahala, and O. Painter, Nature 462, 78 (2009).

- E. Gavartin, P. Verlot, and T. J. Kippenberg, Nat. Nanotechnol. 7, 509 (2012).
- A. G. Krause, M. Winger, T. D. Blasius, W. Lin, and O. Painter, Nat. Photonics 6, 768 (2012).
- Y. Liu, H. Miao, V. Aksyuk, and K. Srinivasan, Opt. Express 20, 18268 (2012).
- X. Sun, J. Zhang, M. Poot, C. W. Wong, and H. X. Tang, Nano Lett. 12, 2299 (2012).
- M. Wu, A. C. Hryciw, C. Healey, D. P. Lake, H. Jayakumar, M. R. Freeman, J. P. Davis, and P. E. Barclay, Phys. Rev. X 4, 021052 (2014).
- J. Chan, T. P. M. Alegre, A. H. Safavi-Naeini, J. T. Hill, A. Krause, S. Groblacher, M. Aspelmeyer, and O. Painter, Nature 478, 89 (2011).
- A. H. Safavi-Naeini, S. Gröblacher, J. T. Hill, J. Chan, M. Aspelmeyer, and O. Painter, Nature 500, 185 (2013).
- J. D. Thompson, B. M. Zwickl, A. M. Jayich, F. Marquardt, S. M. Girvin, and J. G. E. Harris, Nature 452, 72 (2008).
- A. A. Clerk, F. Marquardt, and J. G. E. Harris, Phys. Rev. Lett. 104, 213603 (2010).
- G. A. Brawley, M. R. Vanner, P. E. Larsen, S. Schmid, A. Boisen, and W. P. Bowen, "Non-linear optomechanical measurement of mechanical motion," arXiv:1404.5746 (2014).
- M. Ludwig, A. H. Safavi-Naeini, O. Painter, and F. Marquardt, Phys. Rev. Lett. 109, 063601 (2012).
- M. Bhattacharya, H. Uys, and P. Meystre, Phys. Rev. A 77, 033819 (2008).
- A. Nunnenkamp, K. Børkje, J. G. E. Harris, and S. M. Girvin, Phys. Rev. A 82, 021806 (2010).
- C. Biancofiore, M. Karuza, M. Galassi, R. Natali, P. Tombesi, G. Di Giuseppe, and D. Vitali, Phys. Rev. A 84, 033814 (2011).
- 17. J.-Q. Liao and F. Nori, Sci. Rep. 4, 6302 (2014).
- J. C. Sankey, C. Yang, B. M. Zwickl, A. M. Jayich, and J. G. E. Harris, Nat. Phys. 6, 707 (2010).
- N. Flowers-Jacobs, S. Hoch, J. Sankey, A. Kashkanova, A. Jayich, C. Deutsch, J. Reichel, and J. Harris, Appl. Phys. Lett. 101, 221109 (2012).
- M. Karuza, M. Galassi, C. Biancofiore, C. Molinelli, R. Natali, P. Tombesi,
 G. Di Giuseppe, and D. Vitali, J. Opt. 15, 025704 (2013).
- D. Lee, M. Underwood, D. Mason, A. Shkarin, S. Hoch, and J. Harris, "Multimode optomechanical dynamics in a cavity with avoided crossings," arXiv:1401.2968 (2014).
- J. T. Hill, "Nonlinear optics and wavelength translation via cavityoptomechanics," Ph.D. thesis (California Institute of Technology, 2013).
- C. Doolin, B. Hauer, P. Kim, A. MacDonald, H. Ramp, and J. Davis, Phys. Rev. A 89, 053838 (2014).
- 24. G. Heinrich, J. Harris, and F. Marquardt, Phys. Rev. A 81, 011801 (2010).
- H. Miao, S. Danilishin, T. Corbitt, and Y. Chen, Phys. Rev. Lett. 103, 100402 (2009).
- S. G. Johnson, M. Ibanescu, M. A. Skorobogatiy, O. Weisberg, J. D. Joannopoulos, and Y. Fink, Phys. Rev. E 65, 066611 (2002).
- A. W. Rodriguez, A. P. McCauley, P.-C. Hui, D. Woolf, E. Iwase, F. Capasso, M. Loncar, and S. G. Johnson, Opt. Express 19, 2225 (2011).
- M. Eichenfield, J. Chan, A. H. Safavi-Naeini, K. J. Vahala, and O. Painter, Opt. Express 17, 20078 (2009).
- A. Jayich, J. Sankey, B. Zwickl, C. Yang, J. Thompson, S. Girvin,
 A. Clerk, F. Marquardt, and J. Harris, New J. Phys. 10, 095008 (2008).
- 30. A. C. Hryciw and P. E. Barclay, Opt. Lett. 38, 1612 (2013).
- Q. Quan, P. B. Deotare, and M. Loncar, Appl. Phys. Lett. 96, 203102 (2010).
- B. Hauer, J. Maciejko, and J. Davis, "Nonlinear power spectral densities for the harmonic oscillator," arXiv:1502.02372 (2015).